New Approaches for De-novo Motif Discovery Using Phylogenetic Footprinting: From Data Acquisition to Motif Visualization

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Peer-reviewed publications

This thesis is a cumulative thesis based on the following publications.


I hereby declare that the copyright of the content of the articles Alexiou et al., [2009] and Nettling et al., [2017b] is by Oxford University Press. These papers are available at:

- [http://nar.oxfordjournals.org/content/38/suppl_1/D137](http://nar.oxfordjournals.org/content/38/suppl_1/D137)
- [https://academic.oup.com/bioinformatics/article/2959846](https://academic.oup.com/bioinformatics/article/2959846)

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- [https://bmcbioinformatics.biomedcentral.com/articles/10.1186/s12859-017-1495-1](https://bmcbioinformatics.biomedcentral.com/articles/10.1186/s12859-017-1495-1)
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1 Summary

1.1 English version

The versatility of organisms and their adaptability to environmental changes are essential for their viability and are achieved by expressing proteins on demand. The expression of proteins is orchestrated by the process of gene regulation, which belong to the most complex and comprehensive processes in nature. Hence, the understanding of gene regulation is a prerequisite in modern biology, medicine, and, biodiversity research. A crucial sub-process in gene regulation is the transcriptional initiation, i.e., the interaction of transcription factors (TFs) with their transcription factor binding sites (TFBSs). Hence, predicting TFBSs and their binding motifs in biological sequences is essential for the understanding of gene regulation.

Identifying TFBSs and binding motifs using wet-lab experiments is expensive and time-consuming, and thus neither economical nor feasible. Consequently, bioinformatics approaches have been developed for, first, data acquisition and data preparation, second, for the prediction of putative TFBSs on genomic scale, and third, for the visualization of models for TFBSs.

A typical task in bioinformatics covering these three fields is the prediction of TFBSs in ChIP-sequencing (ChIP-seq) data. This task starts with obtaining sequence data directly from a ChIP-seq experiment or some database. After transforming the data into an appropriate format, de-novo motif discovery is performed and putative TFBSs are predicted. Finally, the results are visualized and compared to related work. This thesis covers six peer reviewed articles and one work-in-progress article, which fit into the mentioned three fields as follows.

First, demanded by business and academic needs, the number of data-intensive processes in bioinformatics, like next generation sequencing, is continuously increasing and so is the amount of produced data. The post-processing of these data increases this amount even further. By combining various data sources and different types of data, like sequence data with gene expression data, the data to manage becomes more and more complex. Hence, new databases are needed for an appropriate handling of complex data and new concepts are needed for an efficient handling of increasingly large data volumes.

My colleagues and I developed miRGen, a relational MySQL database that stores microRNA (miRNA) transcripts with target genes, contained single nucleotide polymor-
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Phenotypes (SNPs), TFBSs in near distance, and prominent literature sources. Over the last years, miRGen has already become an important resource for researchers that are interested in miRNA regulation and miRNA function.

We also developed the open-source Java library DRUMS which is designed to store billions of position specific DNA related records. DRUMS is capable of performing fast and resource sparing requests and runs on a single standard computer. When comparing DRUMS to the standard database MySQL regarding insert performance and lookup performance on two data sets, it outperforms MySQL by a factor of two up to a factor of 15456.

Second, predicting TFBSs in sequence data is essential for the understanding of gene regulation and dozens of bioinformatics approaches have been developed for the prediction of TFBSs. These approaches use diverse statistical characteristics to distinguish TFBSs from their flanking Deoxyribonucleic acid (DNA) and can be subdivided in phylogenetic and non-phylogenetic approaches. Phylogenetic approaches take into account phylogenetic dependencies in aligned sequences of more than one species whereas non-phylogenetic approaches based on sequences of only one species typically take into account intra-motif dependencies. The articles comprising this thesis are related to de-novo motif discovery using phylogenetic approaches as follows.

We extended a traditional phylogenetic footprinting model (PFM) by the capability to take into account the binding affinity bias (BA bias) in ChIP-seq data. The BA bias is a result of the over-representation of high-scoring binding sites in ChIP-seq data, causing the inference of potentially distorted motifs. My colleagues and I found that correcting the binding-affinity bias typically leads to softened motifs and significantly improves motif prediction.

We further studied the influence of phylogenetic trees on the performance of phylogenetic footprinting and motif prediction. We surprisingly found that unrealistic phylogenetic trees often lead to more accurate predictions of TFBSs than realistic phylogenetic trees.

Based on these results, we developed an approach for de-novo motif discovery that extends phylogenetic footprinting by the capability of taking into account intra-motif dependencies of higher order. My colleagues and I found intra-motif dependencies of order 1 and 2 in motifs of all investigated species and we found that modelling intra-motif dependencies within phylogenetic footprinting significantly improves classification performance.

Third, visualizing the results of motif discovery is fundamental for researchers to interpret, present, and share their findings and sequence logos are the de facto standard in biology and bioinformatics to accomplish this task. The number of data sets and motif extraction algorithms is continuously growing and therefor the number of published motifs. Hence, it is often not sufficient to just show motifs but it becomes more and more important.
to perceive differences between motifs. Comparing multiple sequence motifs by visual inspection of the corresponding sequence logos can be tricky and especially differences of multiple motifs of the same TF are often hard to perceive.

To address this problem my colleagues and I developed **DiffLogo**, an R-package that is specifically designed for visualizing differences between similar sequence motifs. **DiffLogo** visualizes differences between multiple motifs in a tabular plot of all pairwise comparisons. The resulting matrix guides the viewer to the most prominent pairwise differences between motifs. **DiffLogo** is already used in several articles of this thesis to depict differences between motifs of the same TF from phylogenetically related species and to depict differences between motifs of the same TF but captured by different de-novo motif discovery approaches.

We know that not all researchers have access to hardware with R and DiffLogo installed and not all researchers have the time or the technical background to use R and DiffLogo without high effort. Hence, we integrated DiffLogo into the web-server **WebDiffLogo** accessible via [http://difflogo.com](http://difflogo.com). This web-server allows the user to upload motifs in several common formats. Further, **WebDiffLogo** allows the user to upload motifs of different length and orientation. Hence, **WebDiffLogo** is much easier to use and thus applicable to a much larger community.

Taken together, the findings of this thesis may advance our understanding of transcriptional gene regulation and its evolution. Specifically, our work in the field of data acquisition and data preparation may improve knowledge transfer among researchers and data handling. Our findings in the field of de-novo motif discovery based on phylogenetic footprinting may lead to an improved prediction of TFBSs. Our work in the field of comparative motif visualisation may help researchers regarding decision making, knowledge sharing, and the presentation of results.
1.2 German version


Die Identifikation von TFBSen und ihren Bindemotiven mittels klassischer Laborexperimente ist jedoch teuer und zeitaufwändig und damit weder ökonomisch noch praktikabel. Folglich wurden bioinformatische Methoden und Ansätze entwickelt, um Daten effizient zu beschaffen und vor zu verarbeiten, um mögliche TFBSen genomweit vorherzusagen und um Modelle für TFBSen zu visualisieren.


1.2 German version

In diesem Kontext haben meine Kollegen und ich miRGen entwickelt, eine relationale MySQL Datenbank zur Speicherung von microRNA (miRNA) Transkripten, angereichert mit deren Zielgenen, mit enthaltenen Einzelnukleotid-Polymorphismen (SNPs), mit TFBS-en in direkter Umgebung und mit prominenten Literaturquellen. miRGen ist bereits zu einer wichtigen Ressource für Forscher geworden, die an der Regulation und der Funktion von miRNAs interessiert sind.

Des Weiteren haben wir die open-source Java Bibliothek DRUMS zur Speicherung von Milliarden von Datensätzen entwickelt, welche sich positionsspezifisch auf Sequenzen beziehen, wie es bei z. B. SNPs der Fall ist. DRUMS ist in der Lage Anfragen schnell und ressourcenschonend zu beantworten und läuft auf Standard-Desktop-Hardware. Bei dem Vergleich von DRUMS mit der Standarddatenbanklösung MySQL bezüglich Einfügegeschwindigkeit und Anfragegeschwindigkeit ist DRUMS 2 bis 15456 mal schneller als MySQL.


In diesem Kontext haben wir als Erstes ein traditionelles Phylogenetic Footprinting Modell um die Fähigkeit erweitert den Bindeaffinitätsbias (BA bias) von TFen in ChIP-seq Daten zu berücksichtigen. Der BA bias resultiert aus der Überrepräsentation von hochqualitativen Bindestellen in ChIP-seq Daten und verursacht die Vorhersage von potentiell verzerrten Motiven. Wir konnten zeigen, dass das Korrigieren des BA bias in der Regel zu weicheren Motiven führt und die Motivvorrhersage signifikant verbessert.


2 Introduction

From 1857 to 1864, Gregor Mendel studied the inheritance patterns in pea plants and suggested the idea of discrete inheritable units. At the same time Darwin published his famous work “On the Origin of Species,” proposing continual evolution of species (Darwin, 1859). It took over 50 years (1909) until Wilhelm Johannsen coined the word gene to name those inheritable units proposed by Mendel, and it took another 44 years before James Watson and Francis Crick published their model for DNA, which is now known as the double-helix model of DNA structure (Watson et al., 1953). Three years later, Francis Crick stated the central dogma of molecular biology for the first time. This dogma describes the relationship between DNA, Ribonucleic acid (RNA), and proteins and was finally published in 1970 (F. Crick et al., 1970). Ever since then, molecular biology has undergone a rapid and extensive development and after 150 years, terms like gene, DNA, RNA, proteins, evolution, and mutation have found its way into our daily language.

This development was accompanied by the digital revolution, starting with the invention of the transistor in 1947, the fundamental building block of any modern digital device. In the 70s, home computers were introduced and the transformation of analog to digital data began. In 1969 the first message was sent over the ARPANET, the predecessor of the Internet, which became publicly accessible in 1991 as the World Wide Web. Nowadays, 50% of the world population has access to the Internet and everybody is passively and actively generating data that can be used to improve our daily lives. For example, GPS data of many individuals can be used to predict traffic anomalies (Pang et al., 2013), data of fitness trackers can be used to prevent cardiovascular diseases (Neubeck et al., 2015), and differences in human genomes can be used to understand the genetic contribution to various diseases (E. P. Consortium et al., 2012; I. G. P. Consortium et al., 2012; Sudmant et al., 2015). It is expected that in 2020 the digital universe will comprise over 5,200 gigabytes per living person, summing up to 40 trillion gigabytes of data (Gantz et al., 2012; Dragland, 2013). The continuously growing quantity of information and its availability at any time, in any place, already permeates both our work and our daily lives.

