

A rolling horizon approach for shunting operations – An emission oriented simulation study

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ABSTRACT

Marshalling yards are nodes in rail networks to sort railcars from incoming trains to outgoing trains. To build outgoing trains in the correct sequence, railcars are shunted by shunting locomotives. Thereby, green house gas emissions are emitted as those locomotives are usually diesel powered. As the planning of shunting operations is a very complex problem, heuristics, so-called sorting strategies, are applied in practice. In this paper the effects of practically relevant sorting strategies on green house gas emissions are studied in a rolling horizon model. The rolling horizon model is used in a simulation study to investigate the effects of sorting strategies and input parameters (like the number and composition of ingoing and outgoing trains) on green house gas emissions. The results indicate that for different parameter constellations, different emission-optimal sorting strategies exist. Thus, sorting strategy selection should be done carefully depending on the operational conditions at the shunting yards.

1. Introduction

Sustainability is a major issue in transportation research, see [de Dios Ortúzar \(2021\)](#). Regarding the rail freight transportation the use of electric locomotives is typically in railway transportation and more eco-friendly than most other means of transport, but diesel-powered locomotives are still in use which are much less eco-friendly. Particularly in marshalling yards often diesel-powered shunting locomotives are used which produce considerable amounts of greenhouse gas (GHG) emissions. Although there are technological alternatives to diesel-powered shunting locomotives (like battery-electric or fuel-cell powered locomotives), conventional shunting locomotives are still the dominating means of transport in marshalling yards ([Bundesnetzagentur, 2021](#)). To minimize total emissions from rail transportation also GHG emissions in marshalling yards need to be considered. Next to using “I”ocomotives, shunting emissions can also be reduced by considering GHG emissions in shunting operations planning, i.e., when planning how to sort and schedule railcars.

Railcar sorting at shunting yards aims at assembling railcars in the correct order in their dedicated outbound trains. Railcars arrive in inbound trains and are assigned to the receiving tracks. A “r”efers to all railcars assigned to a specific receiving track, see [Fig. 1 \(Boysen et al.,](#)

[2012\)](#). Once a cut is complete, all railcars are decoupled and shunted by locomotives over the hump from where they roll into the classification tracks (so-called “j”). Usually, on each classification track one outbound train is built. If after humping the sequence of railcars assigned to a classification track does not match the corresponding outbound train’s target configuration, the railcars have to be (“also called “j”). I.e., all railcars assembled on a classification track are moved back to the receiving area and humped again. Usually, railcars have to be humped multiple times before all outbound trains are assembled completely and correctly as usually the sequences of incoming railcars do not match the required outbound sequences.

In general marshalling yards consist of receiving, classification and departure tracks for the arrival of incoming trains, sorting railcars and building outgoing trains, respectively. In the remainder of this article the layout refers to one of the most up-to-date marshalling yard in Germany, the marshalling yard in Halle (Saale), i.e. no departure tracks are available ([DB Netz AG, 2022](#)). If no departure tracks are available, trains are sorted and built directly on classification tracks. This implies that completely assembled outbound trains block classification tracks until their departure. A different treatment of no departure tracks results in the arrival and departure on the receiving tracks, see [Gestrelius \(2022\)](#). A different layout comprises two yards in opposite direction, see [Otto](#)

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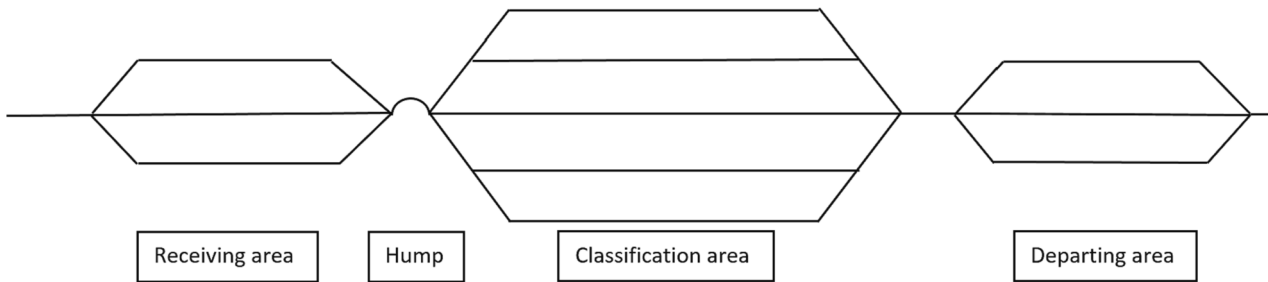


Fig. 1. Schematic layout of a marshalling yard with hump, incoming trains arrive at the receiving area, railcars are sorted in the classification area and outgoing trains are prepared for departure in the departing area.

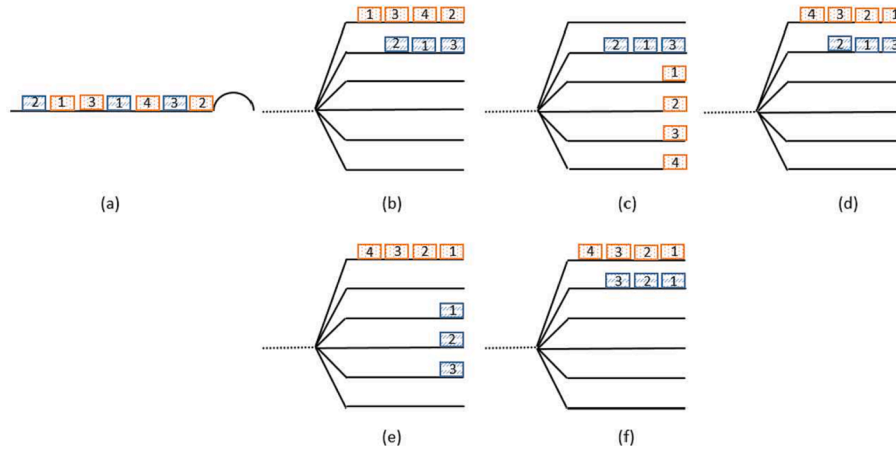


Fig. 2. Example for Sorting by train, (a) Initial situation (7 blocks, dedicated to two trains distinguished by hatching), (b) situation after initial humping, (c) 1st pullback & rehumping: split dot hatched train, (d) second pullback & rehumping: sequence dot hatched train, (e)/(f) splitting & sequencing zigzag hatched train.

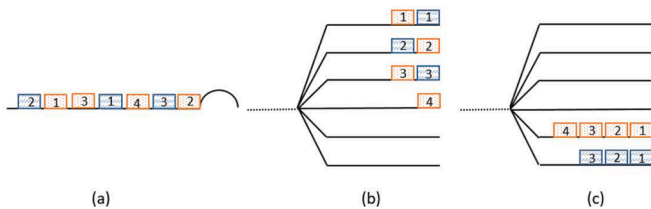


Fig. 3. Example for Sorting by block, (a) Initial situation (7 blocks, dedicated to two trains distinguished by hatching), (b) Initial humping: Sorting by block number, (c) Final result after 4 pullbacks.

and Pesch (2017) or two humps and no departure tracks, see Márton et al. (2009). The marshalling yard layout can also transfer to other facilities, see Jaehn et al. (2017). The authors interpret the layout of a railcar workshop as the layout of a flat yard (marshalling yard without hump).

Multi-stage sorting strategies are procedures to assign railcars to classification tracks efficiently such that e.g. rehumping is minimized, outbound trains are built on time, etc. Usually, railcars with the same destination and, thus, position in an outbound train are grouped into so-called “(Gatto et al., 2009)”. Therefore, in the following we refer to the units to be sequenced in outbound trains as blocks. Another objective is to minimize the number of used tracks, see Gatto et al. (2009).

Zien and Kirschstein (2021) studies GHG emissions of shunting operations for a set of simple railcar sorting strategies. Those sorting strategies are rule-based procedures to reassemble groups of railcars from incoming trains into outbound trains, see Boysen et al. (2012), Maue (2011) and Jacob et al. (2010). Because those sorting strategies

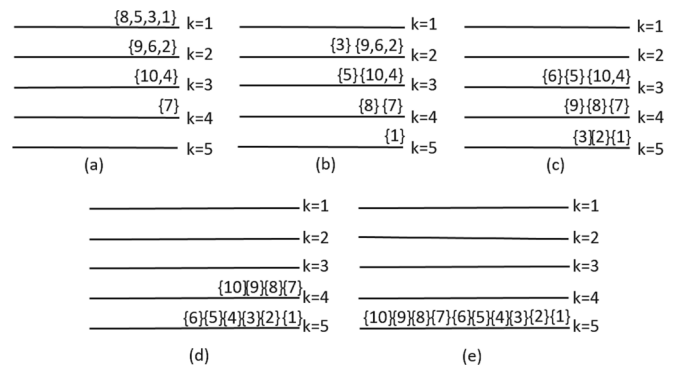


Fig. 4. Triangular Sorting: (a) Initial assignment of first 10 blocks, $k = 1, \dots, 4$ represents the classification tracks for sorting, track $k = 5$ is used to build one outbound train, (b)–(e) Sorting blocks to classification tracks with the final outbound train in (e) on track $k = 5$.

neglect the fact of time it is assumed that the whole set of incoming trains arrive in the marshalling yard before shunting starts, i.e. only one humping process is considered. In Zien and Kirschstein (2021) analytical emission functions for each sorting strategy are deduced for calculating GHG emissions. The analyses show that GHG emissions of the considered sorting strategies vary quite heavily depending on the structure of the problem instance regarding incoming and outgoing rail group composition. In this paper, the model of Zien and Kirschstein (2021) is extended by embedding the sorting strategies in a rolling horizon approach as it is common in practice. Therefore, incoming trains arrive at the marshalling yard at different points in time, i.e. humping of the

incoming trains and shunting of the blocks to outgoing trains rotate. Depending on the outbound train schedules, the sorting strategies are applied in regular intervals to sort and reassemble railcars such that outbound trains are built. Additionally to the sorting strategies studied in Zien and Kirschstein (2021), parallel pullback sorting is considered which can deal with a limited number of classification tracks explicitly. For all considered sorting strategies emission functions are deduced analytically. The effects of problem instance parameters (like number and composition of incoming trains/outgoing trains, ...) on a sorting strategies' total GHG emissions are analysed by systematically varying those parameters in a simulation study.

The paper is structured as follows. In Section 2 five sorting strategies are formally described. Additionally, a rolling horizon model is derived for each sorting strategy. The underlying emission model to calculate GHG emissions is briefly reviewed in Section 3. The simulation study and results are presented in Section 4. A summary of the paper and an outlook are given in Section 5.

2. Shunting operations in a rolling horizon setting

In this section the five sorting strategies *sorting by train* (SBT), *sorting by block* (SBB), *triangular sorting* (TS), *geometric sorting* (GS), and *parallel pullback sorting* (PPS) are introduced. In Subsection 2.1 shunting performance functions for each sorting strategy are presented. Adapting the performance functions of all sorting strategies to a rolling horizon approach is explained in Subsection 2.2.

2.1. Description of sorting strategies

In Gatto et al. (2009) several sorting strategies for sorting blocks in marshalling yards are proposed. One of them is *Sorting by train* (SBT). The main idea of SBT is to sort blocks on classification tracks according

corresponding classification track, all railcars are pulled back and humped again. Thereby each block is assigned to an empty classification track. Finally, the blocks are pulled back one more time according to their order number w . Thus, each block is humped three times when applying SBT. Fig. 2 illustrates the procedure for an example with two trains.

Applying *Sorting by block* (SBB), see Gatto et al. (2009), means to sort all blocks to the classification tracks based on their order numbers w irrespective of their outbound train r . I.e., all blocks with the same order number are shunted to the same classification track. Subsequently, the blocks are pulled back sequentially starting with blocks $w = 1$. When rehumping, each outbound train is assigned to a classification track and the corresponding blocks are shunted accordingly. Thus, each block is humped twice. An example is displayed in Fig. 3.

SBT and SBB are simple sorting rules, but require many classification tracks if the number of blocks or the number of outbound trains is large. In Gatto et al. (2009) and Daganzo et al. (1983) a more complex method, called *Triangular sorting* (TS), can be found which requires less classification tracks.