The digital revolution also enabled new data sources and new technologies in the field of molecular biology, e.g., sequence data and sequencing technologies. Starting in 1990, it took 13 years to sequence the first human genome, whereas in 2015, this task could be accomplished in 26 hours (Miller et al., 2015). The extensive and continuously growing amount of data enabled the emergence of new sciences like bioinformatics, unleashing
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new potentials regarding the study of fundamental biological processes like the complex process of gene regulation. Nowadays, molecular biology is a field of research that serves a broad audience with a scientific background as well as non-scientific backgrounds. In this sense, with this thesis, I want to contribute to a deeper understanding of the process of gene regulation and its evolution. Specifically, my colleagues and I try to contribute to data acquisition and data preparation by developing new databases for knowledge sharing and for efficient data handling. We also attempt to develop new approaches based on phylogenetic footprinting for the de-novo motif discovery in ChIP-seq data. Finally, we try to develop a new approach for the comparative visualization of sequence motifs. The next four sections introduce the reader to molecular biology, computer science, bioinformatics, and the research objectives of this thesis.

2.1 Biological background

This section gives a general introduction into gene expression and gene regulation. The introduction also includes a description of the transcriptional initiation and the post-transcriptional gene regulation by miRNAs.

2.1.1 Gene expression and gene regulation

DNA is the intra-cellular substance that carries the definition of an organism’s potentials. It is composed of the nucleotides of the four organic bases adenine (A), cytosine (C), guanine (G), and thymine (T). The sequence of these bases encodes the genetic information. Genes are information units on the DNA and gene expression is the process used by all known life that translates genes into proteins or functional RNA. In all organisms, gene expression comprises at least two processes, transcription and translation (Figure 2.1). Transcription is the process that transcribes a DNA sequence to the corresponding messenger RNA (mRNA) sequence. Translation is the process that translates the mRNA into the corresponding polypeptide, which may then fold to a protein.

Gene regulation is the process that regulates gene expression and is the basis for cellular differentiation, morphogenesis, versatility, and adaptability of any organism. Whenever a protein is needed, due to e.g., environmental stimuli, a complex signaling cascade is initiated to first, make the corresponding DNA region accessible for the transcription machinery and second, to ensure the correct processing of the genetic information. This fundamental process is established by diverse sub-processes such as epigenetics (Reik, 2007; Slotkin et al., 2007; Dolinoy et al., 2007), regulation by miRNAs (He et al., 2004; K. Chen et al., 2007), siRNA interference (Fougerolles et al., 2007; Tam et al., 2008), and alternative splicing (Sultan et al., 2008; Luco et al., 2010).
2.1 Biological background

![Flowchart of gene expression](image)

**Figure 2.1: Flowchart of gene expression.** A gene is an information unit on the DNA. The process of gene expression typically comprises the two sub-processes transcription and translation. Transcription is the process that transcribes the gene to the corresponding mRNA. Translation is the process that translates the mRNA into the corresponding protein.

2.1.2 Transcriptional initiation

An important sub-process is the initiation of transcription, which is mediated by the interaction of TFs with the DNA. Specifically, TFs are proteins that bind to specific DNA signals, so called TFBSs. TFBSs are often located in the upstream promotor region of a gene but can also be found in other, more distant, intergenic regions. The binding of a TF to a TFBS can enhance or repress the expression of the gene. **Figure 2.2** shows a schematic representation of the binding of three TFs to the DNA to initiate the transcription of the downstream located gene.

Uncovering TFBSs in genomic DNA and inferring DNA binding motifs for TFs also known as de-novo motif discovery, is a prerequisite in modern biology, medicine, and biodiversity research (D’haeseleer, 2006). TFBSs cover short DNA regions of about 10 bases in contrast to the human genome which is about 3.3 billion bases long (Tompa et al., 2005). The complexity of de-novo motif discovery even doubles due to the double strand property of the DNA that allows TFBSs to be located on either of the two reverse complementary DNA strands. Hence, studying gene regulation by time-consuming and expensive wet-lab experi-
2. INTRODUCTION

Figure 2.2: Initiation of transcription. Three transcription factors bind to the DNA to mediate the binding of the basal transcription complex and hence the start of transcription. The gene to transcribe consists of three exons (red) and two introns (yellow).

iments is neither economical nor practical, and the computational investigation of DNA binding motifs and their binding sites seems to be feasible. New approaches for uncovering TFBSs in genomic DNA using phylogenetic footprinting are studied in Sections 3.2.2 and 3.2.3 and in Sections 5.2 and 5.3.

2.1.3 Gene regulation by miRNAs

miRNAs are short single stranded non-coding RNAs with a length of about 22 bases. These post–transcriptionally influence gene expression by binding to specific sites within the 3’-untranslated region (UTR) of mRNAs causing a decrease of gene expression by inhibiting the translation of mRNAs or by directly causing degradation of mRNAs. miRNAs appear to target about 60% of the human genes and other mammals and hence play a key role in the development of organisms (Carrington et al., 2003).

Especially in medicine, the understanding of gene regulation by miRNAs is of great interest since these have been linked to several human pathologies such as cardiovascular and neurodegenerative diseases as well as human malignancies (Calin et al., 2006; Nelson et al., 2008). Further, miRNAs are believed to be involved in many stages of cancer progression by both promoting and suppressing oncogenesis, tumor growth, invasion, and metastasis (Farazi et al., 2011; Small et al., 2011). The influence of miRNAs on gene regulation is studied in Sections 3.1.1 and 4.1.
2.2 Computer science background

This section gives a general introduction to the programming techniques and concepts used in this thesis. Specifically, the first subsection will introduce the reader into Java and the open source Java library Jstacs. The second subsection gives a short overview about R. In the third subsection, the reader finds a brief overview to relational and non relational databases.

2.2.1 The Java programming language and the Java library Jstacs

Java is one of the most popular programming languages in use (O’Grady, 2015). It is concurrent, class-based, and object-oriented (Gosling et al., 2014). Java code needs to be compiled into standard byte code before it can be executed on all platforms that support Java. Regarding this thesis, we use Java to implement DRUMS (Sections 3.1.2 and 4.2) and new approaches for de-novo motif discovery based on phylogenetic footprinting (Sections 3.2.1-3.2.3 and Sections 5.1-5.3).

Jstacs is an open source Java library for the statistical analysis of biological sequences developed by the groups Pattern Recognition and Bioinformatics at the Institute of Computer Science of Martin Luther University Halle-Wittenberg and the Bioinformatics group of the Julius Kuehn Institute (Grau, Keilwagen, et al., 2012). Jstacs provides convenient and efficient classes for the representation of sequence data, many statistical models suitable for the prediction of TFBSs in sequence data, ready to use numerical optimization procedures, and several performance measures. The design of Jstacs is a strictly object-oriented framework with a deep class hierarchy and there is a rich documentation. Hence, Jstacs is easy-to-use, extensible, and customizable to a great extend.

In this thesis, my colleagues and I use Jstacs to implement prototypes of new approaches for de-novo motif discovery based on phylogenetic footprinting (Sections 3.2.1-3.2.3 and Sections 5.1-5.3). Specifically, we extend the class Sample from Jstacs by the capability to handle multi-dimensional sequence data (e.g. alignments). We the resulting class PhyloSample also provides convenient methods for the processing of phylogenetic data. Further, we implement several Models related to phylogenetic footprinting extending Jstacs’ AbstractModel class. This allows us to use optimization procedures and performance measures available in Jstacs and thus facilitates development and decreases the probability of implementation bugs. Finally, we extend Jstacs’ numerical optimization procedures by the capability to optimize parameters from phylogenetic trees and PFM s. We make our implementations available in the PhyFoo project on GitHub.

https://github.com/mgledi/PhyFoo
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shows a high-level overview regarding the usage of Jstacs for prototyping new approaches for de-novo motif discovery based on phylogenetic footprinting.

Figure 2.3: High level overview regarding the usage of Jstacs within the PhyFoo project. Blue puzzle pieces denote Jstacs classes. Green puzzle pieces denote parts of the PhyFoo project.

The phylogenetic footprinting (PF) related models in the PhyFoo project extend Jstacs’ AbstractModel to allow the usage of Jstacs’ optimization procedures and performance measures. This also includes the possibility to wrap PF related models in Jstacs’ StrandModel to allow modelling TFBSs on both DNA strands. Finally, Jstacs’ SingleHiddenMotifMixture class comprises methods to run an EM algorithm on the PF related models. All PF related models need a PhyloSample as input whereas the PhyloSample class extends Jstacs’ Sample class by the capability to handle multi-dimensional sequence data.

2.2.2 The R programming language and Bioconductor

R is a programming language and software environment for statistical computing. In contrast to Java, R is an interpreted language, i.e., R code does not need to be compiled and hence can be executed at any time, allowing the developer to easily and quickly prototype new computational methods. Another reason for the continuously growing popularity of R among researchers is that many libraries exist providing, inter alia, a wide variety of statistical and graphical techniques (Tippmann et al., 2015). At the end of 2016 the Comprehensive R Archive Network (CRAN) package repository features 9699 available packages. Another interesting feature for advanced users is that they can manipulate R objects directly using other, more efficient programming languages like Java, C, C++, or Phython.
2.2 Computer science background

R is extensively used in the field of bioinformatics and Bioconductor is an open development software project that provides many high quality R packages regarding this field (R. C. Gentleman et al., 2004). Specifically, the Bioconductor project provides over 1000 powerful statistical and graphical packages for the analysis of genomic data. Popular examples are the package geneFilter for the filtering of genes from high-throughput data (Bourgon et al., 2010), the package GenomicAlignments for the handling of short genomic alignments (M. Lawrence et al., 2013), and the package seqLogo for the visualization of sequence motifs (Bembom, n.d.). It also provides over 900 packages with annotation data for, e.g., human, mouse, yeast, or rockcress (Huber et al., 2015). A popular example in this group is the biomaRt package which integrates BioMart data resources (e.g. Ensembl) with data analysis software in Bioconductor (Durinck et al., 2005). Further, the Bioconductor project contains more than 300 packages providing extensive experimental data of any kind, e.g., sequencing data or expression data.

I also want to mention the two projects Shiny and OpenCPU that allow the integration of R into a web-server and hence make it easy to publish and share work with other researchers.

Regarding this thesis, R is used to implement DiffLogo (Sections 3.3.1, 3.3.2 and 6.1). DiffLogo is available as R package in the Bioconductor software suite and via GitHub.

2.2.3 Databases

Databases are used to store collections of data. The data are typically organized in a structured way enabling fast and purposeful access. There exist hundreds of different databases that can be divided into two groups.

The first group, relational databases, comprises databases that are based on the relational model of data (Codd, 1970). That means, that data is organized in tables consisting of rows and columns, where each row can be identified with a unique key. Data in a relational database can be queried using structured query language (SQL). Relational databases are used when the structure of the data is well defined, i.e., rely on a schema, and when the data is mainly accessed using complex queries with many relations. Examples for relational databases are MySQL, DB2, or PostgreSQL. Regarding this thesis, MySQL is used for the implementation of miRGen (Sections 3.1.1 and 4.1).

The second group, not only SQL (NoSQL) databases or non relational databases, are often simpler designed than relational databases and typically lack tabular relations. The

https://shiny.rstudio.com/
https://www.opencpu.org/
https://github.com/mgledi/DiffLogo
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data stored in NoSQL databases can be unstructured, i.e., NoSQL databases are typically schema-free. Hence, these databases are typically faster, can store more data, have a higher scalability, and are easier to maintain. Examples for NoSQL databases are MongoDB, Cassandra, or BerkleyDB.

Sometimes, it is not sufficient to just choose a meaningful database or database management system for a certain data handling problem. In these cases a comprehensive storage concept is needed. One example for such a storage concept is the Disk Repository with Update Management (DRUM) concept which was initially proposed by Lee et al. to store billions of URLs with meta-data using a single-server implementation (Lee et al., 2009). The central idea of the DRUM concept is to maintain fast sequential read and write access from and to the underlying storage device by holding and preparing as much records as possible in memory.

In context of this thesis, my colleagues and I propose a NoSQL database based on the DRUM concept for the management of large biological datasets on single desktop hardware (Sections 3.1.2 and 4.2).

2.3 Bioinformatics background

This section introduces the reader into the fields of bioinformatics touched by this thesis and its limitations. Specifically, this section includes a brief description of integration of biological data (Section 2.3.1) and ChIP-seq data analysis (Section 2.3.2). The reader will also be introduced to the idea of de-novo motif discovery based on phylogenetic footprinting (Section 2.3.3) and to the visualization of sequence motifs (Section 2.3.4).

2.3.1 Integration of biological data

With the continuously growing amount of biological data, the need to store, share, and organize it also grows. The current NAR database issue comprises 62 articles describing new biological databases and 112 articles describing updates on existing databases for e.g., storing ChIP-seq data (Daniel J Rigden et al., 2016). The online molecular biology database collection therewith now comprises 1685 biological databases (Daniel J. Rigden et al., 2016).

Biological databases can be divided into primary and secondary databases. Primary databases typically contain data of only one type. Their main purpose is completeness and up-to-dateness. Secondary databases often combine data from primary databases and typically already analyze the data depending on the corresponding requirements.
2.3 Bioinformatics background

My colleagues and I identified two limitations regarding biological databases. First, there exists no database that provides comprehensive information about miRNA transcripts together with their regulation by transcription factors, expression profiles, SNPs, and miRNA targets. We address this problem in Sections 3.1.1 and 4.1. Second, there exists no database that is capable of storing billions of position-specific DNA-related records, performing fast and resource saving requests, and running on a standard personal computer. We propose a database which fulfills these requirements and we present our idea in Sections 3.1.2 and 4.2.

2.3.2 ChIP-seq data analysis

ChIP-seq is a powerful experimental method for identifying binding sites for TFs and other proteins on a genomic scale (T. Bailey et al., 2013). The idea is to immunoprecipitate the DNA-bound protein using a specific antibody. The bound DNA is then coprecipitated, purified, and sequenced resulting in extremely large sets of raw data which necessitate different post-processing steps like quality control, read mapping, and peak detection. Figure 2.4 gives a high level overview over a ChIP-seq experiment.

![Figure 2.4: High level overview of a ChIP-seq experiment.](image)

The filtered ChIP-seq data is then typically subjected to de-novo motif discovery and dozens of approaches exist for this purpose (Tran et al., 2014). Unfortunately, as many...
other techniques, motifs predicted by these computational approaches are distorted by the presence of various biases, such as the ubiquitous binding-affinity bias (Håndstad et al., 2011; Ross et al., 2013; Timothy L. Bailey, Krajewski, et al., 2013). My colleagues and I propose an approach to estimate and diminish the BA bias in ChIP-seq data. We present our idea in Sections 3.2.1 and 5.1.

2.3.3 De-novo motif discovery based on phylogenetic footprinting

The last decade has witnessed a spectacular development of sequencing technologies unleashing new potentials in identifying TFBSs (D. S. Johnson et al., 2007; I. V. Kulakovskiy et al., 2010; Furey, 2012). Countless approaches exist for predicting TFBSs of known TFs and for de-novo motif discovery of TFBSs in sequence data. There are many meaningful ways to group these approaches. Tran et al. (Tran et al., 2014) grouped several motif finding web tools by the way the sequence motif is modelled. The resulting groups are Profiles, consensus sequences (Consensuses), Projections, Graph representations, Clustering of k-mers, and Tree-based data structures. Another way to distinguish different approaches could be by learning principle like generative learning principles and discriminative learning principles. A list with 36 different tools for motif discovery is available in the supplement of the work of Zambelli et al. (2012). In this thesis, we divide approaches for de-novo motif discovery into phylogenetic approaches and non-phylogenetic or single-species approaches.

Due to the increasing number of available genomes from different organisms and due to ever-increasing computational resources, approaches that incorporate sequence information from phylogenetically related species have become increasingly attractive. These approaches can typically be assigned to phylogenetic footprinting or phylogenetic shadowing. The border between both is very blurry as phylogenetic footprinting is called phylogenetic shadowing when a large number of closely related species is used.

The idea behind phylogenetic footprinting and phylogenetic shadowing is that regions containing functional elements, like TFBSs, are considered to evolve more slowly than regions without any functional elements. The reason for this is that mutations in functional elements are more likely to be lethal than mutations in non-functional sequences. Thus, we observe manifested mutations more often in regions without any functional elements than in regions comprising functional elements. With other words, sequences comprising functional elements are subject to a larger evolutionary pressure than sequences without functional elements. To profit from this idea, approaches incorporating sequence information from phylogenetically related species typically use alignments of orthologous sequences as well as a phylogenetic tree that represents the relationship among the species of interest. Figure 2.5 illustrates this idea.
2.3 Bioinformatics background

Figure 2.5: Idea of phylogenetic footprinting. Sequences are denoted by black lines and binding sites are depicted by blue boxes. The upper panel illustrates the idea of de–novo motif discovery ignoring dependencies among orthologous sequences from phylogenetically related species. Orthologous sequences are arranged in rows. All sequences among all species are assumed to be statistically independent from each other.

The lower panel illustrates the idea of de–novo motif discovery incorporating dependencies among orthologous sequences from phylogenetically related species. Each set of orthologous sequences is now aligned. The sequences of an alignment are phylogenetically related, i.e., statistically dependent. The phylogenetic context is given by the phylogenetic tree on the left.

The above described idea helps methods incorporating phylogenetic dependencies to detect functional elements like TFBSs with higher sensitivity compared to methods neglecting phylogenetic dependencies (Moses et al., 2004; Gertz et al., 2006). Several tools using alignments of orthologous sequences have been proposed to uncover TFBSs, e.g., FootPrinter (Blanchette et al., 2003), PhyME (Sinha et al., 2004), MONKEY (Moses et al., 2004), PhyloGibbs (Siddharthan et al., 2005), Phylogenetic Gibbs Sampler (Newberg et al., 2007), PhyloGibbs-MP (Siddharthan, 2008), and MotEvo (Arnold et al., 2012).

All of these approaches use a phylogenetic tree with predefined substitution probabilities as preliminary input, but none of them investigates the influence of different phylogenetic trees and different substitution probabilities on classification performance and motif prediction on ChIP-seq data. My colleagues and I fill this knowledge gap in Sections 3.2.2 and 5.2. Another limitation of these approaches is that they neglect intra–motif dependencies, although it has been shown that more complex motif models that take into account intra–motif dependencies outperform simpler motif models like the position weight matrix (PWM) model. We address this problem in Sections 3.2.3 and 5.3.
2. INTRODUCTION

2.3.4 visualization of sequence motifs

An important task in research is the visualization of results and sequence logos are the *de facto* standard for visualizing sequence motifs obtained from *de-novo* motif discovery (Schneider et al., 1990). A sequence logo represents the characteristics of each motif position by the two properties stack height and symbol height within a stack. The stack height is proportional to the information content of the symbol distribution and the symbol height is proportional to the degree of symbol abundance. **Figure 2.6** shows an example of two similar sequence logos of the TF CTCF.

![Sequence logos](image)

**Figure 2.6:** Sequence logos of the CTCF motifs from the cell lines H1-hESC (left) and HUVEC (right). The two sequence logos are highly similar in their conservation profile (height of stacks) and nucleotide preferences at the individual motif positions.

Sequence logos are used by researchers to interpret findings, document work, share knowledge, and present results. However, comparing multiple sequence logos by visual inspection is tricky, especially when the sequence motifs to compare are highly similar as in **Figure 2.6**. My colleagues and I address this problem in **Sections 3.3.1** and **6.1**.

2.4 Research objectives

The previous three sections introduced the reader to molecular biology, computer science, and bioinformatics. Six limitations in fields “data acquisition and data preparation,” “*de-novo* motif discovery using *phylogenetic footprinting*,” and “visualisation of sequence motifs” were shown, which my colleagues and I wish to address as follows.

First, we wish to improve knowledge sharing in the field of miRNA-induced gene regulation and we wish to develop a new approach for the efficient storage of sequence related data with standard desktop hardware. Second, we wish to develop new approaches for *de-novo* motif discovery based on *phylogenetic footprinting*. Specifically, we propose an approach
2.4 Research objectives

based on phylogenetic footprinting to detect and correct the ubiquitous BA bias in ChIP-seq data. Further, we systematically study the influence of phylogenetic trees with different substitution probabilities on the classification performance of phylogenetic footprinting using synthetic and real data. Finally, we extend phylogenetic footprinting by the capability of taking into account intra-motif dependencies. Third, we wish to improve the comparative visualization of sequence motifs.