The basic idea of TS is to sort blocks regarding a triangular sorting plan, see (a) to (d) in Fig. 4. For this purpose the number of blocks for each track has to be determined. Blocks of outgoing trains $r = 1, \dots, m$ are numbered from 1 to n_r and hence, $\tilde{w}_{max} = \{n_r | r = 1, \dots, m\}$ denotes the highest block number over all outgoing trains, while k denotes the index of the classification tracks and $\tilde{\mathcal{W}}_k^{TS}$ denotes the set of blocks assigned to classification track k , e.g. for $\tilde{w}_{max} = 10$ the initially shunted blocks to track $k = 2$ are blocks 2, 6 and 9. In TS, similar to SBB, blocks are assigned to classification tracks based on their order (irrespective of their outbound train). Blocks are assigned to $\tilde{\mathcal{W}}_k^{TS}$ according to the following scheme

$$\tilde{\mathcal{W}}_k^{TS} = \begin{cases} \emptyset & \text{for } \tilde{w}_{max} < \frac{k(k-1)}{2} + 1 \\ \frac{k \cdot (k-1)}{2} + 1 & \text{for } \frac{k(k-1)}{2} + 1 \leq \tilde{w}_{max} < \frac{k(k-1)}{2} + 1 + 2k \\ \frac{k \cdot (k-1)}{2} + 1, g_2^k, \dots, g_{j_k}^k & \text{for } \frac{k(k-1)}{2} + 1 + 2k \leq \tilde{w}_{max} \end{cases} \quad (1)$$

to their corresponding outbound train r . I.e., first all blocks of an outbound train are assigned to the same classification track irrespective of their order w . Once all blocks of the outbound train are waiting on the

whereby

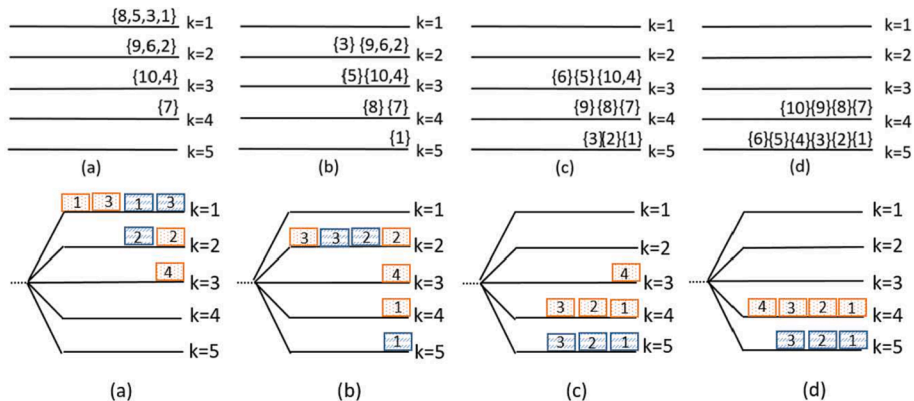


Fig. 5. Example for TS/GS: (a) Initial humping (7 blocks, dedicated to two trains distinguished by hatching), $k = 1, 2, 3$ represents the classification tracks for sorting, $k = 4, 5$ are used to build two outbound trains, (b)–(d) Sorting regarding general scheme of TS/GS, see Fig. 4 or Fig. 6, (d) Final result after 3 pullbacks.

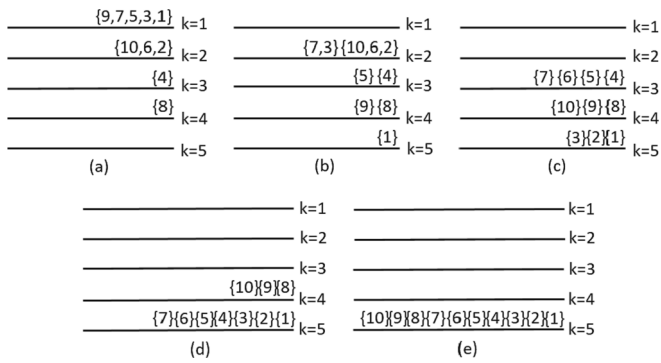


Fig. 6. Geometric Sorting: (a) Initial assignment of first 10 blocks, $k = 1, \dots, 4$ represents the classification tracks for sorting, track $k = 5$ is used to build one outbound train, (b)–(e) Sorting blocks to classification tracks with the final outbound train in (e) on track $k = 5$.

$$g_j^k = \frac{k \cdot (k - 1)}{2} + j \cdot k + 1 + \frac{(j - 1) \cdot (j - 2)}{2} \quad (2)$$

and

$$\bar{j}_k^{TS} = \lfloor -k + \frac{3}{2} + \frac{\sqrt{-8 \cdot k - 7 + 8 \cdot \tilde{w}_{max}}}{2} \rfloor \quad (3)$$

Determining the last block g_s^k which can be shunted on track k for a given maximum block number \tilde{w}_{max} results in calculating index $s \in \mathbb{R}_+$ such that $g_s^k - \tilde{w}_{max} = 0$ holds. The result s is not applicable in practice because only integer indices, i.e. integer block numbers, are applicable.

Hence, $\bar{j}_k^{TS} \in \mathbb{N}$ holds and equation $\lfloor -k + \frac{3}{2} + \frac{\sqrt{-8 \cdot k - 7 + 8 \cdot \tilde{w}_{max}}}{2} \rfloor$ is derived.

Afterwards initial humping according to the aforementioned scheme, the blocks are pulled back and humped again sequentially starting with track $k = 1$. All blocks with $w = 1$ are sorted to an empty classification track to start composing the corresponding outbound train. Each block with $w > 1$ is sequenced to the classification track which contains block $w - 1$, i.e. to a classification track on which blocks are pull backed later or to a classification track on which the outgoing train is built.

Note that this implies that each block is rehumped at most twice. Fig. 4 illustrates the general assignment for the first 10 blocks and in Fig. 5 can be found an example with two trains (zigzag and dot hatched).

Geometric Sorting (GS), see Boysen et al. (2012) and Gatto et al. (2009), is similar to TS and mainly differs in the blocks' assignment scheme.

The initial assignment of blocks to classification tracks follows a geometric distribution as follows

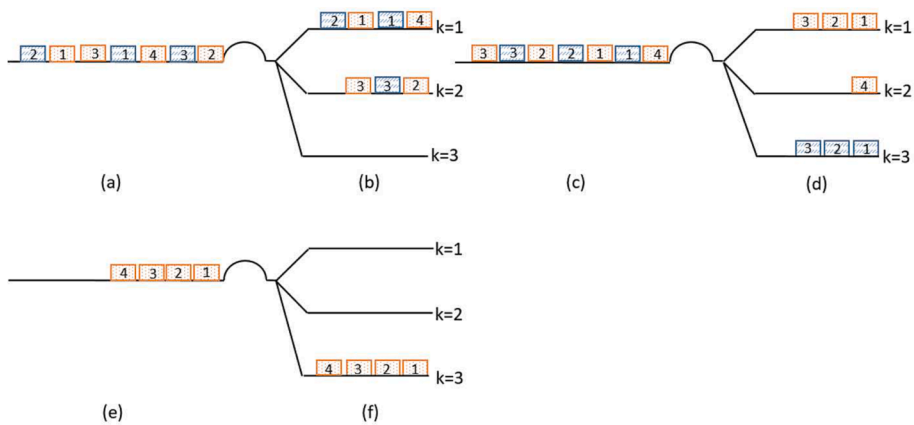


Fig. 7. Parallel Pullbacks with presortedness applied to two classification tracks for sorting $k = 1, 2$ and one track for departure $k = 3$, (a) one inbound train has to be shunted to two outgoing trains; assembling of initial batches: dot hatched train (= train 1) $B_{1,1}^0 = \{1\}$, $B_{2,1}^0 = \{2, 3\}$, $B_{3,1}^0 = \{4\}$, zigzag hatched train (= train 2) $B_{1,2}^0 = \{1, 2\}$, $B_{2,2}^0 = \{3\}$, (b) Push batchelements of each outgoing train into their designated classification track, (c) Pullback of the second ($k = 2$) and afterwards the first ($k = 1$) classification track; assembling of batches by combining each two batches: dot hatched train $B_{1,1}^1 = \{1, 2, 3\}$, $B_{2,1}^1 = \{4\}$, zigzag hatched train $B_{1,2}^1 = \{1, 2, 3\}$, (d) Push batchelements into their designated classification track; blocks of the zigzag hatched train to $k = 3$ for departure, (e) Pullback of the second ($k = 2$) and afterwards the first ($k = 1$) classification track to get the final composition, (f) humping of the blocks to $k = 3$ for departure of the dot hatched train.

$$\tilde{w}_k^{GS} = \bigcup_{j=0}^{-gs} \{2^{k-1} + 2^k \cdot j\} \quad (4)$$

The maximum number of blocks assigned to track k is

$$\bar{j}_k^{GS} = \lfloor \frac{\tilde{w}_{max} - 2^{k-1}}{2^k} \rfloor \quad (5)$$

where \tilde{w}_{max} denotes the maximum index of all blocks again. The proof of \bar{j}_k^{GS} is similar to the proof of (3).

Due to the geometric block assignment, typically less classification tracks are occupied by GS than by TS, but blocks are pulled back more frequently. Similar to TS, the blocks are pulled back sequentially starting with track $k = 1$. Again, the blocks with $w = 1$ are shunted to an empty classification track to start composing an outbound train. Other blocks are shunted to their corresponding outbound train or to the classification track which holds its direct predecessor. Fig. 6 illustrates the general assignment of blocks to classification tracks for GS and in Fig. 5 can be found an example with two outgoing trains.

Parallel Pullback sorting (PPS) is a sorting strategy which can build trains with a predetermined number of classification tracks \bar{k} . If the sequence of blocks in the incoming trains is taken into consideration PPS includes “.” The strategy is described in Gatto et al. (2009) and Dahlhaus et al. (2000) for one incoming and one outgoing train and with or without presortedness. Because PPS with presortedness is at least equal or better than PPS without presortedness the following explanations are referred to PPS with presortedness. Also the procedure is extended for more than one incoming and one outgoing train. Adapting the procedure to multiple incoming trains is straightforward. For adapting to multiple outgoing trains allows multiple options. One option is to number the blocks of each outgoing train r from 1 to n_r which is applied in the rolling horizon approach in Subsection 2.2.

The blocks of an incoming train are assigned to batches of blocks $B_{b,r}^{pss}$ in sorting step $pss = 1, 2, \dots$ for batch $b = 1, 2, \dots$ and outgoing train r . This assignment can be found in the procedure below. To apply PPS a preprocessing step is necessary. The preprocessing step involves creating batches $B_{b,r}^0$ ($b = 1, 2, \dots$), where all relatively sequenced blocks in the incoming train are assigned to the same batch. Afterwards the following sorting steps $pss = 1, 2, \dots$ are repeated until the correct block sequences are reached on the classification tracks:

1. Blocks on the receiving tracks are humped into the classification tracks depending on their assignment to batches. Batch $B_{b,r}^{pss-1}$ is assigned to classification track $1 + ((b - 1) \bmod \bar{k})$.

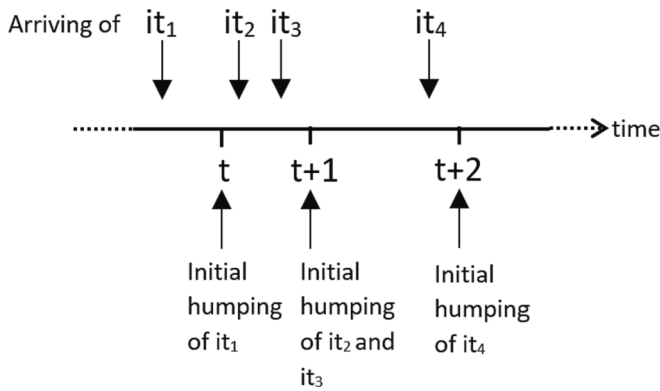


Fig. 8. Example for arriving of four incoming trains (it) and their initial humping at the beginning of period $t, t + 1$ and $t + 2$. After initial humping sorting of blocks is taken place until period ends.

2. Pull back each classification track in descending order ($\bar{k}, \bar{k} - 1, \dots, 2, 1$) into the receiving tracks.
3. Determine $B_{b,r}^{DSS} = \bigcup_{i=1+(b-1)\bar{k}}^{b\bar{k}} B_{i,r}^0$ for $b = 1, 2, \dots$

For an example of PPS with presortedness, see Fig. 7. If n is the number of blocks of the incoming train, the number of needed sorting steps is $\lceil \log_{\bar{k}} n \rceil$ which refers to PPS without presortedness. If d is the number of batches which are necessary for the presorted blocks, the number of needed sorting steps is $\lceil \log_{\bar{k}} d \rceil$. Inequality $n \geq d$ implies $\lceil \log_{\bar{k}} n \rceil \geq \lceil \log_{\bar{k}} d \rceil$, i.e. if presortedness is included the number of sorting steps is less or equal compared to the procedure without presortedness.

2.2. Rolling horizon approach in a shunting environment

The sorting strategies described in Subsection 2.1 generate a sorting plan for a given set of outbound trains to be built from a given set of inbound trains without considering time. In practice, however, sorting is conducted perpetually in certain time intervals depending on the train schedules. This implies that the sets of inbound and outbound trains are incomplete and change dynamically over time. To study the effects of those sorting strategies in such a rolling horizon environment requires to deduce generalized forms of performance functions for each sorting strategy which ables to deal with incomplete train sets already waiting for completion or humping.

Definitions and the general rolling horizon procedure are described in Subsubsection 2.2.1. Specific generalized performance functions for each sorting strategy are deduced in the subsequent subsections.

2.2.1. General procedure and definitions

In the following, a multi-period planning horizon is assumed which consists of p periods. If all blocks of an outgoing train have arrived in the marshalling yard in a certain period, the outgoing train is called “.” Otherwise, the outgoing train is called “.” If R denotes the set of all outgoing trains $\mathcal{R}_t \in \mathcal{R}$ marks the set of outgoing trains in the marshalling yard in period t . Let \mathcal{W} be the set of blocks and $v_{w,r}$ the number of railcars in block w of train r . At the beginning of a period, all blocks of all incoming trains are humped to the classification tracks which is called “.” At the beginning of period $t = 1$ there are no blocks on the classification tracks. In each period a termination criterion determines the transition to a new period, i.e. shunting of blocks is stopped and a new period starts with initial humping of the newly arrived trains. This termination criterion \bar{g}_t corresponds to a step for SBT, a track for SBB, TS and GS and a sorting step for PPS and is to be determined initially.

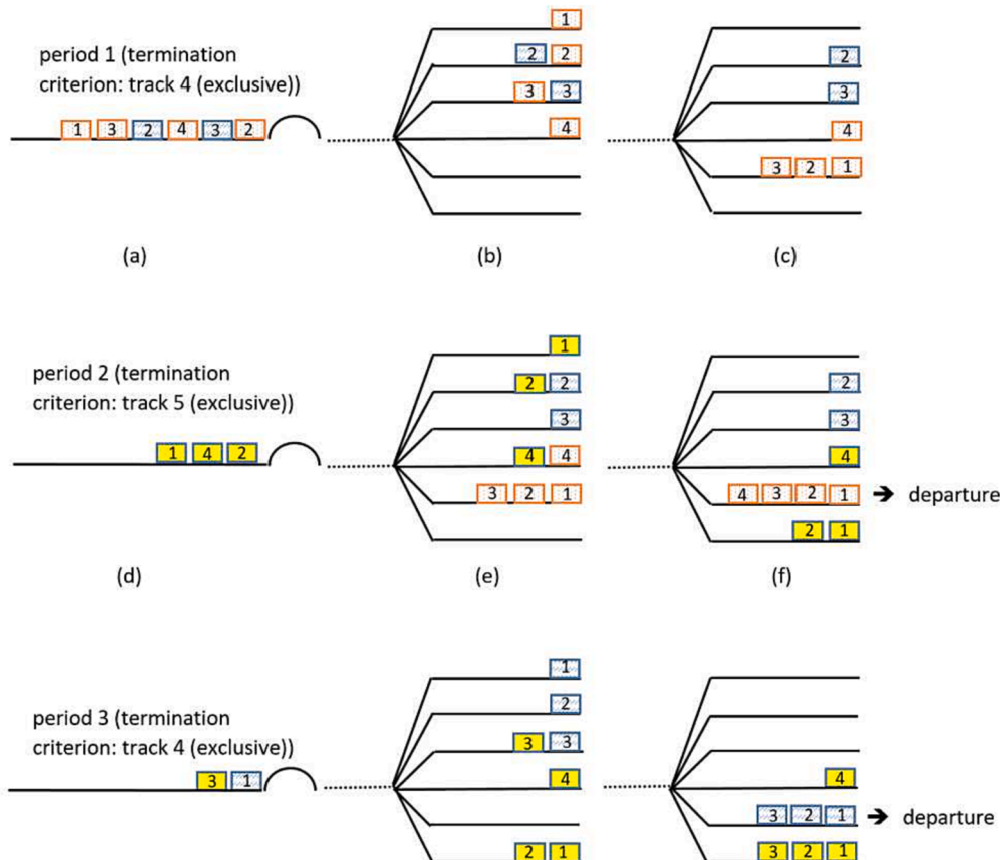


Fig. 9. Rolling horizon with 3 periods, 3 trains and the sorting procedure SBB, (a) incoming blocks of the dot hatched (constructable) and zigzag hatched (not constructable) train, (b) shunting blocks w.r.t. SBB, (c) pulling back track 1 to 3 without track 4, (d) incoming blocks of the continuously hatched (not constructable) train, (e) shunting blocks w.r.t. SBB, (f) pulling back track 1 to 4, i.e. afterwards the dot hatched train departs, (g) missing blocks of the continuously hatched and zigzag hatched blocks arrive in the marshalling yard, (h) shunting blocks w.r.t. SBB, (i) pulling back track 1 to 3 without track 4, i.e. afterwards the zigzag hatched train departs and the continuously hatched train remains in the marshalling yard at the end of the planning horizon.

Table 1

Best sorting strategies for varying expected numbers of blocks in outgoing trains, numbers of outgoing trains and numbers of incoming trains, b – Sorting-by-block (SBB), t – Sorting-by-Train (SBT).

a) $\lambda = 5$										
ot \ it	10	20	30	40	50	60	70	80	90	100
10	b	b	b	b	b	b	b	b	b	b
20	b	b	b	b	b	b	b	b	b	b
30	b	b	b	b	b	b	b	b	b	b
40	b	b	b	t	t	t	t	t	t	t
50	b	b	t	t	t	t	t	t	t	t
60	b	t	t	t	t	t	t	t	t	t
70	b	t	t	t	t	t	t	t	t	t
80	b	t	t	t	t	t	t	t	t	t
90	t	t	t	t	t	t	t	t	t	t
100	t	t	t	t	t	t	t	t	t	t

b) $\lambda = 10$										
ot \ it	10	20	30	40	50	60	70	80	90	100
10	b	b	b	b	b	b	b	b	b	b
20	b	b	b	b	b	b	b	b	b	b
30	b	b	b	b	b	b	b	b	b	b
40	b	b	b	b	b	b	b	b	b	b
50	b	b	b	b	b	b	b	b	b	b
60	b	b	b	b	t	t	t	t	t	t
70	b	b	t	t	t	t	t	t	t	t
80	b	b	t	t	t	t	t	t	t	t
90	b	t	t	t	t	t	t	t	t	t
100	b	t	t	t	t	t	t	t	t	t

c) $\lambda = 15$										
ot \ it	10	20	30	40	50	60	70	80	90	100
10	b	b	b	b	b	b	b	b	b	b
20	b	b	b	b	b	b	b	b	b	b
30	b	b	b	b	b	b	b	b	b	b
40	b	b	b	b	b	b	b	b	b	b
50	b	b	b	b	b	b	b	b	b	b
60	b	b	b	b	b	b	b	b	b	b
70	b	b	b	b	b	b	b	b	b	b
80	b	b	b	b	b	b	b	b	b	b
90	b	b	b	b	b	b	b	b	b	b
100	b	b	b	b	b	b	t	b	t	b

d) $\lambda = 20$										
ot \ it	10	20	30	40	50	60	70	80	90	100
10	b	b	b	b	b	b	b	b	b	b
20	b	b	b	b	b	b	b	b	b	b
30	b	b	b	b	b	b	b	b	b	b
40	b	b	b	b	b	b	b	b	b	b
50	b	b	b	b	b	b	b	b	b	b
60	b	b	b	b	b	b	b	b	b	b
70	b	b	b	b	b	b	b	b	b	b
80	b	b	b	b	b	b	b	b	b	b
90	b	b	b	b	b	b	b	b	b	b
100	b	b	b	b	b	b	b	b	b	b

e) $\lambda = 25$										
ot \ it	10	20	30	40	50	60	70	80	90	100
10	b	b	b	b	b	b	b	b	b	b
20	b	b	b	b	b	b	b	b	b	b
30	b	b	b	b	b	b	b	b	b	b
40	b	b	b	b	b	b	b	b	b	b
50	b	b	b	b	b	b	b	b	b	b
60	b	b	b	b	b	b	b	b	b	b
70	b	b	b	b	b	b	b	b	b	b
80	b	b	b	b	b	b	b	b	b	b
90	b	b	b	b	b	b	b	b	b	b
100	b	b	b	b	b	b	b	b	b	b

f) $\lambda = 30$										
ot \ it	10	20	30	40	50	60	70	80	90	100
10	b	b	b	b	b	b	b	b	b	b
20	b	b	b	b	b	b	b	b	b	b
30	b	b	b	b	b	b	b	b	b	b
40	b	b	b	b	b	b	b	b	b	b
50	b	b	b	b	b	b	b	b	b	b
60	b	b	b	b	b	b	b	b	b	b
70	b	b	b	b	b	b	b	b	b	b
80	b	b	b	b	b	b	b	b	b	b
90	b	b	b	b	b	b	b	b	b	b
100	b	b	b	b	b	b	b	b	b	b

Table 1 (continued)

10	b	b	b	b	b	b	b	b	b	b
20	b	b	b	b	b	b	b	b	b	b
30	b	b	b	b	b	b	b	b	b	b
40	b	b	b	b	b	b	b	b	b	b
50	b	b	b	b	b	b	b	b	b	b
60	b	b	b	b	b	b	b	b	b	b
70	b	b	b	b	b	b	b	b	b	b
80	b	b	b	b	b	b	b	b	b	b
90	b	b	b	b	b	b	b	b	b	b
100	b	b	b	b	b	b	b	b	b	b

The general procedure of the five sorting strategies regarding the rolling horizon is as follows. First, initial humping is conducted, i.e. each incoming train is humped on the classification tracks based on the chosen sorting strategy, see subsection 2.1. Afterwards, the chosen sorting strategy is applied iteratively but adapted to deal with the blocks left over from the previous period. I.e. a sorting strategy with a rolling horizon adaption is applied to the blocks in the classification tracks. An example which visualizes the course of time can be found in Fig. 8. While shunting, blocks left over from previous periods and initially humped blocks newly arrived are taken into account at the same time. If track k which includes blocks of not constructable trains is pulled back, the blocks of not constructable trains are shunted to track k again. Later, emissions are calculated for each applied sorting strategy. Therefore, it is necessary to investigate the number of railcars for each pullback. For this purpose the so-called “f” or each of the five sorting strategies is derived, i.e. a set of numbers (= amount of railcars) per pullback is determined in period t . An example of shunting blocks in three subsequent periods can be found in Fig. 9.

2.2.2. Rolling horizon approach for Sorting-by-train

SBT is insensitive to the rolling horizon approach in the following way. The SBT sorting strategy is only applied to constructable trains. Blocks of not constructable trains remain on their assigned classification tracks and, therefore, do not influence shunting operations of constructable trains. Each constructable train r is processed by the following steps:

- $s_{r,0}$: Pull back and roll in all blocks of constructable train r
- $s_{r,1}$: Pull back and roll in railcars of blocks 1
- \vdots
- s_{r,n_r} : Pull back and roll in railcars of blocks n_r .

where n_r denotes the number of blocks of train r .

Outgoing trains can be built in arbitrary sequences until period t ends, i.e. if $r_{(1)}, r_{(2)}, \dots$ marks the construction sequence of the outgoing trains, a list of shunting steps can be defined as follows

$$L = \left(s_{r_{(1)},0}, s_{r_{(1)},1}, \dots, s_{r_{(1)},n_{r_{(1)}}}, s_{r_{(2)},0}, s_{r_{(2)},1}, \dots, s_{r_{(2)},n_{r_{(2)}}}, \dots \right). \tag{6}$$

When period t ends while step $s \in L$ is conducted, the building of the corresponding train r' can be continued in period $t+1$ in step $s+1 (= \bar{g}_t)$ where \bar{g}_t marks the (excluded) termination criterion of SBT in period t . Shunting of train $r' \in \mathcal{R}$ can be continued in period $t+1$ without consideration of incoming blocks because classification tracks with blocks of constructable trains receive no more blocks in further periods and hence, do not change over time.

Therefore, sorting performance of SBT can be derived without consideration of period t by

$$SP^{SBT} \left(\mathcal{W}, \mathcal{R} \right) = \bigcup_{r \in \mathcal{R}} \left\{ \sum_{w=1}^{n_r} v_{w,r}, v_{1,r}, \dots, v_{n_r,r} \right\}. \tag{7}$$

2.2.3. Rolling horizon approach for sorting-by-block

Applying SBB in a rolling horizon approach requires additional as-

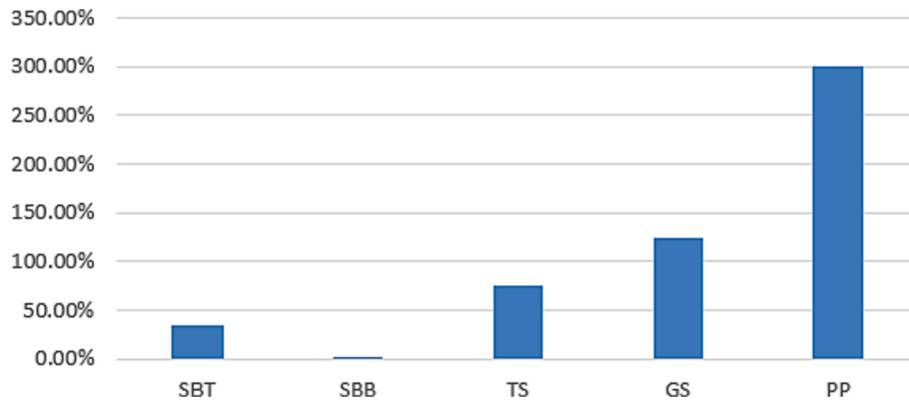


Fig. 10. Average deviation (in %) from the best sorting strategy.