An important task in bioinformatics is the prediction of TFBSs in sequence data. This task typically starts with data acquisition and data preparation, e.g., sequence data are obtained from a ChIP-seq experiment. After transforming the data into an appropriate format, de–novo motif discovery is performed and putative TFBSs are predicted. Finally, the results are visualized and compared to related work. With this thesis, I wish to contribute to each of these three steps.
3 Context of publications

This chapter introduces the reader to the articles assembling this thesis. As indicated in Section 2.4, these articles can be divided into the three groups “Data acquisition and data preparation,” “De–novo motif discovery using phylogenetic footprinting,” and “Visualisation of sequence motifs.” With all six publications and the one work-in-progress article my colleagues and I want to contribute to the understanding of the process of gene regulation and its evolution. Figure 3.1 shows the applicability of the six peer reviewed publications and the one work-in-progress article and their relatedness to the process of gene regulation.

Figure 3.1: Articles of this thesis in context of gene expression. The first column summarizes the process of gene regulation. The second column (red) shows the two publications related to “Data acquisition and data preparation”. The third column (blue) shows the three publications related to “De–novo motif discovery using phylogenetic footprinting”. The fourth column (green) shows the publications and the one work-in-progress article related to “Visualisation of sequence motifs”.

Data acquisition and data preparation are essential and preliminary tasks in all natural sciences. In the context of this thesis it would be impossible to perform phylogenetic footprinting without acquiring sequences from databases or similar sources and without aligning them in a preprocessing step. Further, the comparative visualization of sequence motifs using DiffLogo would be hardly possible without databases providing sequence motifs. Publications presented in this thesis related to this “Data acquisition and data preparation” are “miRGen 2.0: a database of microRNA genomic information and reg-
3. CONTEXT OF PUBLICATIONS

De–novo motif discovery is an essential task in bioinformatics and a preliminary for understanding the process of gene regulation. Phylogenetic footprinting comprises approaches for de–novo motif discovery that take into account sequences of at least two phylogenetically related species. Publications presented in this thesis related to “De–novo motif discovery using phylogenetic footprinting” are “Detecting and correcting the binding-affinity bias in ChIP-seq data using inter-species information”, “Unrealistic phylogenetic trees may improve phylogenetic footprinting”, and “Combining phylogenetic footprinting with motif models incorporating intra-motif dependencies”. All three proposed approaches may lead to an improved prediction of TFBSs and thus advance our understanding of transcriptional gene regulation and its evolution.

The visualization of results is an essential task in all sciences and it is needed to interpret findings, document work, share knowledge, and present results. Work related to “Visualisation of sequence motifs” in this thesis are the publication “DiffLogo: a comparative visualization of sequence motifs” and the work-in-progress article “WebDiffLogo: A web-server for the construction and visualization of multiple motif alignments”.

The following subsections will introduce the reader into the publications and the one work-in-progress article comprising this work (Figure 3.1) and provide for each work a summary on the addressed objectives, the used methods, and the results. The full articles are presented in Chapters 4, 5, and 6.

3.1 Data acquisition and data preparation

The next two subsections provide a short summary of our publications “miRGen 2.0: a database of microRNA genomic information and regulation” and “DRUMS: Disk Repository with Update Management and Select option for high throughput sequencing data”.

3.1 Data acquisition and data preparation

3.1.1 miRGen 2.0: a database of microRNA genomic information and regulation

The main objective of this work is to provide microRNA transcripts with related information to researchers of diverse disciplines who are interested in the regulation and function of microRNAs. Therefore, we collect microRNA transcripts from prominent literature sources and enrich these transcripts with information about TFBSs near the transcription start sites (TSS), microRNA expression profiles, and SNPs in microRNA hairpins.

Methods

In this work, we collect 812 human microRNA coding transcripts and 386 mouse microRNA coding transcripts from four literature sources. We identify for each microRNA primary transcript putative TFBSs in the region 5 kb upstream and 1 kb downstream of the TSS using MatchTM (Kel et al., 2003) and all vertebrate PWMs from Transfac 6.0 (Matys et al., 2003) minimizing the number of falsely predicted TFBSs. We provide for each predicted TFBS the matrix similarity score and the core similarity score calculated by MatchTM. We also identify microRNA expression profiles using the mammalian microRNA expression atlas (Ozsolak et al., 2008). We integrate data about SNPs located within the genomic positions corresponding to microRNA hairpins and TFBSs from the UCSC table browser (Karolchik et al., 2009). All data of the miRGen repository are stored using the relational database management system MySQL. Figure 3.2 shows the relational schema of the database.

Results, discussion, and conclusions

Over 800 microRNA transcripts with TFBSs near their TSS microRNA expression profiles, and SNPs in the microRNA hairpins are stored in the miRGen repository and are accessible via a user-friendly interface that allows searches for microRNAs and/or TFs of interest. The integration of the different information sources enables in-depth studies of microRNAs functions and contributes to the understanding of post-transcriptional gene regulation. Currently, miRGen is cited by more than 100 articles, specifically in the field of cancer research (Juan et al., n.d.; H.-D. Huang, 2012; Mar-Aguilar et al., 2016) and hence contributes to cancer diagnostics and therapeutics.

The TFBS annotations in miRGen from 2009 could be improved by using more sophisticated algorithms and motif models (instead of the PWM motif model) for the prediction of TFBSs. In addition, http://www.factorbook.org/ (J. Wang et al., 2012) meanwhile provides extensive information for 167 TFs and their PWM representations for many exper-
3. CONTEXT OF PUBLICATIONS

Figure 3 shows an overview of the interface and highlights links to external databases—UCSC genome browser (13), iHop (16), dbSNP (14), mirBase (11).

DISCUSSION

This version of miRGen is the first attempt to build a widely accessible and user-friendly database that connects TFs and miRNAs through putative and experimentally supported functional relationships. The connections identified in the database will further our understanding of the TF-mediated regulation of miRNA genes, and pave the way for the mapping of the interplay between TFs and miRNAs as regulatory molecules.

The identification of SNPs on miRNA locations and their corresponding TFBSs, as well as the expression profiles of miRNAs can improve our insight into the involvement of miRNAs in developmental processes and disease.

Deregulation of TF-mediated gene expression has been shown to extensively affect protein coding genes, and lead to disease (17,18). MiRNA expression levels have also been shown to change significantly in different disease states (19,20). The availability of both these resources in the same database will allow researchers to identify regulatory elements, such as TFs that may affect the expression of miRNAs. For this reason, we believe miRGen 2.0 will be an important resource for researchers of diverse disciplines interested in miRNA regulation and function.

AVAILABILITY

The miRGen database will be continuously maintained and freely available at http://www.microrna.gr/mirgen/.

---

Figure 3.2: The miRGen database schema. TFs (top left) activate miRNA genes (top center) by binding to TFBSs (middle left). miRNA genes (top center) contain miRNA hairpins (middle right) that signify the genomic location of the mature miRNA-miRNA* duplex. miRNA hairpins are processed into mature miRNAs. Typically, one miRNA hairpin produces two mature miRNAs, but a mature miRNA can be produced by more than one hairpin from different miRNA genes. Both TFBSs and miRNA hairpins are genomic features that can contain SNPs. Mature miRNAs are associated with expression levels in various tissues and cell types.
3.1 Data acquisition and data preparation

Experiments from the ENCODE project (E. P. Consortium et al., 2004). Since many researchers use data from the ENCODE project for their research it would be of advantage if miRGen would use PWMs predicted on the very same data.

This work refers to version 2.0 of miRGen. The current version of miRGen is 3.0. miRGen is freely available at [http://www.microrna.gr/mirgen/](http://www.microrna.gr/mirgen/).

3.1.2 DRUMS: Disk Repository with Update Management and Select option for high throughput sequencing data

An important task of bioinformatics in the scope of computational biology projects is the efficient and well-organized data management. In fact often neglected, this issue becomes essential when dealing with many data sets that consist of millions or even billions of records. In addition, researchers from biology and biochemistry prefer to keep and analyze these data sets on a standard desktop machine for reasons of data privacy, limited computer skills, and convenience. Noble, 2009 describes how to organize data in computational biology projects and Wilson et al., 2014 describes best practices for scientific computing. In this work we tackle the problem of handling large data sets on a single standard desktop machine.

One kind of data extensively used in bioinformatics is position specific data related to DNA sequences. Examples are SNPs (Single Nucleotide Polymorphism 2012), transcription factor binding affinities, and probabilities (M. Bulyk, 2003; Nguyen et al., 2009), RNAseq data (Z. Wang et al., 2009; Malone et al., 2011), and mapping data from BLAST (M. Johnson et al., 2008). These data are essential for the understanding of biological and biochemical processes. We generalize this kind of data by the term position-specific DNA related data (psDrd).

Due to the rapid development of sequencing technologies and the ever-increasing number of tools and algorithms for analysing, manipulating, and combining psDrd the data volume is growing exponentially. Thus, requesting data becomes challenging and expensive and is often tackled using specialised and/or distributed hardware. The objective of this work is the development of a data repository that is capable of storing billions of records of psDrd, performing fast and resource saving requests, and running on a single standard desktop hardware.

Methods

psDrd records have the following three characteristics that are important for finding or developing a suitable data repository. First, a psDrd record is representable by a key-value
pair, consisting of a unique key that defines a position on a sequence and a value that is associated to this sequence position. Second, all psDrd records of the same kind are storable using the same amount of memory. Third, researchers who work with psDrd are usually interested in all records near a certain sequence locus and the exact position of this locus is typically unknown.

By literature research we found the DRUM concept which was designed to store billions of URLs with meta data when crawling the world wide web (Lee et al., 2009). DRUM is already capable of storing large collections of key-value pairs by supporting fast bulk inserts without generating duplicate entries. Unfortunately, DRUM was not designed to request data in an efficient manner. We extended the DRUM concept by the capability of requesting a single record by key or a set of records in an interval between two keys. We developed the open-source Java library DRUMS meeting our requirements.

During the implementation of DRUMS, we focused on decoupling I/O-processes from memory processes to avoid blocking single components. We made extensively use of the prototype design pattern and the flyweight design pattern to reduce object instantiations. This relieves Java’s object heap and hence dramatically reduces the number of runs of Java’s garbage collector. Figure 3.3 gives a high level overview of the insert process and the select process.