Table 2

Best sorting strategies w.r.t. minimal emissions for varying expected numbers of blocks in outgoing trains, numbers of outgoing trains and numbers of incoming trains, interval of periods of blocks comprises only two sequential periods, b – Sorting-by-Block (SBB), x – Parallel Pullbacks sorting (PPS).

g) $\lambda = 10$										
ot \ it	10	20	30	40	50	60	70	80	90	100
10	x	x	x	x	x	x	x	x	x	x
20	b	b	b	b	b	b	b	b	b	b
30	b	b	b	b	b	b	b	b	b	b
40	b	b	b	b	b	b	b	b	b	b
50	b	b	b	b	b	b	b	b	b	b
60	b	b	b	b	b	b	b	b	b	b
70	b	b	b	b	b	b	b	b	b	b
80	b	b	b	b	b	b	b	b	b	b
90	b	b	b	b	b	b	b	b	b	b
100	b	b	b	b	b	b	b	b	b	b

h) $\lambda = 20$										
ot \ it	10	20	30	40	50	60	70	80	90	100
10	x	x	x	x	x	x	x	x	x	x
20	b	b	x	x	x	x	x	x	x	x
30	b	b	b	b	b	b	b	b	b	b
40	b	b	b	b	b	b	b	b	b	b
50	b	b	b	b	b	b	b	b	b	b
60	b	b	b	b	b	b	b	b	b	b
70	b	b	b	b	b	b	b	b	b	b
80	b	b	b	b	b	b	b	b	b	b
90	b	b	b	b	b	b	b	b	b	b
100	b	b	b	b	b	b	b	b	b	b

i) $\lambda = 30$										
ot \ it	10	20	30	40	50	60	70	80	90	100
10	x	x	x	x	x	x	x	x	x	x
20	b	b	b	b	b	x	b	x	b	x
30	b	b	b	b	b	b	b	b	b	b
40	b	b	b	b	b	b	b	b	b	b
50	b	b	b	b	b	b	b	b	b	b
60	b	b	b	b	b	b	b	b	b	b
70	b	b	b	b	b	b	b	b	b	b
80	b	b	b	b	b	b	b	b	b	b
90	b	b	b	b	b	b	b	b	b	b
100	b	b	b	b	b	b	b	b	b	b

sumptions. In each period the sorting process starts (after initial humping) with the first classification track, i.e. the track where blocks with number $w = 1$ are collected. If one or more classification tracks contain only blocks which can not be shunted to their designated departing tracks, all blocks of the considered classification tracks are not shunted.

To express the sorting performance of SBB in a rolling horizon approach sets of blocks are defined and combined. $\mathcal{W}_{t,0}^{SBB,r}$ defines the set

of blocks of the outgoing train r which arrive in the marshalling yard in period $t - 1$. Therefore, they are available for initial humping in period t . Blocks waiting on the classification tracks in period t are summarized in $\mathcal{W}_t^{SBB,r}$. $\mathcal{W}_t^{SBB,r,ex}$ denotes the set of blocks of train r on the corresponding departing track at the beginning of period t .

Thus, the set of blocks of train r humped into the classification tracks in period t is defined by $\mathcal{W}_t^{SBB,r,in} = \mathcal{W}_{t,0}^{SBB,r} \cup \mathcal{W}_t^{SBB,r}$. The set of blocks of train r shunted from classification to departing tracks in period t is denoted by $\mathcal{W}_t^{SBB,r,out}$ and is constructed as follows

$$\mathcal{W}_t^{SBB,r,out} = \{w | w^v \in \mathcal{W}_t^{SBB,r,ex} \cup (\mathcal{W}_t^{SBB,r} \cup \mathcal{W}_{t,0}^{SBB,r}) \setminus \{\bar{g}_t, \bar{g}_t + 1, \dots\} \forall w^v = 0, 1, \dots, w\} \setminus \mathcal{W}_t^{SBB,r,ex} \tag{8}$$

Thereby, block w is shunted to the departing tracks, if all predecessor blocks w^v are already on the departing tracks ($\mathcal{W}_t^{SBB,r,ex}$) or they are shunted from the classification tracks to the departing tracks in period t . I.e. predecessor block w^v is already on the classification tracks at the beginning of period t ($\mathcal{W}_t^{SBB,r}$) or is initially humped in period t ($\mathcal{W}_{t,0}^{SBB,r}$). In the latter case, blocks are not shunted if the termination criterion is exceeded. I.e. all blocks which are equal or exceed \bar{g}_t are not shunted in period t , but wait for further processing in subsequent periods.

At the beginning of period t blocks on the classification tracks ($W_t^{SBB,r}$) can be expressed by blocks on the classification tracks ($W_t^{SBB,r,in}$) without outgoing blocks ($W_t^{SBB,r,out}$) of the previous period $t - 1$ through

$$W_t^{SBB,r} = \begin{cases} \emptyset & \text{for } t = 1 \\ W_{t-1}^{SBB,r,in} \setminus W_{t-1}^{SBB,r,out} & \text{for } t > 1 \end{cases} \tag{9}$$

Blocks of train $r \in \mathcal{R}$ on the departing tracks at the beginning of period t can be formulated by

$$W_t^{SBB,r,ex} = \begin{cases} \emptyset & \text{for } t = 1 \\ W_{t-1}^{SBB,r,ex} \cup W_{t-1}^{SBB,r,out} & \text{for } t > 1 \end{cases} \tag{10}$$

i.e. blocks on the departure tracks in period $t - 1$ ($W_{t-1}^{SBB,r,ex}$) and outgoing blocks in period $t - 1$ ($W_{t-1}^{SBB,r,out}$). Finally, the sorting performance for SBB can be expressed by

$$SP_t^{SBB} \left(\mathcal{W}_t, \mathcal{R}_t \right) = \bigcup_{w=1, \dots, \bar{g}_t-1} \left\{ \sum_{r \in \mathcal{R}_t | w \in W_{t,0}^{SBB,r} \cup W_t^{SBB,r}} V_{w,r} \right\} \tag{11}$$

i.e. the set of initially humped railcars ($W_{t,0}^{SBB,r}$) and already existing railcars on the classification tracks ($W_t^{SBB,r}$) up to the excluded termination criterion \bar{g}_t is determined for (not) constructable trains $r \in \mathcal{R}_t$ in period t .

Table 3

Best sorting strategies w.r.t average number of pulled back railcars for varying expected numbers of blocks in outgoing trains, numbers of outgoing trains and numbers of incoming trains, b – Sorting-by-block (SBB), t – Sorting-by-Train (SBT).

a) $\lambda = 5$										
ot \ it	10	20	30	40	50	60	70	80	90	100
10	b	b	b	b	b	b	b	b	b	b
20	b	b	b	b	b	b	b	b	b	b
30	b	b	t	t	t	t	t	t	t	t
40	b	t	t	t	t	t	t	t	t	t
50	b	t	t	t	t	t	t	t	t	t
60	b	t	t	t	t	t	t	t	t	t
70	b	t	t	t	t	t	t	t	t	t
80	b	t	t	t	t	t	t	t	t	t
90	b	t	t	t	t	t	t	t	t	t
100	b	t	t	t	t	t	t	t	t	t

b) $\lambda = 10$										
ot \ it	10	20	30	40	50	60	70	80	90	100
10	b	b	b	b	b	b	b	b	b	b
20	b	b	b	b	b	t	t	t	t	t
30	b	t	t	t	t	t	t	t	t	t
40	b	t	t	t	t	t	t	t	t	t
50	b	t	t	t	t	t	t	t	t	t
60	b	t	t	t	t	t	t	t	t	t
70	b	t	t	t	t	t	t	t	t	t
80	b	t	t	t	t	t	t	t	t	t
90	b	t	t	t	t	t	t	t	t	t
100	b	t	t	t	t	t	t	t	t	t

c) $\lambda = 15$										
ot \ it	10	20	30	40	50	60	70	80	90	100
10	b	b	b	b	b	b	b	b	b	b
20	b	b	b	b	b	t	b	b	t	t
30	b	b	t	t	t	t	t	t	t	t
40	b	t	t	t	t	t	t	t	t	t
50	b	t	t	t	t	t	t	t	t	t
60	b	t	t	t	t	t	t	t	t	t
70	b	t	t	t	t	t	t	t	t	t
80	b	t	t	t	t	t	t	t	t	t
90	b	t	t	t	t	t	t	t	t	t
100	b	t	t	t	t	t	t	t	t	t

d) $\lambda = 20$										
ot \ it	10	20	30	40	50	60	70	80	90	100
10	b	b	b	b	b	b	b	b	b	b
20	b	b	b	b	b	b	b	b	b	b
30	b	b	b	t	t	b	b	t	t	t
40	b	b	t	t	t	t	t	t	t	t
50	b	b	t	t	t	t	t	t	t	t
60	b	b	t	t	t	t	t	t	t	t
70	b	t	t	t	t	t	t	t	t	t
80	b	t	t	t	t	t	t	t	t	t
90	b	t	t	t	t	t	t	t	t	t
100	b	t	t	t	t	t	t	t	t	t

e) $\lambda = 25$										
ot \ it	10	20	30	40	50	60	70	80	90	100
10	b	b	b	b	b	b	b	b	b	b
20	b	b	b	b	b	b	b	b	b	b
30	b	b	b	b	b	t	b	b	t	t
40	b	b	b	b	t	t	t	t	t	t
50	b	b	b	t	t	t	t	t	t	t
60	b	b	t	t	t	t	t	t	t	t
70	b	b	t	t	t	t	t	t	t	t
80	b	b	t	t	t	t	t	t	t	t
90	b	b	t	t	t	t	t	t	t	t
100	b	b	t	t	t	t	t	t	t	t

f) $\lambda = 30$										
ot \ it	10	20	30	40	50	60	70	80	90	100
10	b	b	b	b	b	b	b	b	b	b
20	b	b	b	b	b	b	b	b	b	b
30	b	b	b	b	b	t	b	b	t	t
40	b	b	b	b	t	t	t	t	t	t
50	b	b	b	t	t	t	t	t	t	t
60	b	b	t	t	t	t	t	t	t	t
70	b	b	t	t	t	t	t	t	t	t
80	b	b	t	t	t	t	t	t	t	t
90	b	b	t	t	t	t	t	t	t	t
100	b	b	t	t	t	t	t	t	t	t

Table 3 (continued)

ot \ it	10	20	30	40	50	60	70	80	90	100
10	b	b	b	b	b	b	b	b	b	b
20	b	b	b	b	b	b	b	b	b	b
30	b	b	b	b	b	b	b	b	b	b
40	b	b	b	b	t	t	b	t	t	t
50	b	b	b	t	t	t	t	t	t	t
60	b	b	b	t	t	t	t	t	t	t
70	b	b	t	t	t	t	t	t	t	t
80	b	b	t	t	t	t	t	t	t	t
90	b	b	t	t	t	t	t	t	t	t
100	b	b	t	t	t	t	t	t	t	t

Table 4

Best sorting strategies w.r.t average number of pulled back railcars for varying expected numbers of blocks in outgoing trains, numbers of outgoing trains and numbers of incoming trains, interval of periods of blocks comprises only two sequential periods, b – Sorting-by-Block (SBB)

g) $\lambda = 10$										
ot \ it	10	20	30	40	50	60	70	80	90	100
10	b	b	b	b	b	b	b	b	b	b
20	b	b	b	b	b	b	b	b	b	b
30	b	b	b	b	b	b	b	b	b	b
40	b	b	b	b	b	b	b	b	b	b
50	b	b	b	b	b	b	b	b	b	b
60	b	b	b	b	b	b	b	b	b	b
70	b	b	b	b	b	b	b	b	b	b
80	b	b	b	b	b	b	b	b	b	b
90	b	b	b	b	b	b	b	b	b	b
100	b	b	b	b	b	b	b	b	b	b

h) $\lambda = 20$										
ot \ it	10	20	30	40	50	60	70	80	90	100
10	b	b	b	b	b	b	b	b	b	b
20	b	b	b	b	b	b	b	b	b	b
30	b	b	b	b	b	b	b	b	b	b
40	b	b	b	b	b	b	b	b	b	b
50	b	b	b	b	b	b	b	b	b	b
60	b	b	b	b	b	b	b	b	b	b
70	b	b	b	b	b	b	b	b	b	b
80	b	b	b	b	b	b	b	b	b	b
90	b	b	b	b	b	b	b	b	b	b
100	b	b	b	b	b	b	b	b	b	b

i) $\lambda = 30$										
ot \ it	10	20	30	40	50	60	70	80	90	100
10	b	b	b	b	b	b	b	b	b	b
20	b	b	b	b	b	b	b	b	b	b
30	b	b	b	b	b	b	b	b	b	b
40	b	b	b	b	b	b	b	b	b	b
50	b	b	b	b	b	b	b	b	b	b
60	b	b	b	b	b	b	b	b	b	b
70	b	b	b	b	b	b	b	b	b	b
80	b	b	b	b	b	b	b	b	b	b
90	b	b	b	b	b	b	b	b	b	b
100	b	b	b	b	b	b	b	b	b	b

2.2.4. Rolling horizon approach for Triangular sorting/Geometric sorting

The sorting performances for TS and GS can be derived simultaneously because they only differ in several input factors. The derived formulas are more complex compared to SBB and need more assumptions. Shunting starts with the first classification track in each period. If a classification track has no blocks or only blocks which can not be shunted, the blocks are not pulled back. Each outgoing train $r \in \mathcal{R}$ contains blocks numbered from 1 to n_r . After initial humping, blocks can be shunted to their designated departure track without detours on other classification tracks. Blocks remain on the classification tracks if predecessor blocks are not on the classification or departing tracks.

The termination criterion \bar{g}_t corresponds to a classification track

Table 5
Average technical parameters of DB railcar types.

railcar type	Average tare weight	Average load limit
E (Open railcars)	23.6	63.0
F (Open hopper railcars)	31.3	68.7
H (High-capacity sliding-wall covered railcars)	28.1	42.8
K (Flat railcars with 2 axles)	25.8	41.3
L (Car transporter units)	36.5	35.5
R (Bogie flat railcars)	26.6	63.3
S (Six-axle bogie flat railcars)	29.5	75.6
S (Bogie coil railcars)	26.8	68.9
S (Bogie flat railcars with cargo ratchet straps)	25.0	63.0
T (Covered bulk railcars)	22.9	60.0
T (Railcar with opening roof)	23.3	66.5

(excluded) where shunting in period t ends. The total amount of necessary tracks to shunt outgoing train r is given by $\bar{k}^{TS,r} = \lfloor \sqrt{2 \cdot n_r - \frac{7}{4}} + \frac{1}{2} \rfloor$ for TS, see Daganzo et al. (1983) and $\bar{k}^{GS,r} = \lfloor \log_2 n_r \rfloor + 1$ for GS, see Gatto et al. (2009). Thus, the maximum number of classification tracks can be derived as $\bar{k}^{TS/GS} = \max_{r \in R} \bar{k}^{TS/GS,r}$. For each classification track, sets of sequenced blocks can be determined, e.g. blocks {2, 3} or {6, 7} on classification track 2. These sets consist of blocks which are shunted throughout initial humping, e.g. 2 or 6 and successor blocks of predecessor classification tracks, e.g. 3 or 7. Shunted blocks throughout initial humping can be expressed by

$$\tilde{W}_{kj}^{TS} = \begin{cases} \left\{ \frac{k \cdot (k-1)}{2} + 1 \right\} & \text{for } j = 1 \\ \left\{ \frac{k \cdot (k-1)}{2} + 1 + j \cdot k + \frac{(j-1)(j-2)}{2} \right\} & \text{for } j > 1 \end{cases} \quad (12)$$

for TS and $\tilde{W}_{kj}^{GS} = \{2^{k-1} + 2^k \cdot (j-1)\}$ with $k, j \in \mathbb{N}_{>0}$ for GS, where k denotes the considered classification track and j the sequenced blocks set. Successor blocks can be derived as $\overline{W}_k^{TS} = \{w \mid \bar{w}_{k-1} < w < \bar{w}_k, \bar{w}_k = \frac{k(k+1)}{2} + 1\}$ for TS and $\overline{W}_k^{GS} = \{2^k \cdot j - i \mid i = 1, \dots, 2^{k-1} - 1\}$ with $k, j \in \mathbb{N}_{>0}$ for GS. Combining initially humped blocks sets ($\tilde{W}_{kj}^{TS/GS}$) and successor blocks sets ($\overline{W}_k^{TS/GS}$) results in

$$\widehat{W}_{kj}^{TS} = \begin{cases} \emptyset & \text{for } k = 0 \\ \tilde{W}_{kj}^{TS} & \text{for } k > 0, j > 1 \\ \tilde{W}_{kj}^{TS} \cup \overline{W}_k^{TS} & \text{for } k > 0, j = 1 \end{cases} \quad (13)$$

for TS and

$$\widehat{W}_{kj}^{GS} = \begin{cases} \emptyset & \text{for } k = 0 \\ \tilde{W}_{kj}^{GS} \cup \overline{W}_k^{GS} & \text{for } k > 0 (j > 0) \end{cases} \quad (14)$$

for GS. The set of blocks of train $r \in \mathcal{R}$ on the departing tracks at the end of period t can be expressed by

$$W_t^{TS/GS,r,ex} = \begin{cases} \emptyset & \text{for } t = 0 \\ \left\{ w \mid w \in \left\{ W_{t-1}^{TS/GS,r,ex} \cup \bigcup_{k' < \bar{g}_t} W_{t,k'}^{TS/GS,r} \right\} \right. \\ \quad \left. \wedge w = 1, 2, \dots, \text{consecutively numbered} \right\} & \text{for } t > 0 \end{cases} \quad (15)$$

i.e. the union of blocks on the departing track of the previous period $t-1$ ($W_{t-1}^{TS/GS,r,ex}$) and blocks pulled back in period t ($\bigcup_{k' < \bar{g}_t} W_{t,k'}^{TS/GS,r}$). The set of shunted blocks in period t can be derived as

$$W_{t,k}^{TS/GS,r,out} = \begin{cases} \emptyset, & \text{for } k \geq \bar{g}_t \\ \left(\bigcup_{k' > k} W_{t,k'}^{TS/GS,r} \cup W_t^{TS/GS,r,ex} \right) \cap W_{t,k}^{TS/GS,r} & \text{for } k < \bar{g}_t \end{cases} \quad (16)$$

For classification tracks $k < \bar{g}_t$, all blocks of outgoing train r which leave track k in period t are summarized in $W_{t,k}^{TS/GS,r,out}$. This set consists of blocks which are not yet shunted on classification tracks ($\bigcup_{k' > k} W_{t,k'}^{TS/GS,r}$) and blocks on the departing tracks ($W_t^{TS/GS,r,ex}$). However, these blocks are only considered if these blocks are in the set of pulled back blocks on classification track k ($W_{t,k}^{TS/GS,r}$).

To formulate the sorting performance of TS and GS, an additional set of blocks of train r at the end of period t on classification track k is necessary. This set can be described by

$$W_{t,k}^{TS/GS,r} = \begin{cases} W_{t,0}^r & \text{for } k = 0 \\ \emptyset & \text{for } k > 0, t = 0, \\ W_{t,k}^{TS/GS,r} \setminus W_{t,k}^{TS/GS,r,out} & \text{for } k > 0, t > 0 \end{cases} \quad (17)$$

i.e. classification track $k = 0$ corresponds to the receiving track and equals the set of incoming blocks in period t . At the beginning of period $t = 1$ (i.e. at the end of period $t = 0$) there are no blocks on the classification tracks. Other combinations of $k > 0$ and $t > 0$ results in the set of pulled back blocks ($W_{t,k}^{TS/GS,r}$) without blocks which are on further classification tracks or on the departing tracks ($W_{t,k}^{TS/GS,r,out}$), i.e. blocks on classification track k at the end of period t . Describing the consecutively numbered blocks in $W_{t,k,j}^{TS/GS,r}$, parameter $\alpha_{kj}^{TS/GS}$ defines the first blocks of the sequenced block set j on track k as follows

$$\alpha_{kj}^{TS} = \begin{cases} \frac{k \cdot (k-1)}{2} + 1 & \text{for } j = 1 \\ \frac{k \cdot (k-1)}{2} + 1 + k \cdot j + \frac{(j-1)(j-2)}{2} & \text{for } j > 1 \end{cases} \quad (18)$$

for TS and $\alpha_{kj}^{GS} = 2^{k-1} + 2^k(j-1)$ for GS. E.g., regarding again the sets of sequenced blocks {2, 3} and {6, 7} the first blocks are $\alpha_{2,1}^{TS/GS} = 2$ and $\alpha_{2,2}^{TS/GS} = 6$. Parameter $\alpha_{kj}^{TS/GS}$ is used to express the set of shunted blocks of the sequenced blocks set j on track k as

$$W_{t,k,j}^{TS/GS,r} = \begin{cases} \emptyset & \text{for } k > \bar{k}^{TS/GS,r} \\ \left\{ w \mid w \in \widehat{W}_{kj}^{TS/GS} \cap \bigcup_{k' \leq k} W_{t-1,k'}^{TS/GS,r} \right. \\ \quad \left. \wedge w = \alpha_{kj}^{TS/GS}, \alpha_{kj}^{TS/GS} + 1, \dots \right. \\ \quad \left. \text{consecutively numbered} \right\} & \text{for } k \leq \bar{k}^{TS/GS,r} \end{cases} \quad (19)$$

I.e. considering the intersection of theoretically blocks on track k in sequenced block set j ($\widehat{W}_{kj}^{TS/GS}$) and the actually shunted blocks of all

Table 6
Technical parameters for shunting locomotive and railcars used in the emission model of Kirschstein and Meisel (2015).

ϵ	k	p	c_{roll}^{loc}	$c_{roll}^{railcar}$	c_{roll}^{aux1}	c_{roll}^{aux2}	c_{air}^{loc}	$c_{air}^{railcar}$	A	n_{axles}
0.4	3.15	0.1004	0.003	0.0006	0.0005	0.0006	0.8	0.218	9	4

Table 7
Total emissions (kg CO₂e) for expected value of blocks = 5 (ot = number of outgoing trains, it = number of incoming trains)

ot\it	10	20	30	40	50	60	70	80	90	100						
10	326	SBB	333	SBB	334	SBB	340	SBB	344	SBB	348	SBB	356	SBB	356	SBB
20	730	SBB	754	SBB	782	SBB	804	SBB	824	SBB	844	SBB	879	SBB	818	SBB
30	1173	SBB	1251	SBB	1276	SBB	1314	SBB	1346	SBB	1381	SBB	1351	SBB	1367	SBB
40	1671	SBB	1807	SBB	1813	SBB	1867	SBB	1866	SBB	1854	SBB	1849	SBB	1857	SBB
50	2216	SBB	2371	SBB	2378	SBB	2358	SBB	2347	SBB	2345	SBB	2337	SBB	2327	SBB
60	2824	SBB	2914	SBB	2864	SBB	2830	SBB	2832	SBB	2807	SBB	2798	SBB	2793	SBB
70	3465	SBB	3435	SBB	3364	SBB	3330	SBB	3318	SBB	3294	SBB	3284	SBB	3267	SBB
80	4228	SBB	3969	SBB	3864	SBB	3832	SBB	3784	SBB	3768	SBB	3742	SBB	3743	SBB
90	4866	SBB	4501	SBB	4384	SBB	4344	SBB	4261	SBB	4265	SBB	4237	SBB	4223	SBB
100	5496	SBB	5045	SBB	4899	SBB	4817	SBB	4778	SBB	4746	SBB	4702	SBB	4704	SBB

Table 8
Total emissions (kg CO₂e) for expected value of blocks = 10 (ot = number of outgoing trains, it = number of incoming trains).

ot\it	10	20	30	40	50	60	70	80	90	100						
10	314	SBB	346	SBB	365	SBB	365	SBB	370	SBB	372	SBB	384	SBB	369	SBB
20	691	SBB	755	SBB	809	SBB	815	SBB	807	SBB	823	SBB	855	SBB	851	SBB
30	1134	SBB	1243	SBB	1263	SBB	1362	SBB	1357	SBB	1381	SBB	1381	SBB	1407	SBB
40	1608	SBB	1750	SBB	1802	SBB	1942	SBB	1952	SBB	1912	SBB	1971	SBB	2010	SBB
50	2132	SBB	2380	SBB	2461	SBB	2557	SBB	2553	SBB	2570	SBB	2631	SBB	2625	SBB
60	2700	SBB	2955	SBB	3109	SBB	3133	SBB	3212	SBB	3208	SBB	3192	SBB	3187	SBB
70	3276	SBB	3635	SBB	3812	SBB	3773	SBB	3759	SBB	3748	SBB	3726	SBB	3731	SBB
80	3966	SBB	4345	SBB	4388	SBB	4328	SBB	4322	SBB	4293	SBB	4268	SBB	4257	SBB
90	4698	SBB	5094	SBB	4951	SBB	4920	SBB	4847	SBB	4837	SBB	4802	SBB	4806	SBB
100	5402	SBB	5688	SBB	5539	SBB	5454	SBB	5421	SBB	5415	SBB	5353	SBB	5345	SBB