Results, discussion, and conclusions

We compared the performance of our implementation of DRUMS to the widely spread standard database MySQL on two data sets, considering database inserts, random lookups, and random range selects. The smaller data set contains SNPs for 251 accessions of the reference plant Arabidopsis thaliana. The larger data set represents a mapping of over 7000 HERV-fragments to the human genome which comprises more than 800 million records. In each test, DRUMS was considerably faster than MySQL by a factor of 2 up to a factor of 15456.

Based on this work, we added an additional feature to DRUMS which has not been evaluated systematically nor published yet. Namely, we added the capability of performing state dependent updates without rewriting or reorganising the files on disk. For example, to increment a counter in a traditional key-value store, first the counter is requested by key, then the fetched counter is incremented, and finally the incremented counter is written back as a new key-value pair. In contrast, DRUMS is capable of manipulating the corresponding data directly on disk resulting in a dramatic performance increase.

DRUMS is freely available at http://mgledi.github.io/DRUMS/
3.2 Predicting transcription factor binding sites using *phylogenetic footprinting*

The next three subsections provide a short summary of our publications “Detecting and correcting the binding-affinity bias in ChIP-seq data using inter-species information”, “Unrealistic phylogenetic trees may improve phylogenetic footprinting”, and “Combining phylogenetic footprinting with motif models incorporating intra-motif dependencies”.

A common mathematical starting point for all three publications is the statistical model for a motif bearing alignment. The probability that the alignment $X_n$ of length $L_n$ is generated by the PFM as a motif bearing alignment is:

$$
p(X_n | \theta) = \sum_{\ell_n = 1}^{L_n - W + 1} \frac{1}{L_n - W + 1} \prod_{u=1}^{L_n} \sum_{Y_u^{\ell_n}} p(Y_u^{\ell_n} | \ell_n, \theta) \prod_{o=1}^{O} p(X_u^{o, \ell_n} | Y_u^{\ell_n}, \ell_n, \theta) \quad (3.1)
$$

where $O$ denotes the number of species, $W$ denotes the length of the motif, $\ell_n$ denotes the position of the motif, $X_u^{o, \ell_n}$ denotes the $u$-th symbol of the $o$-th sequence of the $n$-th align-
3. CONTEXT OF PUBLICATIONS

3.2.1 Detecting and correcting the binding-affinity bias in ChIP-Seq data using inter-species information

The computational investigation of genomic regions containing TFBSs is a prerequisite for elucidating the process of gene regulation. ChIP-seq has become the major technology to uncover genomic regions containing TFBSs and countless approaches exist for predicting motifs from these genomic regions. It is known that ChIP-seq data and similar experimental data is contaminated with false positive genomic regions and there is evidence that there is an enrichment with high-affinity binding sites. Both factors potentially distort the results of de novo motif prediction which would affect all downstream analyses (Ross et al., 2013; Park et al., 2013; Teytelman et al., 2013; Elliott et al., 2015).

The contamination with false positive genomic regions leads to the contamination bias (Timothy L. Bailey, Krajewski, et al., 2013) and thus to the prediction of artificially softened motifs, whereas the enrichment of sequences with high-affinity binding sites leads to the binding-affinity bias (Handstad et al., 2011) and thus to the prediction of artificially sharpened motifs. Most existing approaches for de novo motif prediction are capable of detecting and correcting the contamination bias and it has been shown that this increases the quality of motif prediction considerably (Timothy L. Bailey and Elkan, 1995; Wilbanks et al., 2010; Gomes et al., 2014).

The main objective of this work is to detect and correct the binding affinity bias and to improve phylogenetic footprinting by extending a traditional PFM that already takes into account the contamination bias by the capability to also take into account the BA bias.

Methods

To our knowledge, it is impossible to detect the BA bias based on sequence data from only one species, but detecting the BA bias appears to be possible using sequences from phylogenetically related species. The key idea is that mutations decrease the effect of BA bias in phylogenetically related species. Hence, the direct effect of the BA bias in the reference species is stronger than the indirect effect of the BA bias in phylogenetically related species. Under this assumption the information content of the predicted motif in the reference species should be higher than the information content of the predicted motifs in
3.2 Predicting transcription factor binding sites using phylogenetic footprinting

phylogenetically related species. More specifically, the information content of the predicted motifs in the phylogenetically related species should decrease with the phylogenetic distance from the reference species. The detailed idea and a toy example can be found in the section "Using sequence information of phylogenetically related species to detect the binding-affinity bias" of the corresponding article (Nettling et al., 2016).

We investigate our hypothesis on 2132 sequence alignments comprising human ChIP-seq data of the five TFs CTCF, GABP, NRSF, SRF, and STAT1 with orthologous regions from the monkey, dog, cow, and horse by comparing the degree of information content in species-specific motifs. We propose a PFM capable of taking into account the contamination bias ($M^C$), the BA bias ($M^B$), neither one or the other ($M^−$), or both ($M^{CB}$). We model the contamination bias using the popular zero or one occurrence of a binding site per sequence (ZOOPS) model, which is widely used for de-novo motif discovery (C. E. Lawrence et al., 1993; Redhead et al., 2007; Keilwagen et al., 2011; Agostini et al., 2014) and we model the effect of the BA bias using the Boltzmann distribution from thermodynamics (Maza et al., 1993). We transformed Formula 3.1 in a way that the statistical model of a motif bearing alignment $X_n$ of length $L_n$ consisting of sequences from $O$ species is defined as:

$$p(X_n|\theta) = \frac{1}{L_n - W + 1} \prod_{u=1}^{L_n} p(X_{n}^{u,1}|\ell_n, \theta) \sum_{Y_n^u \in \mathcal{A}} p(Y_n^u|X_{n}^{u,1}, \ell_n, \theta) \cdot \prod_{o=2}^{O} p(X_{n}^{u,o}|Y_n^u, \ell_n, \theta).$$

(3.2)

The inner factors of the sum are defined as follows:

$$p(X_{n}^{u,1}|\ell_n, \theta) = \left\{ \begin{array}{ll} \pi_0^a & \text{if } u < \ell_n \text{ or } u \geq \ell_n + W \\ \frac{\pi_a^a (\pi_{n-\ell_n+1})^a}{\sum_{a \in \mathcal{A}} (\pi_{n-\ell_n+1})^a} & \text{if } \ell_n \leq u < \ell_n + W \end{array} \right.$$  

(3.4)

$$p(Y_n = a|X_{n}^{u,1} = b, \ell_n, \theta) = \left\{ \begin{array}{ll} \gamma_1 \cdot \pi_0^a + (1 - \gamma_1) \cdot \delta_{a=b} & \text{if } u < \ell_n \text{ or } u \geq \ell_n + W \\ \gamma_1 \cdot \pi_a^a + (1 - \gamma_1) \cdot \delta_{a=b} & \text{if } \ell_n \leq u < \ell_n + W \end{array} \right.$$  

(3.5)

$$p(X_{n}^{u,o} = a|Y_n = b, \ell_n, \theta) = \left\{ \begin{array}{ll} \gamma_o \cdot \pi_0^a + (1 - \gamma_o) \cdot \delta_{a=b} & \text{if } u < \ell_n \text{ or } u \geq \ell_n + W \\ \gamma_o \cdot \pi_a^a + (1 - \gamma_o) \cdot \delta_{a=b} & \text{if } \ell_n \leq u < \ell_n + W \end{array} \right.$$  

(3.6)

where $\pi_0^a$ denotes the probability of a base $a$ in the background sequence, $\pi_a^a$ denotes the probability of a base $a$ in the motif sequence, $\gamma_o$ denotes the substitution probability from the primordial species to species $o$. 


3. CONTEXT OF PUBLICATIONS

\( \beta \) denotes the inverse temperature from the Boltzmann distribution and quantifies the degree of the BA bias in the reference species. We assume that a TF binds the binding site \( B \) with a probability proportional to \( p(B|\pi)^{\beta-1} \). As \( B \) occurs in vivo with probability \( p(B|\pi) \), it occurs in the set of immunoprecipitated sequences with a probability proportional to \( p(B|\pi) \cdot p(B|\pi)^{\beta-1} = p(B|\pi)^{\beta} \). A value for \( \beta \) greater than one indicates that the ChIP-seq data set is affected by the binding-affinity bias, i.e., high-affinity binding sites are over-represented.

In Supplementary Section 1 of the corresponding article and in Section 7.1.1 of this thesis, the reader can find a detailed definition of the probabilistic model that is capable of taking into account both the contamination bias and the BA bias. In the corresponding article, we describe the PFM that is capable of taking into account the BA bias from the perspective of the data generating process.

We measure the classification performance of the four models \( \mathcal{M}_- \), \( \mathcal{M}_{BA} \), \( \mathcal{M}_C \), and \( \mathcal{M}_{BA}^C \) using 100 fold stratified repeated random sub-sampling validation. We calculate the information contents of the motifs predicted by the models taking into account the BA bias and the models neglecting the BA bias. We use DiffLogo to investigate differences in sequence motifs predicted by \( \mathcal{M}_{BA} \) and \( \mathcal{M}_{BA}^C \) and the traditional motifs predicted by \( \mathcal{M}_- \) and \( \mathcal{M}_C \).

Results, discussion, and conclusions

We found in case of all five TFs that the information contents of the human motifs are significantly higher than the information contents of the motifs from the monkey, dog, cow, and horse. We also found that the correction of the BA bias is possible using the proposed PFM leading to a more accurate inference of sequence motifs and to a more precise prediction of TFBSs. Interestingly, we found that the enrichment of ChIP-seq data with high-affinity binding sites causes a distortion of DNA binding motifs that is even stronger than the distortion caused by the contamination bias. The comparison of novel and traditional motifs showed small but noteworthy differences, suggesting that the refinement of traditional motifs from literature and databases might lead to the inference of novel binding sites, cis-regulatory modules, and gene-regulatory networks and may thus advance our attempt of understanding transcriptional gene regulation as a whole.

3.2.2 Unrealistic phylogenetic trees may improve phylogenetic footprinting

Two prerequisites for most phylogenetic footprinting algorithms are multiple sequence alignments (MSAs) of the DNA regions to analyse and phylogenetic trees, including substitution
3.2 Predicting transcription factor binding sites using phylogenetic footprinting

Probabilities attached to the branches. These phylogenetic trees are used to quantify the evolution of functional elements and their flanking DNA in the input MSAs. Hence, the choice of the phylogenetic trees and the substitution probabilities has a strong influence on the performance of phylogenetic footprinting and hence on the prediction of TFBSs (Kc et al., 2011). Typically, the phylogenetic trees used by nature to evolve the DNA regions of interest have been lost and are unknown. Estimating appropriate phylogenetic trees with appropriate substitution probabilities is hardly possible (Blanchette et al., 2003), so that the needed information is often simply taken from literature or guessed.