Table 11
Total emissions (kg CO₂e) for expected value of blocks = 25 (ot = number of outgoing trains, it = number of incoming trains).

ot\it	10	20	30	40	50	60	70	80	90	100								
10	391	SBB	434	SBB	439	SBB	449	SBB	458	SBB	465	SBB	467	SBB	485	SBB	479	SBB
20	822	SBB	915	SBB	929	SBB	949	SBB	961	SBB	963	SBB	951	SBB	1004	SBB	992	SBB
30	1353	SBB	1403	SBB	1450	SBB	1571	SBB	1544	SBB	1623	SBB	1535	SBB	1585	SBB	1587	SBB
40	1895	SBB	1943	SBB	2055	SBB	2100	SBB	2214	SBB	2209	SBB	2206	SBB	2213	SBB	2258	SBB
50	2470	SBB	2632	SBB	2704	SBB	2817	SBB	2823	SBB	2852	SBB	2786	SBB	2902	SBB	2870	SBB
60	3165	SBB	3304	SBB	3429	SBB	3519	SBB	3563	SBB	3652	SBB	3632	SBB	3598	SBB	3704	SBB
70	3891	SBB	3978	SBB	4101	SBB	4150	SBB	4353	SBB	4313	SBB	4326	SBB	4454	SBB	4404	SBB
80	4628	SBB	4786	SBB	4915	SBB	4948	SBB	5002	SBB	5236	SBB	5025	SBB	5105	SBB	5159	SBB
90	5476	SBB	5557	SBB	5768	SBB	5765	SBB	5884	SBB	6012	SBB	6033	SBB	6051	SBB	6023	SBB
100	6367	SBB	6341	SBB	6601	SBB	6726	SBB	6721	SBB	6807	SBB	6849	SBB	6862	SBB	6757	SBB

Table 12
Total emissions (kg CO₂e) for expected value of blocks = 30 (ot = number of outgoing trains, it = number of incoming trains).

ot\it	10	20	30	40	50	60	70	80	90	100								
10	409	SBB	478	SBB	482	SBB	465	SBB	487	SBB	515	SBB	514	SBB	513	SBB	502	SBB
20	906	SBB	933	SBB	1038	SBB	1029	SBB	1056	SBB	1080	SBB	1087	SBB	1052	SBB	1099	SBB
30	1413	SBB	1529	SBB	1602	SBB	1651	SBB	1687	SBB	1684	SBB	1683	SBB	1661	SBB	1700	SBB
40	2053	SBB	2232	SBB	2254	SBB	2257	SBB	2339	SBB	2323	SBB	2360	SBB	2344	SBB	2346	SBB
50	2710	SBB	2911	SBB	2869	SBB	2996	SBB	2996	SBB	3052	SBB	3035	SBB	3162	SBB	3129	SBB
60	3464	SBB	3591	SBB	3665	SBB	3786	SBB	3827	SBB	3782	SBB	3919	SBB	3894	SBB	3832	SBB
70	4258	SBB	4197	SBB	4521	SBB	4529	SBB	4641	SBB	4668	SBB	4817	SBB	4637	SBB	4704	SBB
80	5158	SBB	5120	SBB	5378	SBB	5424	SBB	5412	SBB	5431	SBB	5580	SBB	5465	SBB	5566	SBB
90	6087	SBB	5988	SBB	6260	SBB	6588	SBB	6290	SBB	6590	SBB	6503	SBB	6430	SBB	6401	SBB
100	7104	SBB	6950	SBB	6999	SBB	7241	SBB	7401	SBB	7301	SBB	7205	SBB	7158	SBB	7362	SBB

Table 13
Total emissions (kg CO₂e) for expected value of blocks = 10 and two sequential periods (ot = number of outgoing trains, it = number of incoming trains).

ot\it	10	20	30	40	50	60	70	80	90	100
10	309	314	319	323	328	325	331	332	328	335
20	612	622	636	643	652	654	654	654	659	655
30	917	933	945	954	958	962	963	972	974	970
40	1245	1241	1240	1257	1260	1264	1265	1280	1288	1270
50	1595	1548	1557	1554	1570	1588	1570	1586	1577	1583
60	1970	1874	1872	1879	1870	1869	1886	1894	1869	1892
70	2348	2212	2190	2189	2181	2193	2187	2196	2181	2185
80	2777	2558	2515	2516	2501	2506	2489	2501	2499	2495
90	3193	2928	2861	2838	2823	2801	2810	2802	2801	2785
100	3661	3303	3202	3178	3135	3136	3120	3103	3123	3101

Table 14
Total emissions (kg CO₂e) for expected value of blocks = 20 and two sequential periods (ot = number of outgoing trains, it = number of incoming trains).

ot\it	10	20	30	40	50	60	70	80	90	100
10	404	411	415	423	423	424	431	425	424	425
20	773	830	852	863	866	868	876	883	882	883
30	1140	1193	1222	1249	1261	1261	1271	1281	1266	1267
40	1524	1556	1585	1636	1639	1644	1638	1654	1650	1653
50	1947	1920	1955	1998	2011	2010	2020	2012	2018	2019
60	2416	2327	2345	2368	2379	2372	2370	2364	2383	2384
70	2847	2717	2703	2732	2730	2733	2749	2739	2727	2740
80	3345	3136	3091	3114	3111	3098	3111	3106	3100	3091
90	3858	3530	3504	3488	3457	3468	3475	3451	3482	3442
100	4445	3984	3902	3887	3855	3860	3818	3815	3793	3810

Table 15
Total emissions (kg CO₂e) for expected value of blocks = 30 and two sequential periods (ot = number of outgoing trains, it = number of incoming trains).

ot\it	10	20	30	40	50	60	70	80	90	100
10	517	PPS	532	PPS	541	PPS	542	PPS	541	PPS
20	980	SBB	1079	SBB	1104	SBB	1123	SBB	1129	SBB
30	1473	SBB	1561	SBB	1601	SBB	1610	SBB	1613	SBB
40	1973	SBB	2016	SBB	2069	SBB	2085	SBB	2080	SBB
50	2540	SBB	2489	SBB	2530	SBB	2544	SBB	2539	SBB
60	3110	SBB	2959	SBB	2981	SBB	3011	SBB	3010	SBB
70	3762	SBB	3497	SBB	3483	SBB	3440	SBB	3458	SBB
80	4452	SBB	3979	SBB	3951	SBB	3930	SBB	3901	SBB
90	5227	SBB	4479	SBB	4437	SBB	4396	SBB	4357	SBB
100	5930	SBB	5057	SBB	4913	SBB	4863	SBB	4811	SBB

Table 16
Average number of pulled back railcars for expected value of blocks = 5 (ot = number of outgoing trains, it = number of incoming trains).

ot\it	10	20	30	40	50	60	70	80	90	100
10	409	SBB	425	SBB	440	SBB	444	SBB	468	SBB
20	934	SBB	1011	SBB	1121	SBB	1142	SBB	1152	SBB
30	1458	SBB	1684	SBB	1753	SBT	1762	SBT	1747	SBT
40	2030	SBB	2339	SBT	2325	SBT	2319	SBT	2334	SBT
50	2595	SBB	2916	SBT	2916	SBT	2917	SBT	2922	SBT
60	3201	SBB	3499	SBT	3491	SBT	3500	SBT	3504	SBT
70	3807	SBB	4080	SBT	4081	SBT	4082	SBT	4082	SBT
80	4470	SBB	4662	SBT	4678	SBT	4660	SBT	4662	SBT
90	5017	SBB	5242	SBT	5282	SBT	5258	SBT	5251	SBT
100	5619	SBB	5829	SBT	5810	SBT	5835	SBT	5835	SBT

Table 17
Average number of pulled back railcars for expected value of blocks = 10 (ot = number of outgoing trains, it = number of incoming trains).

ot\it	10	20	30	40	50	60	70	80	90	100
10	386	SBB	473	SBB	480	SBB	483	SBB	477	SBB
20	879	SBB	1137	SBB	1133	SBB	1150	SBT	1140	SBT
30	1444	SBB	1719	SBT	1735	SBT	1731	SBT	1734	SBT
40	2005	SBB	2300	SBT	2308	SBT	2291	SBT	2303	SBT
50	2608	SBB	2864	SBT	2884	SBT	2887	SBT	2859	SBT
60	3207	SBB	3449	SBT	3456	SBT	3453	SBT	3451	SBT
70	3767	SBB	4037	SBT	4020	SBT	4026	SBT	4031	SBT
80	4446	SBB	4600	SBT	4614	SBT	4595	SBT	4588	SBT
90	5123	SBB	5167	SBT	5162	SBT	5164	SBT	5166	SBT
100	5743	SBB	5752	SBT	5746	SBT	5757	SBT	5740	SBT

Table 18
Average number of pulled back railcars for expected value of blocks = 15 (ot = number of outgoing trains, it = number of incoming trains).

ot\it	10	20	30	40	50	60	70	80	90	100
10	401	SBB	464	SBB	491	SBB	487	SBB	488	SBB
20	868	SBB	1108	SBB	1156	SBB	1133	SBB	1191	SBB
30	1423	SBB	1790	SBT	1793	SBT	1793	SBT	1795	SBT
40	1925	SBB	2394	SBT	2392	SBT	2399	SBT	2385	SBT
50	2594	SBB	2983	SBT	2989	SBT	2992	SBT	2989	SBT
60	3071	SBB	3598	SBT	3573	SBT	3596	SBT	3581	SBT
70	3698	SBB	4183	SBT	4180	SBT	4187	SBT	4179	SBT
80	4288	SBB	4779	SBT	4773	SBT	4778	SBT	4781	SBT
90	4864	SBB	5368	SBT	5371	SBT	5378	SBT	5368	SBT
100	5569	SBB	5995	SBT	5997	SBT	5971	SBT	5985	SBT

Table 19
Average number of pulled back railcars for expected value of blocks = 20 (ot = number of outgoing trains, it = number of incoming trains).

ot\it	10	20	30	40	50	60	70	80	90	100
10	421	SBB	485	SBB	511	SBB	532	SBB	535	SBB
20	951	SBB	1152	SBB	1220	SBB	1258	SBB	1239	SBB
30	1476	SBB	1887	SBB	1987	SBB	1939	SBB	1991	SBB
40	2017	SBB	2643	SBB	2656	SBB	2638	SBB	2656	SBB
50	2519	SBB	3292	SBB	3307	SBB	3308	SBB	3288	SBB
60	3246	SBB	3937	SBB	3960	SBB	3954	SBB	3956	SBB
70	3778	SBB	4622	SBB	4629	SBB	4642	SBB	4615	SBB
80	4486	SBB	5288	SBB	5278	SBB	5278	SBB	5276	SBB
90	4970	SBB	5946	SBB	5950	SBB	5956	SBB	5951	SBB
100	5642	SBB	6602	SBB	6629	SBB	6590	SBB	6612	SBB

Table 20
Average number of pulled back railcars for expected value of blocks = 25 (ot = number of outgoing trains, it = number of incoming trains).

ot\it	10	20	30	40	50	60	70	80	90	100
10	454	SBB	539	SBB	559	SBB	572	SBB	576	SBB
20	991	SBB	1246	SBB	1375	SBB	1316	SBB	1291	SBB
30	1625	SBB	1976	SBB	2182	SBB	2208	SBB	2178	SBB
40	2196	SBB	2815	SBB	3023	SBB	3022	SBB	3011	SBB
50	2725	SBB	3408	SBB	3776	SBB	3771	SBB	3768	SBB
60	3442	SBB	4222	SBB	4518	SBB	4523	SBB	4531	SBB
70	4101	SBB	4980	SBB	5293	SBB	5263	SBB	5301	SBB
80	4640	SBB	5915	SBB	6019	SBB	6052	SBB	5999	SBB
90	5364	SBB	6689	SBB	6782	SBB	6772	SBB	6805	SBB
100	6111	SBB	7492	SBB	7532	SBB	7530	SBB	7543	SBB

Table 21
Average number of pulled back railcars for expected value of blocks = 30 (ot = number of outgoing trains, it = number of incoming trains).