There are many articles that state that phylogenetic footprinting improves motif prediction but none of them investigates the influence of different phylogenetic trees on classification performance and motif prediction on non-synthetic data (Moses et al., 2004; Gertz et al., 2006; Clark et al., 2007; Hardison et al., 2012). Thus, the main objective of this work is to study systematically the influence of the phylogenetic trees on the performance of phylogenetic footprinting.

Methods

To systematically investigate the influence of phylogenetic trees on the performance of phylogenetic footprinting we made the following simplification. The PFM uses a star topology instead of a more complex phylogenetic tree with all branches having the same length, i.e., the substitution probability γ is the same for all species. With this simplification it is now possible to investigate the performance of a PFM as function of the substitution probability γ, where small γ encode closely phylogenetic relations and large γ encode loosely phylogenetic relations. The statistical model of a motif bearing alignment looks different to Formula 3.1 but is the same. We extracted the parameter γ from the set of parameter set θ. The probability that the alignment Xn of length Ln consisting of sequences from O observed species can be calculated as follows:

\[
p(X_n|\gamma, \theta) = \sum_{\ell_n=1}^{L_n-W+1} \frac{1}{L_n-W+1} \prod_{u=1}^{L_n} \sum_{Y_u} p(Y_u^n|\ell_n, \gamma, \theta) \prod_{o=1}^{O} p(X_u^n|Y_u^n, \ell_n, \gamma, \theta) \tag{3.7}
\]

The inner factors are defined as follows:

\[
p(Y_u^n|\ell_n, \gamma, \theta) = \begin{cases} 
\pi_0^a & \text{if } u < \ell_n \text{ or } u \geq \ell_n + W \\
\pi_{u-\ell_n+1}^a & \text{if } \ell_n \leq u < \ell_n + W 
\end{cases} \tag{3.8}
\]

\[
p(X_u^n|Y_u^n, \ell_n, \gamma, \theta) = \begin{cases} 
\gamma \times \pi_0^a + (1 - \gamma)\delta_{a=b} & \text{if } u < \ell_n \text{ or } u \geq \ell_n + W \\
\gamma \times \pi_{u-\ell_n+1}^a + (1 - \gamma)\delta_{a=b} & \text{if } \ell_n \leq u < \ell_n + W 
\end{cases} \tag{3.9}
\]
3. CONTEXT OF PUBLICATIONS

where $\pi_0^a$ denotes the probability of a base $a$ in the background sequence, $\pi_w^a$ denotes the probability of a base $a$ in the motif sequence, $\gamma_k$ denotes the substitution probability from the primordial species to species $k$. The complete statistical model and all parameters are explained in Methods 1 of the corresponding article.

We investigate the classification performance and the likelihood of the $\text{PFM}$ for $\gamma = \{0.05, 0.1, \ldots, 1.0\}$ on human ChIP-seq data of the five TFs CTCF, GABP, NRSF, SRF, and STAT1 enriched with orthologous regions from the monkey, dog, cow, and horse as well as on synthetic data generated using a $\text{PFM}$ with $\gamma = 0.2$. We further compare the classification performance of the three $\text{PFMs}$ using a tree from literature (Arnold et al., 2012) ($M_{\text{tree lit}}$), a star topology with the maximum likelihood estimated $\gamma$ ($M_{\gamma=1.0}^{\text{star ML}}$), and a star topology with $\gamma = 1$ ($M_{\gamma=1.0}^{\text{star}}$).

Results, discussion, and conclusions

When studying the likelihood, we found that on synthetic data the best likelihood is achieved when using the same phylogenetic tree for learning as for data generation. We also observed that on organic data the best likelihood is achieved when using realistic phylogenetic trees indicating that we are capable of identifying reasonable substitution probabilities for synthetic and for real data using the maximum-likelihood principle.

When investigating the classification performance, we found that on synthetic data the best classification performance is achieved when using the same phylogenetic tree for learning as for data generation. In contrast, we found that on organic data unrealistic phylogenetic trees often lead to more accurate predictions of transcription factor binding sites than realistic phylogenetic trees. We also observed that $M_{\gamma=1.0}^{\text{star}}$ significantly outperforms $M_{\gamma=1.0}^{\text{star ML}}$ and $M_{\text{tree lit}}$. With other words, choosing unrealistic model assumptions with phylogenetic footprinting – namely using a star topology with unrealistic large substitution probabilities – may yield higher classification performances than using realistic phylogenetic trees with more realistic substitution probabilities.

Although we have no concrete explanation for this observation, we speculate that evolutionary effects like heterogeneous and heterotachious substitution probabilities among different DNA positions are violating model assumptions like the assumption of time reversibility. Further, these effects might already have lead to the construction of incorrect or at least partially erroneous $\text{MSAs}$. $\text{PFMs}$ using a star topology with substitution probabilities of $\gamma = 1$ seem to be more robust toward these effects than $\text{PFMs}$ using realistic phylogenetic trees with realistic substitution probabilities. Hence, we need to give the strange but practical recommendation to use $\text{PFMs}$ based on these unrealistic model assumptions until there are more appropriate $\text{PFMs}$ that take into account heterogeneity and heterotachy as well as putative misalignments in the input $\text{MSAs}$. 
3.2 Predicting transcription factor binding sites using phylogenetic footprinting

3.2.3 Combining phylogenetic footprinting with motif models incorporating intra-motif dependencies

As stated repeatedly in this work, de-novo motif discovery is a challenging task in bioinformatics and many different approaches exist for solving this task. These approaches can be divided in two groups.

The first group comprises approaches using sequences of only one species, which we refer to as one-species approaches. Within this group, a variety of statistical models are used for the binding of TFs to their TFBSs ranging from the simple PWM model, neglecting intra-motif dependencies, to more complex models, taking into-account intra-motif dependencies (Grau, Posch, et al., 2013; I. Kulakovskiy et al., 2013; Ma et al., 2014; Alipanahi et al., 2015; Siebert et al., 2016).

The second group comprises approaches using sequences of at least two phylogenetic related species, which is known as phylogenetic footprinting. Within this group, statistical models are used that are capable of modeling the binding of TFs to their TFBSs and their evolution simultaneously (Blanchette et al., 2003; Sinha et al., 2004; Moses et al., 2004; Siddharthan et al., 2005; Neph et al., 2006; Newberg et al., 2007; Siddharthan, 2008; Arnold et al., 2012).

It has been shown that more complex motif models taking into account intra-motif dependencies outperform simpler motif models like the PWM model and that models that take into account phylogenetic dependencies also outperform the PWM model (M. L. Bulyk et al., 2002; Salama et al., 2010; Eggeling et al., 2015). One-species approaches neglect phylogenetic information, whereas phylogenetic footprinting, which incorporates this information, neglects intra-motif dependencies.

The main objective of this work is to improve phylogenetic footprinting by taking into account base dependencies, i.e., developing an approach for de-novo motif discovery that takes into account both phylogenetic dependencies and base dependencies simultaneously.

Methods

We extend a PFM model based on the Felsenstein evolutionary model (Felsenstein, 1981) by the capability of taking into account base dependencies resulting in a model that is capable of taking into account base dependencies and phylogenetic dependencies simultaneously. We use Formula 3.1 as starting point and split up the product \( \prod_{n=1}^{L} \) that takes into account the whole alignment into three products, namely the region left of the motif, the
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motif region, and the region right of the motif. The statistical model of a motif bearing alignment $X_n$ of length $L_n$ consisting of sequences from $O$ species is defined as:

$$p(X_n, \theta) = \sum_{\ell_n=1}^{L_n-W+1} \frac{1}{L_n-W+1} \prod_{o=1}^{O} p(X_n^{i(\ell_n),o}|\ell_n, \theta) \cdot p(X_n^{m(\ell_n),o}|\ell_n, \theta) \cdot p(X_n^{e(\ell_n),o}|\ell_n, \theta)$$

(3.10)

The inner factors are defined as follows:

$$p(X_n^{i(\ell_n),o}|\ell_n, \theta) = \prod_{u \in \{1, \ldots, \ell_n-1\}} \pi^{a,\zeta}_u$$  \hspace{1cm} (left flanking region) \hspace{1cm} (3.11)

$$p(X_n^{m(\ell_n),o}|\ell_n, \theta) = \prod_{u \in \{\ell_n, \ldots, \ell_n+W-1\}} \pi^{a,\zeta}_{u-\ell_n+1}$$  \hspace{1cm} (motif region) \hspace{1cm} (3.12)

$$p(X_n^{e(\ell_n),o}|\ell_n, \theta) = \prod_{u \in \{\ell_n+W, \ldots, L_n\}} \pi^{a,\zeta}_0$$  \hspace{1cm} (right flanking region) \hspace{1cm} (3.13)

where the probability of a base $a$ in the background sequence provided that its predecessors are in joint state $\zeta$ is given by the parameter $\pi^{a,\zeta}_0$ and the probability of a base $a$ in the motif sequence provided that its predecessors are in joint state $\zeta$ is given by the parameter $\pi^{a,\zeta}_{u-\ell_n+1}$. The complete statistical model and all parameters are explained in Methods 2 of the corresponding article.

We study the proposed PFM models on datasets based on ChIP-seq data of 35 TFs. First, we measure the degree of intra-motif dependencies captured by the proposed PFM models by computing the position-wise mutual information (mutual information). We call the resulting vector of mutual information values mutual information profile. For each of the 35 TFs, we compute the mutual information profiles of orders 1 and 2 from the motifs obtained by the PFM models of order 2. Moreover, we study for each TF the similarity of the species-specific motifs using DiffLogo and the similarity of the species-specific mutual information profiles using statistical tests.

Second, we study the classification performance of the PFM models of orders 0, 1, and 2 using 25-fold stratified repeated random sub-sampling validation. We calculate and show for each TF the relative increase of the PFM models of orders 1 and 2 relative to the PFM model of order 0. Moreover, we compare the classification performance of phylogenetic footprinting and one-species approaches when neglecting and taking into account base dependencies of order 2.
Results, discussion, and conclusions

First, we found for the studied TFs statistically significant intra-motif dependencies between neighboring bases at all positions and we found even stronger intra-motif dependencies between dimers and their neighboring bases at all positions. We excluded the possibility that the captured intra-motif dependencies are an artifact resulting from a mixture of different species-specific motifs.