ot\it	10	20	30	40	50	60	70	80	90	100
10	469	SBB	595	SBB	608	SBB	645	SBB	644	SBB
20	1080	SBB	1407	SBB	1437	SBB	1494	SBB	1451	SBB
30	1624	SBB	2197	SBB	2389	SBB	2399	SBB	2358	SBB
40	2307	SBB	3066	SBB	3295	SBB	3295	SBB	3296	SBB
50	2940	SBB	3759	SBB	4105	SBB	4128	SBB	4123	SBB
60	3622	SBB	4857	SBB	4930	SBB	4935	SBB	4941	SBB
70	4345	SBB	5058	SBB	5762	SBB	5787	SBB	5772	SBB
80	5086	SBB	6131	SBB	6600	SBB	6580	SBB	6609	SBB
90	5813	SBB	7019	SBB	7417	SBB	7406	SBB	7410	SBB
100	6590	SBB	8009	SBB	8238	SBB	8232	SBB	8233	SBB

Table 22
Average number of pulled back railcars for expected value of blocks = 10 and two sequential periods (ot = number of outgoing trains, it = number of incoming trains).

ot\it	10	20	30	40	50	60	70	80	90	100
10	296	SBB	301	SBB	311	SBB	315	SBB	317	SBB
20	610	SBB	625	SBB	642	SBB	662	SBB	670	SBB
30	925	SBB	968	SBB	1014	SBB	1026	SBB	1047	SBB
40	1236	SBB	1310	SBB	1372	SBB	1390	SBB	1418	SBB
50	1543	SBB	1628	SBB	1726	SBB	1765	SBB	1796	SBB
60	1873	SBB	1957	SBB	2047	SBB	2134	SBB	2192	SBB
70	2174	SBB	2291	SBB	2468	SBB	2506	SBB	2565	SBB
80	2477	SBB	2632	SBB	2840	SBB	2883	SBB	2934	SBB
90	2804	SBB	2981	SBB	3193	SBB	3258	SBB	3338	SBB
100	3084	SBB	3303	SBB	3572	SBB	3601	SBB	3708	SBB

Table 23
Average number of pulled back railcars for expected value of blocks = 20 and two sequential periods (ot = number of outgoing trains, it = number of incoming trains).

ot \ it	10	20	30	40	50	60	70	80	90	100										
10	351	SBB	359	SBB	367	SBB	368	SBB	370	SBB	372	SBB	372	SBB						
20	705	SBB	744	SBB	782	SBB	787	SBB	794	SBB	797	SBB	811	SBB	810	SBB	809	SBB		
30	1070	SBB	1141	SBB	1180	SBB	1210	SBB	1231	SBB	1236	SBB	1246	SBB	1264	SBB	1247	SBB	1248	SBB
40	1444	SBB	1532	SBB	1596	SBB	1664	SBB	1678	SBB	1701	SBB	1702	SBB	1726	SBB	1724	SBB	1733	SBB
50	1807	SBB	1920	SBB	2019	SBB	2091	SBB	2132	SBB	2159	SBB	2172	SBB	2182	SBB	2196	SBB	2194	SBB
60	2184	SBB	2345	SBB	2448	SBB	2531	SBB	2587	SBB	2602	SBB	2622	SBB	2633	SBB	2657	SBB	2670	SBB
70	2536	SBB	2709	SBB	2853	SBB	2961	SBB	3007	SBB	3065	SBB	3107	SBB	3111	SBB	3111	SBB	3140	SBB
80	2887	SBB	3086	SBB	3266	SBB	3408	SBB	3468	SBB	3506	SBB	3568	SBB	3579	SBB	3589	SBB	3589	SBB
90	3249	SBB	3460	SBB	3693	SBB	3813	SBB	3878	SBB	3967	SBB	4019	SBB	4015	SBB	4085	SBB	4064	SBB
100	3606	SBB	3887	SBB	4079	SBB	4272	SBB	4353	SBB	4442	SBB	4445	SBB	4474	SBB	4489	SBB	4531	SBB

Table 24
Average number of pulled back railcars for expected value of blocks = 30 and two sequential periods (ot = number of outgoing trains, it = number of incoming trains).

ot \ it	10	20	30	40	50	60	70	80	90	100										
10	436	SBB	446	SBB	458	SBB	459	SBB	469	SBB	465	SBB	467	SBB	475	SBB	468	SBB	479	SBB
20	881	SBB	945	SBB	970	SBB	998	SBB	998	SBB	1007	SBB	1024	SBB	1020	SBB	1027	SBB	1028	SBB
30	1349	SBB	1441	SBB	1497	SBB	1543	SBB	1571	SBB	1588	SBB	1591	SBB	1601	SBB	1602	SBB	1609	SBB
40	1800	SBB	1952	SBB	2016	SBB	2084	SBB	2134	SBB	2151	SBB	2181	SBB	2196	SBB	2192	SBB	2206	SBB
50	2270	SBB	2444	SBB	2540	SBB	2625	SBB	2689	SBB	2742	SBB	2768	SBB	2782	SBB	2781	SBB	2802	SBB
60	2693	SBB	2898	SBB	3044	SBB	3199	SBB	3239	SBB	3318	SBB	3357	SBB	3382	SBB	3401	SBB	3392	SBB
70	3164	SBB	3411	SBB	3595	SBB	3750	SBB	3845	SBB	3917	SBB	3907	SBB	3960	SBB	3982	SBB	3983	SBB
80	3606	SBB	3911	SBB	4134	SBB	4276	SBB	4407	SBB	4479	SBB	4521	SBB	4544	SBB	4556	SBB	4566	SBB
90	4131	SBB	4387	SBB	4652	SBB	4890	SBB	4981	SBB	5064	SBB	5094	SBB	5126	SBB	5146	SBB	5134	SBB
100	4519	SBB	4913	SBB	5212	SBB	5458	SBB	5525	SBB	5619	SBB	5654	SBB	5684	SBB	5714	SBB	5746	SBB

previous shunted tracks $k' \leq k$ in period t results in the set of blocks w of the sequenced blocks set j which are actually shunted on track k .

If blocks of each shunted and sequenced blocks set are combined, the result is the set of blocks of train $r \in \mathcal{R}$ which are shunted from classification track k to other tracks in period t and can be expressed by $W_{t,k}^{TS/GS,r} = \bigcup_{j=1}^{\bar{g}_t} W_{t,k,j}^{TS/GS,r}$. Finally, the sorting performance for TS and GS is derived as

$$SP_t^{TS/GS} \left(\mathcal{W}_t, \mathcal{R}_t \right) = \bigcup_{k=1, \dots, \bar{g}_t-1} \sum_{r \in \mathcal{R}_t} \left(\sum_{w \in W_{t,k}^{TS/GS,r}} v_{w,r} \right) \quad (20)$$

In each period t sorting performances are determined for each track $k \leq \bar{g}_t - 1$ by summing up railcars of pulled back blocks $w \in W_{t,k}^{TS/GS,r}$ for each train $r \in \mathcal{R}_t$. These sorting performances correspond to the total number of shunted railcars on each track k .

2.2.5. Rolling horizon approach for parallel pullbacks

To derive the sorting performance for PPS in a rolling horizon setting, basic assumptions have to be made. If blocks of not constructable trains are in the classification tracks these blocks are rehumped to the same classification track. If there are no constructable trains in the marshalling yard, no sorting step is carried out. Let \bar{k} be the number of available classification tracks for PPS. Each outgoing train $r \in \mathcal{R}$ is numbered from 1 to n_r , where n_r denotes its number of blocks. d_r marks the number of sets for train $r \in \mathcal{R}$. $s_k^r := \lceil \log_{\bar{k}} d_r \rceil$ denotes the number of sorting steps to construct train $r \in \mathcal{R}$ with \bar{k} available classification tracks. Let $B^r[j]$ ($j = 1, \dots, d_r$) be the initial assignment of blocks of train $r \in \mathcal{R}$ to batches. The set of batches of train $r \in \mathcal{R}$ in sorting step pss on track k can be expressed by

$$BU^r(pss, k, d_r) = \bigcup_{i=0}^{\lim_1(pss, k, d_r)} \bigcup_{j=1}^{\lim_2(pss, k, i, d_r)} B^r \left[j + (k-1) \bar{k}^{pss-1} + \bar{k}^{pss} i \right] \quad (21)$$

$$\lim_1(pss, k, d_r) = \left\lfloor \frac{d_r - (k-1) \bar{k}^{pss-1}}{\bar{k}^{pss}} \right\rfloor \quad (22)$$

$$\lim_2(pss, k, i, d_r) = \min(\bar{k}^{pss-1}, d_r - (k-1) \bar{k}^{pss-1} - \bar{k}^{pss} i) \quad (23)$$

The main idea is to derive sets of blocks by initial sets $B^r[j]$. For each sorting step pss and on each classification track k different initial sets have to be chosen. Therefore, consider the three terms of the square brackets: ‘ j ’ is the amount of consecutively chosen initial sets, i.e. either \bar{k}^{pss-1} initial sets are chosen or if no initial sets are available, less classification tracks are chosen, see $\lim_2(pss, k, i, d_r)$. Term $(k-1) \bar{k}^{pss-1}$ shifts the initial set chosen first for each classification track, e.g. on classification track $k = 1$ the initial set chosen first is $B^r[1]$, on classification track $k = 2$ the second chosen set is $B^r[2]$, and so on. Term $\bar{k}^{pss} i$ shifts the initial sets on a classification track up to $\lim_1(pss, k, d_r)$, e.g. in a marshalling yard with $\bar{k} = 3$ classification tracks in total, the selected initial sets are $B^r[1], B^r[4], B^r[7], \dots$ on classification track $k = 1$ in sorting step $pss = 1$.

Let \bar{t}_{ko} be the period when all blocks of train $r \in \mathcal{R}$ arrived in the marshalling yard, i.e. train $r \in \mathcal{R}$ is constructable. If \bar{g}_t describes the termination criterion of PPS in period t the number of conducted sorting steps before period t can be expressed by $\bar{y}_t = \sum_{t'=\bar{t}_{ko}}^{t-1} (\bar{g}_{t'} - 1)$. Set $W_{t,0}^{PPS,r}$ describes incoming blocks of train $r \in \mathcal{R}_t$ in period $t-1$. Let $W_{t,k,pss}^{PPS,r}$ be the set of shunted blocks of train $r \in \mathcal{R}_t$ in period t on track k for sorting step pss which can be expressed by

$$W_{t,k,pss}^{PPS,r} = \begin{cases} BU^r(1, k, d_r) \cap \bigcup_{t'=1}^t W_{t',0}^{PPS,r} & \text{for } \bar{t}_{ko} > t \\ BU^r(\bar{y}_t + pss, k, d_r) & \text{for } \bar{t}_{ko} \leq t \wedge \bar{y}_t + pss \leq s_k^r \\ \emptyset & \text{for } \bar{t}_{ko} \leq t \wedge \bar{y}_t + pss > s_k^r \end{cases} \quad (24)$$

If train $r \in \mathcal{R}_t$ is not constructable in period t , i.e. $\bar{t}_{ko} > t$, blocks of train $r \in \mathcal{R}_t$ remain or can be rehumped on the track after initial humping. $BU^r(1, k, d_r)$ denotes the set of blocks which are theoretical on track k after sorting step $pss = 1$. $\bigcup_{t'=1}^t W_{t',0}^{PPS,r}$ reveals the blocks in the marshalling yard of train r up to period t . The intersection of both sets denotes the actual set of blocks of train r on track k . If $\bar{t}_{ko} \leq t$ holds, two cases may arise: If $\bar{y}_t + pss \leq s_k^r$, i.e. the number of previous conducted sorting steps plus the actual sorting step of period t is less or equal to the number of necessary sorting steps of train $r \in \mathcal{R}_t$, blocks of train $r \in \mathcal{R}_t$ have to be shunted. Otherwise no more sorting steps of train r are necessary and the set of shunted blocks is empty. Finally, the sorting performance of PPS can be expressed by

$$SP_t^{PPS} \left(\mathcal{W}_t, \mathcal{R}_t \right) = \bigcup_{pss=1}^{\bar{g}_t-1} \bigcup_{k=1}^{\bar{k}} \left\{ \sum_{r \in \mathcal{R}_t} \left(\sum_{w \in W_{t,k,pss}^{PPS,r}} v_{w,r} \right) \right\} \quad (25)$$

Sorting performance values are determined for each sorting step pss and each classification track k in period t . Each value consists of railcars of shunted blocks $W_{t,k,pss}^{PPS,r}$ of train $r \in \mathcal{R}_t$.

3. Emission model for shunting operations

The chosen emission model for the simulation in Section 4 is presented in this section. Because there is no emission model for marshalling yards, a model of the related field rail transportation is applied. An overview of models in rail transportation (microscopic/macrosopic/mesosopic) can be found in Heinold (2020). In this paper the mesoscopic emission model of Kirschstein and Meisel (2015) is applied. The main idea of the paper is to overcome the four resistances rolling P^{roll} , air drag P^{air} , ascent P^{grade} and acceleration P^{inert} . The approximation of a train’s total energy demand is calculated as

$$\bar{E} \left(d, m, \bar{v}, \bar{i}, n^{acc} \right) = \frac{d}{\bar{v}} \left(P^{roll}(\bar{v}, m) + P^{air}(\bar{v}) + P^{grade}(\bar{v}, \bar{i}, m) + n^{acc} \cdot \hat{E}^{inert}(\bar{v}, m) \right) \quad (26)$$

where the three resistances rolling P^{roll} , air drag P^{air} and ascent P^{grade} can be calculated with the average speed of the train \bar{v} and the mass m of the train. However, the energy to overcome acceleration resistance must be approximated by \hat{E}^{inert} with speed v and mass m while parameter n^{acc} represents the average number of acceleration processes per kilometer by the train.

If ϵ denotes the energy transformation efficiency of the locomotive, p the fuel energy coefficient of Diesel and k the GHG emission coefficient of Diesel, the GHG emissions of a diesel train can be calculated with (26) by

$$GHG \left(d, m, \bar{v}, \bar{i}, n^{acc} \right) = \frac{\bar{E}(d, m, \bar{v}, \bar{i}, n^{acc})}{\epsilon} \cdot p \cdot k \quad (27)$$

Generalized marshalling operations consist of ‘inbound train processing’, ‘shunting operations’ and ‘outbound train processing’. Whenever an incoming train arrives in the yard railcars are decoupled and the locomotive is detached. Afterwards, shunting operations are run through a shunting locomotive which is followed by the coupling of railcars and the locomotive. Because incoming and outgoing full trains are only moved over small distances these operations are neglected. Therefore, the main focus is on the shunting operations.

Shunting operations can be distinguished into three suboperations, i. e. humping of the railcars, repositioning of the shunting locomotive and pulling back of railcars. First, the shunting locomotive pushes the railcars from the receiving tracks over the hump into the receiving area. Another shunting operation is the moving of the shunting locomotive from the receiving tracks to the classification tracks. After the arrival at the classification tracks, the shunting locomotive pulls back the railcars from the classification tracks into the receiving tracks. The layout of the marshalling yard determines the distances covered by the railcars and locomotives in each step of the shunting process. Reposition distance of the shunting locomotive from the receiving tracks into the classification tracks is denoted by d^{lp} and from the classification tracks into the receiving tracks by d^{pb} .

Beyond travelling distances, some further parameters have to be determined to apply (27). It is assumed that each railcar has a fixed gross weight m^{RC} and a fixed length l^{RC} . Because total mass includes also the mass of the shunting locomotive, the locomotives weight is denoted as m^{loc} . In (27) height \bar{i} is included for detailed calculation. In marshalling yards \bar{i} represents the height of the hump for the humping process and is set to $\bar{i} = 0$ for the remaining shunting operations. Also the speed \bar{v} is assumed to be fixed and $n^{acc} = 1$. Depending on the selected sorting strategy the number of pullbacks n_t^{pb} in period t and the number of incoming trains n_t^{it} in period t influence the GHG emissions. If s_i^{it} denotes the number of railcars in the incoming train i and s_j^{pb} the number of pulled back railcars in step j the GHG emissions in period t can be calculated by

$$GHG_t(s^{it}, s^{pb}) = n_t^{pb} \cdot GHG(d^{lp}, m^{loc}, \bar{v}, 0, 1) + \sum_{j=1}^{n_t^{pb}} GHG(d^{pb}, m^{loc} + s_j^{pb} \cdot m^{RC}, \bar{v}, 0, 1) + \sum_{i=1}^{n_t^{it}} GHG\left(s_i^{it} \cdot l^{RC}, m^{loc} + s_i^{it} \cdot m^{RC}, \bar{v}, \frac{h}{s_i^{it} \cdot l^{RC}}, 1\right) \tag{28}$$

4. Simulation experiments

The rolling horizon model is evaluated in a simulation study. For this purpose, an exemplary marshalling yard is assumed inspired by a real-world example. The corresponding technical parameters for layout, railcars and locomotives are described in Subsection 4.1. For the remaining parameters (like number of periods or number of outgoing trains) preliminary investigations are conducted to determine reasonable intervals affecting greenhouse gas emissions. The results show that three of five sorting strategies are preferred w.r.t. minimal total emissions, see Subsection 4.2.

4.1. Experimental design

The technical parameters required for the simulation study concern shunting locomotives, railcars and the layout of the yard. In the following, the layout of the marshalling yard in Halle(Saale) is used. To determine distance parameters d^{lp} and d^{pb} . The reposition distance, i.e. the distance from receiving tracks to classification tracks, is set to $d^{lp} = 1$ km. Whenever a shunting locomotive pulls back railcars, the pull back distance is $d^{pb} = 1.5$ km. The length of the classification tracks is 1 km. In contrast to reality, the number of classification tracks is unlimited because the above mentioned sorting strategies (except PPS) cannot be applied when the number of classification tracks is limited (the case of a limited number of classification tracks should be studied in further investigations). The average speed of the shunting locomotive is assumed to be 8 km/h. That is lower than the maximum speed of 25 km/h, but shunting locomotives usually drive slower during shunting due to safety and operational reasons. In the following experiments, the termination

criterion \bar{g}_t for each period is the time when all constructable trains of a period are left in the marshalling yard.

The data generation for the simulation comprises a variety of stochastic variables. For each outgoing train, the number of blocks n_r is modeled by a Poisson distribution $n_r \sim Poi(\lambda)$ where λ describes the expected value of blocks in an outgoing train. The number of railcars of each block is also Poisson distributed with $v_{w,r} \sim Poi(30/\lambda)$, i.e. the expected number of railcars in an outgoing train is 30. Blocks of outgoing trains are randomly assigned to incoming trains which arrive in the yard in a random period. Regarding PPS, the humping sequence of incoming trains is important to know. For this aim, the humping sequence of incoming trains is coincidental in each period.

The railcar weights are based on the railcar types used by Deutsche Bahn (2021). For each railcar type average tare weight and average load limits are calculated based on the available sub-categories. Railway lines are divided into different distance classes depending on the permitted maximum axle load and maximum linear load of a train. Because 86 % of the rail network of DB Netze are assigned to distance class D4 (maximum axle load: 22.5 tons, linear load: 8 tons/meter) (Deutsche Bahn AG, 2019), sub-categories with specification to the considered distance class D4 are involved. If there are no specifications to distance class D4, the considered sub-category is rejected. Average tare weight and average load limits for each railcar type can be found in Appendix A. Because distributions of railcar types in use are hard to find, the weights are chosen as tare weights (10 %, equals empty railcars) or a random number between tare weight plus 50 % of load limit and tare weight plus 100 % of load limit (90 %). Additional parameters of the emission model assumed in the simulation experiments are summarized in Appendix A.

In order to limit the complexity of the simulation experiments, preliminary simulation runs were conducted to screen for the most relevant problem instance parameters. It was suspected that some of the parameters have less impacts on emissions compared to other parameters. Preliminary tests revealed that the number of periods and the number of replications have only small effects on total emissions and are, thus, fixed to 20 periods and 100 runs. The number of classification tracks to be used in PPS is also to be set. As a result of preliminary tests, the number of classification tracks for PPS is reasonably set to the expected value of blocks to be shunted.

Based on the preliminary test, most relevant parameters affecting GHG emissions during shunting are the numbers of incoming and outgoing trains as well as the expected number of blocks. The number of incoming and outgoing trains is varied from 10 to 100 in steps of 10. The expected number of blocks ranges from 5 to 30 in steps of 5. For each simulation setting total GHG emissions for the above-mentioned sorting strategies SBT, SBB, TS, GS and PPS are calculated. The simulation experiments are coded in Java and run on a AMD Ryzen 7 4800H with 8 GB memory.

4.2. Results

For each combination of number of incoming trains, number of outgoing trains and expected number of blocks (λ) the simulation shows that either SBB or SBT works best w.r.t. total GHG emissions. The results can be found in Table 1 and are subdivided for the three varied parameters. For reasons of clarity the tables show only single letters to identify the best sorting strategy. The corresponding emission values can be found in Appendix B.

To get an overview, the five sorting strategies of Table 1 are first assessed by their average relative deviation to the best sorting strategy in terms of total GHG emissions, see Fig. 10. I.e. over all simulation settings, the average deviation to the corresponding best sorting procedure is calculated. The average deviations for all sorting procedures are depicted in Fig. 10. The total average deviation of SBB is close to 0 as it is the best scenario in most cases. SBT, TS and GS produce higher GHG emissions on average than SBB with a surplus of 40–130% on average. PPS performs worst with an average relative performance of 300%

indicating that considering limited numbers of tracks might have a substantial effect on shunting operations.

The average results indicate that SBT and SBB work best. A detailed look at the results reveals, that if the expected number of blocks is small (5 or 10) and the number of outgoing trains is high, SBT is the optimal sorting strategy. For all other combinations, SBB is the best choice to minimize GHG emissions.

Further investigations show that PPS is the best sorting strategy in a specific scenario. In the results above blocks of outgoing trains are distributed on incoming trains over the whole 20 periods. If the interval of periods in which blocks of an outgoing train arrive at the yard comprises only two sequential periods and the number of outgoing trains are low, PPS is the best sorting strategy. This result can be found in [Table 2](#) and the emission values can be found in [Table C](#). For the remaining parameter combinations in this setting SBB is again the best sorting strategy.

To assess the simulation results from another perspective, an additional KPI is introduced. As time is another crucial parameter in shunting operations, the average number of pulled back railcars is a good indicator to evaluate the speed of shunting, i.e. the less railcars are pulled back the less time is needed for shunting. The best sorting strategy w.r.t. minimal average number of pulled back railcars in the same experimental design as above can be found in [Table 3](#). Again, for reasons of clarity the sorting strategies are represented by a single letter and the average number of pulled back railcars for the best sorting strategy can be found in [Appendix D](#). At first sight the results are similar to the results in [Table 1](#), i.e. SBT and SBB are again the best sorting strategies w.r.t. minimal average pulled back railcars. At second glance the behaviour of the best sorting strategy by increasing expected number of blocks per train changes. If the expected number of blocks increases, SBT remains the best sorting strategy in half of all cases. Other strategies (TS, GS, PPS) are still never the best strategy w.r.t. average pulled back railcars. To sum up, SBT is not the best sorting strategy w.r.t. to minimal emissions for an increasing expected number of blocks per outgoing train but shunting time is presumably shorter compared to SBB.

Likewise the results of the experiment with two sequential periods of incoming blocks show a different behaviour. Comparing these results, see [Table 4](#), with previous results, see [Table 2](#), leads to the conclusion that PPS is never the best sorting strategy w.r.t. minimal average pulled back railcars. The numbers of average pulled back railcars for the best sorting strategies can be found in [Table E](#). Hence, PPS is the best sorting strategy w.r.t. minimal emissions for a small number of outgoing trains but shunting needs presumably more time compared to SBB.

5. Outlook

The aim of this article is to find the emission-optimal sorting strategy in shunting yards. For this purpose, sorting strategies well known in literature are embedded in a rolling horizon approach. To assess the sorting strategies' total GHG emissions, performance functions are derived analytically. Experiments with the rolling horizon model results in a simulation study which is conducted for different parameter settings (varying number of incoming/outgoing train,...). The simulation shows that depending on the parameter constellation SBT, SBB, or PPS are the best sorting strategies w.r.t. total emissions. The behaviour of the best sorting strategy varies if the emissions results are compared with the 'average number of pulled back railcars' results. This indicates that shunting operations management has a simple instrument at hand to reduce GHG emissions from shunting operations by selecting a proper sorting strategy.

As studying environmental performance of shunting operations in a rolling horizon approach is new to literature, some further research questions are open. A general assumption to apply SBT, SBB, TS or GS is the unlimited number of classification tracks. In the future, the model can be expanded by incorporating a limited numbers of classification tracks. Some parameters of the emission model are derived by the

marshalling yard in Halle (Saale). Studying other marshalling yard layouts, particularly regarding distances and availability of departure tracks, may lead to further insights in environmental shunting performance. In the above obtained results TS and GS are never the best sorting strategies w.r.t. minimal emissions. In a setting with limited numbers of classification tracks, this may change. Particularly, changing the sorting strategy dynamically depending on the number of ingoing and outgoing trains as well as available classification tracks may lead to further potentials for GHG minimization.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

No data was used for the research described in the article.

Appendix A. Railcar types and technical parameters

[Tables 5 and 6.](#)

Appendix B. Tables of emission values

Emission values of the best sorting strategy for expected railcar numbers 5 to 30 can be found in [Tables 7–12](#).

Appendix C. Tables of emission values for two sequential periods

See [Tables 13–15](#).

Appendix D. Tables of average pulled back railcar values

Average pulled back railcar values of the best sorting strategy for expected railcar numbers 5 to 30 can be found in [Tables 16–21](#).

Appendix E. Tables of average pulled back railcar values for two sequential periods

See [Tables 22–24](#).

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