Second, we found that modeling base dependencies of order 1 improves phylogenetic footprinting for 31 TFs and we found that modeling base dependencies of order 2 improves phylogenetic footprinting for all 35 TFs and always outperforms modeling base dependencies of order 1. By comparing the classification performances of the four cases of one-species approaches and phylogenetic footprinting when neglecting and taking into account base dependencies, we found that taking into account both phylogenetic dependencies and base dependencies outperforms the other three approaches in 31 of the 35 TFs.

These findings suggest that combining phylogenetic footprinting with motif models incorporating intra-motif dependencies may lead to an improved prediction of TFBSs and thus advance our understanding of transcriptional gene regulation and its evolution.

3.3 Visualization of sequence motifs

The next two subsections provide a short summary of the publication “DiffLogo: a comparative visualization of sequence motifs” and the work-in-progress article “WebDiffLogo: A web-server for the construction and visualization of multiple motif alignments”.

3.3.1 DiffLogo: A comparative visualization of sequence motifs

An important task in bioinformatics is the visualization of results from the analysis of biological data. In the field of de-novo motif discovery and TFBSs prediction, sequence motifs are used to represent functional regions of biological sequences, e.g., TFBSs, splice sites in pre-mRNAs, miRNA binding sites, or phosphorylation sites of proteins. Sequence logos are the de facto standard for the visualization of these sequence motifs and are essential for researchers to interpret findings, document work, share knowledge, and present results (Schneider et al., 1990).

Due to the increasing number of datasets and due to the increasing number of approaches for de-novo motif discovery, the research focus has shifted from inferring only “the” sequence motif towards comparative analyses to study the reasons for, e.g., the differential binding of TFBS under different conditions. Sequence logos are not suited for the discovery of the,
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sometimes subtle, differences between, e.g., cell type-specific sequence motifs resulting from the differential binding of the TF of interest.

Initial approaches for comparative visualization of sequence motifs can be found in iceLogo (Colaert et al., 2009; Maddelein et al., 2015), MotifStack (Jianhong Ou, 2014), STAMP (Mahony et al., 2007), and Two Sample Logo (Vacic et al., 2006). None of them allows a configurable and comparative visualization of multiple sequence motifs. Table 1 in “DiffLogo: a comparative visualization of sequence motifs” shows an comparative overview of the main features of each tool. The objective of this work is to develop an easy to use and configurable tool for the comparative visualization of multiple sequence motifs.

Methods

Inspired by the intuitive sequence logo approach, we propose the difference logo to present differences between two sequence motifs. A difference logo depicts position-wise differences between two motifs of length L by L symbol stacks. The height of a stack is proportional to the degree of symbol distribution dissimilarity and the height of a symbol is proportional to the degree of differential symbol abundance. In case of N > 2 motifs, we take into account all N × (N − 1) pair-wise motif comparisons and arrange the resulting difference logos in a N × N grid with one row and one column for each motif. Similar motifs are placed in nearby rows and columns.

Since the software environment R already has a large community among researchers from natural sciences, we implement this idea using R and make it publicly available in the R package DiffLogo. By default, DiffLogo uses the Jensen-Shannon divergence to calculate symbol distribution differences depicted by the height of the symbol stack at position ℓ:

\[
H_\ell = \frac{1}{2} \sum_{a \in A} p_{\ell,a} \log_2 \frac{p_{\ell,a}}{m_{\ell,a}} + \frac{1}{2} \sum_{a \in A} q_{\ell,a} \log_2 \frac{q_{\ell,a}}{m_{\ell,a}},
\]

where \( m_{\ell,a} = \frac{p_{\ell,a} + q_{\ell,a}}{2} \).

The height of a symbol in stack \( \ell \) is by default determined by the probability difference normalized by the sum of absolute probability differences at position \( \ell \):

\[
H_{\ell,a} = H_\ell \cdot \begin{cases} \frac{p_{\ell,a} - q_{\ell,a}}{\sum_{a' \in A} |p_{\ell,a'} - q_{\ell,a'}|} & \text{if } p_\ell \neq q_\ell \\ 0 & \text{otherwise.} \end{cases}
\]
3.3 Visualization of sequence motifs

DiffLogo orders sequence motifs using hierarchical clustering and optimal leaf ordering to ensure that similar motifs are close to each other in the $N \times N$ grid of difference logos. The viewer is able to overlook the overall motif differences by the background color of each difference logo and a leaf-ordered cluster tree on top of the grid.

Results, discussion, and conclusions

We developed the R package DiffLogo for the visualization of differences between various types of sequence motifs. We demonstrated the utility of DiffLogo using binding motifs of the human insulator CTCF from different cell types and successfully reproduced findings from literature. In addition, we applied DiffLogo to E-box motifs of three basic helix-loop-helix transcription factors and to the F-Box binding domain from three different species groups revealing noteworthy motif differences.

Using DiffLogo, it is easily possible to compare motifs from different sources. Hence, DiffLogo facilitates decision making, knowledge sharing, and the presentation of results. The DiffLogo package comprises example data, example code, and further documentation and is freely available at Bioconductor[1]. In 2016, DiffLogo was downloaded more than 100 times per month and more than 1000 times in total.

3.3.2 WebDiffLogo: A web-server for the construction and visualization of multiple motif alignments

In the previous work (Nettling, Treutler, Grau, et al., [2015]), we presented DiffLogo, an R package developed for the comparative visualization of sequence motifs. We think that DiffLogo is already easy to use, but we know that not all researches have access to hardware with R and DiffLogo installed and that not all researches have enough technical background or the time to use R and DiffLogo without high effort. Another hindering preliminary is that all input sequence motifs must have the same length and the same orientation in case of TFBSs to get meaningful difference logos. We experienced that this is often hard to accomplish, especially for users that do not have any background in bioinformatics.

The objective of this work is to make DiffLogo usable to researchers that are less experienced with the R programming language and to researchers without any background in bioinformatics. First, we extend DiffLogo by the capability to align sequence motifs. Second, we integrate DiffLogo into the intuitive to use web-server WebDiffLogo accessible via http://difflogo.com.

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Methods

First, the multiple motif alignment is computed by adjusting the relative shifts and relative orientations of the single sequence motifs based on a heuristic algorithm using the UPGMA algorithm and an extension of the sum-of-pairs score from symbols to conditional probability distributions (Sokal, 1958; Wheeler et al., 2007). We adapted the visualization of difference logos indicating unaligned flanking regions with a gray background. Further, all sequence logos and difference logos in a table of difference logos are shown aligned. Thus, a visual inspection of sequence logos and difference logos can be easily accomplished.

Second, we integrated DiffLogo into the web-server [http://difflogo.com](http://difflogo.com). Frontend and backend are fully implemented using the Javascript library ReactJS. The front-end is designed as a single page application that permanently communicates with the web-server to e.g., validate files or generate sequence logos. This gives the user the feeling of a desktop application.

The source code of the web-server is publicly available at [https://github.com/mgledi/DiffLogoUI](https://github.com/mgledi/DiffLogoUI).

Results, discussion, and conclusions

WebDiffLogo allows building difference logos of two sequence motifs and tables of difference logos of more than two sequence motifs via a user friendly single page application. The user starts by uploading the input set of sequence motifs or the input set of sets of aligned sequences in one of several common formats. WebDiffLogo converts collections of aligned sequences to sequence motifs automatically, and the user is then allowed to select sequence motifs for the subsequent comparison. Sequence motifs of different length and different orientation will be automatically aligned. WebDiffLogo finally compares the aligned motifs in a position-wise manner and visualizes the over- and under-represented symbols as difference logos. The visualization is shown in the browser window. The output data are kept for 24 hours and can be downloaded by the user as PNG files as well as publication-ready vector graphics files. The user can also download and adapt the R code that generated the results. Figure 3.4 shows an example difference logo and the sequence logos of two CTCF motifs differing length and strand orientation.

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3.3 Visualization of sequence motifs

Figure 3.4: Difference logo (bottom) and sequence logos of CTCF motifs from cell lines H1-hESC (top left) and HUVEC (top right). The H1-hESC motif is two bases shorter than the HUVEC motif. The two motifs also differ in their strand orientation. The resulting difference logo depicts the small differences of the aligned motifs. Unaligned regions are indicated with gray background.
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3.4 Conclusions and outlook

In this thesis, my colleagues and I have addressed six limitations in three related fields.

First, we proposed *miRGen* and *DRUMS*, two approaches to improve “data acquisition and data preparation.” Specifically, by providing access to over 800 miRNA transcripts enriched with information about TFBSs near their TSS, miRNA expression profiles, and with SNPs, *miRGen* improves the insights into the involvement of miRNAs in gene regulation and thus contributes to cancer diagnostics and therapeutics. Further, *DRUMS* is a key-value store optimized to handle psDrd running on standard desktop hardware. *DRUMS* is considerably faster than *MySQL* by a factor of 2 up to a factor of 15456 regarding this kind of data.

In comparison to many other NoSQL databases, neither is *DRUMS* horizontally scalable nor does it support redundancy. It would be an interesting follow-up project to investigate if the *DRUMS* concept could be extended by those capabilities.

Second, we proposed three approaches to improve “de–novo motif discovery using phylogenetic footprinting.” Specifically, we found that it is possible to detect and correct the BA bias using inter–species information and that taking into account this bias leads to a more precise prediction of TFBSs using *phylogenetic footprinting* on ChIP-seq data. Further, we found that *phylogenetic footprinting* using a star topology with unrealistic high substitution probabilities seem to be more robust toward violation of model assumptions caused by evolutionary effects like heterogeneous and heterotachious substitution probabilities. Finally, we found that combining *phylogenetic footprinting* with motif models incorporating intra–motif dependencies lead to an improved prediction of TFBSs. Each of these findings advance our attempt of understanding transcriptional gene regulation as a whole.

Regarding “De–novo motif discovery using phylogenetic footprinting,” I propose the following future works. It would be interesting to investigate more complex evolutionary models like the HKY model or the GTR model with the *phylogenetic footprinting* approaches proposed in this thesis. Further, it seems promising to combine the *phylogenetic footprinting* approaches proposed in this thesis to one approach that is capable of detecting and correcting the BA bias and to model intra-motif dependencies. Finally, a combination of *phylogenetic footprinting* with more complex motif models like parsimonious Markov models or Bayesian Markov models could improve de–novo motif discovery based on *phylogenetic footprinting* (Eggeling et al., 2015; Siebert et al., 2016).

Third, we proposed *DiffLogo* to improve “visualisation of sequence motifs.” *DiffLogo* is an R package publicly available via Bioconductor or GitHub, developed for the comparative

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visualization of sequence motifs. *DiffLogo* was downloaded more than 100 times per month and more than 1000 times in total in 2016. To make *DiffLogo* applicable to a broader user-ship, we integrated the *R* package into the easy-to-use web-server *WebDiffLogo*[^1]. *DiffLogo* and *WebDiffLogo* facilitate decision making, knowledge sharing, and the presentation of results.

An interesting extension of *DiffLogo* could be the higher order comparative visualization of sequence motifs, i.e., the comparative visualization of intra-motif dependencies. An interesting follow-up of *WebDiffLogo* could be a web-server that allows the investigation of sequence motifs with several existing tools like *IceLogo*, *motifStack*, or *Two Sample Logo* (Colaert et al., 2009; Jianhong Ou, 2014; Vacic et al., 2006). Additionally, the investigation of sequence motifs could be dramatically improved by allowing user interactions with the results, e.g., investigating only a few motif positions of interest.

[^1]: [http://difflogo.com](http://difflogo.com)
3. CONTEXT OF PUBLICATIONS
Glossary

AUC  area under receiver operating characteristics curve.

BA  bias binding affinity bias.

bp  base pair.

ChIP-seq  ChIP-sequencing.

DNA  Deoxyribonucleic acid.

DRUM  Disk Repository with Update Management.

DRUMS  Disk Repository with Update Management and Select option.

EM  Expectation Maximization.

F81  evolutionary model Felsenstein 81.

HERV  human endogenous retrovirus.

hMM(k)  homogeneous Markov model of order \( k \).

iMM(k)  inhomogeneous Markov model of order \( k \).

KLD  Kullback—Leibler divergence.

miRNA  microRNA.

mRNA  messenger RNA.

MSA  multiple sequence alignment.

mutual information  mutual information.

NoSQL  not only SQL.

PFM  phylogenetic footprinting model.

PR  precision recall.

psDrd  position-specific DNA related data.

PWM  position weight matrix.

RISC  RNA-Induced Silencing Complex.

RNA  Ribonucleic acid.

ROC  receiver operating characteristics.

SNP  single nucleotide polymorphism.

SQL  structured query language.

TF  transcription factor.

TFBS  transcription factor binding site.

TSS  transcription start site.

UTR  untranslated region.

ZOOPS  zero or one occurrence of a binding site per sequence.
References


REFERENCES


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REFERENCES


REFERENCES


REFERENCES
4 Data acquisition and data preparation

4.1 miRGen 2.0: a database of microRNA genomic information and regulation

miRGen 2.0: a database of microRNA genomic information and regulation

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1Institute of Molecular Oncology, Biomedical Sciences Research Center ‘Alexander Fleming’, Vari, 2School of Biology, Aristotle University of Thessaloniki, Thessaloniki, 3Institute for the Management of Information Systems, “Athena” Research Center, 4Knowledge and Database Systems Lab, Department of Computer Science, School of Electrical and Computer Engineering, National Technical University of Athens, Athens, Greece, 5Institute of Computer Science, Martin Luther University Halle-Wittenberg, Halle, Germany, 6Institute for Genome Sciences and Policy, Duke University, Durham, NC and 7Computer and Information Sciences, University of Pennsylvania, Philadelphia, PA, USA

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ABSTRACT

MicroRNAs are small, non-protein coding RNA molecules known to regulate the expression of genes by binding to the 3’UTR region of mRNAs. MicroRNAs are produced from longer transcripts which can code for more than one mature miRNAs. miRGen 2.0 is a database that aims to provide comprehensive information about the position of human and mouse microRNA coding transcripts and their regulation by transcription factors, including a unique compilation of both predicted and experimentally supported data. Expression profiles of microRNAs in several tissues and cell lines, single nucleotide polymorphism locations, microRNA target prediction on protein coding genes and mapping of miRNA targets of co-regulated miRNAs on biological pathways are also integrated into the database and user interface. The miRGen database will be continuously maintained and freely available at http://www.microrna.gr/mirgen/.

INTRODUCTION

MicroRNAs (miRNAs) are single-stranded non-coding RNA molecules of ~21 nucleotides in length, that function as regulators of gene expression by binding to messenger RNA (mRNA) molecules and destabilizing them or inhibiting their translation. They are found to be implicated in a wide range of physiological molecular processes, and their deregulation leads to diverse diseases (1–3).

MiRNAs are located in intergenic regions or in the introns of protein coding genes. They are transcribed by RNA Polymerase II as independent transcripts or as part of the transcript of a host gene. Only a small group of miRNAs located inside ALU repetitive elements is transcribed by RNA Polymerase III. A miRNA primary transcript (pri-miRNA) is processed in the nucleus to form pre-miRNAs, ~70-nucleotide stem–loop structures also called miRNA hairpins. These are later processed into mature miRNAs in the cytoplasm via interaction with the endonuclease Dicer, which also initiates the formation of the RNA-induced silencing complex (RISC). Since primary transcripts are short lived and present only inside the nucleus, it is hard to identify them with standard molecular techniques.

After the Dicer enzyme cleaves the pre-miRNA stem–loop, two complementary short RNA molecules are formed, but only one of them—the guiding strand—is predominantly integrated into the RISC complex.
The remaining strand, known as the \(\text{miRNA}^*\), anti-guide or passenger strand, is usually degraded. However, the proportion of the integration of each strand varies with the miRNA species, with some miRNAs having almost equal abundance of each of the two strands incorporated into RISC. Another common nomenclature for complementary miRNA strands is the –3p and –5p naming convention—these names do not imply which miRNA is more commonly incorporated to the RISC complex. The miRNA–miRNA* and miRNA-3p–miRNA-5p nomenclatures are both widely used in the community, often to denote the same complementary miRNA pair.

Mature miRNA molecules are bound by the RISC complex, are guided to specific motifs within the 3\(^\text{\prime}\) UTR of protein coding mRNAs, and prevent these mRNAs from being translated into protein. The biogenesis of miRNAs and their regulation by TFs is diagrammed in Figure 1.

In the previous version of the miRGen database (6), co-expressed miRNA clusters were identified based on their distance and genomic features surrounding them. With the availability of experimental data we were able, in miRGen 2.0, to mine prominent literature sources that identify miRNA primary transcripts in mammals (human and mouse genomes). Moreover, we have mapped TF binding sites (TFBSs) within the regions upstream of these miRNA primary transcript TSSs and incorporated expression profiles of miRNAs in several tissues, the mapping of SNPs within genomic locations of miRNA hairpins and the mapping of SNPs within the TFBSs found upstream of miRNA genes. The interplay of these different information sources concerning genomic features associated with miRNA genes and their expression levels can be used to study the function of miRNAs and their deregulation in disease. For instance, a user interested in a specific TF can find miRNA genes associated with this TF, find the expression levels of these miRNAs in a possible tissue of interest, possibly find some SNPs on the TFBSs or the miRNA locations on the genome that relate to a possible disease of interest and finally find predicted targets of the miRNAs associated with the TF of interest, and molecular pathways in which the targets of each of these miRNAs separately or together are implicated.
DATA GENERATION

miRNA coding transcripts

MiRNA transcripts in human and mouse were identified from four literature sources:

(i) Corcoran et al. (7) used PolII immunoprecipitation data and ChIP-chip on lung epithelial cells to identify miRNA transcripts and their promoter regions.

(ii) Landgraf et al. (8) sequenced 250 small RNA libraries corresponding to 26 different organ systems and cell types of human and mouse, with ~1000 miRNA clones per library and identified miRNA coding genes. In this study, the whole transcripts of miRNA coding genes were identified, as well as protein coding genes that contain miRNAs.

(iii) Ozsolak et al. (9) predicted the location of the proximal promoters of human miRNAs by combining nucleosome mapping with promoter chromatin signatures in MALME, HeLa and UACC62 cells. Although the TSS of miRNA genes was identified in this study, the end of the transcript was not provided. We have provided end of the last miRNA that is a member of a gene as an approximation of the transcript end.

(iv) Marson et al. (10) used ChIP-seq data to identify promoters of miRNA genes in embryonic stem cells. They identified promoters and co-regulated miRNAs, but the exact position of the TSS was not identified. For this reason we have used the start of the first miRNA of each cluster as the putative TSS. Additionally, coordinates provided by Marson et al. had to be lifted over using ‘UCSC lift over tool’ to the current genome build (hg18, mm9). In cases where putative rather than experimentally verified positions are used, they are denoted in the graphical interface as ‘computational TSS’.

In total, 812 human miRNA coding transcripts and 386 mouse miRNA coding transcripts were identified. Of them, 423 were shown in the corresponding papers to be associated with protein coding genes (intragenic miRNA transcripts). More than one of the above publications are located within the coordinates of clusters given by any of these publications, this miRNA is added to the cluster. For names that changed or were given differently than the current standard, manual curation with reference to miRBase (11) was used to identify and replace these names according to the current standard. For all the above reasons it is possible that the number of genes used in miRGen (Table 1) does not correspond perfectly to the number stated in the corresponding publications.

<table>
<thead>
<tr>
<th>References</th>
<th>Human Genes</th>
<th>Human miRNA</th>
<th>Mouse Genes</th>
<th>Mouse miRNA</th>
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</thead>
<tbody>
<tr>
<td>Corcoran et al. (7)</td>
<td>73</td>
<td>148</td>
<td></td>
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</tr>
<tr>
<td>Landgraf et al. (8)</td>
<td>201</td>
<td>347</td>
<td>191</td>
<td>590</td>
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<tr>
<td>Ozsolak et al. (9)</td>
<td>191</td>
<td>268</td>
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<tr>
<td>Marson et al. (10)</td>
<td>346</td>
<td>507</td>
<td>195</td>
<td>422</td>
</tr>
</tbody>
</table>

TFBS identification

In order to determine putative TFBSs near the TSS of miRNA primary transcripts, we used the freely available tool MatchTM (12). MatchTM uses the public library of position weight matrices from Transfac 6.0—cite: TRANSFAC: an integrated system for gene expression regulation. We matched all vertebrate TF matrices to the regions spanning from 5 kb upstream of each TSS to 1 kb downstream of the TSS. As criterion for determining the cut-off values we chose the minimization of false positives in order to produce a strict set of predictions without too many falsely predicted TFBSs. Two scores are calculated for each putative TFBS. The matrix similarity score describes the quality of the match between a whole matrix and an arbitrary part of the input sequences. Analogously, the core similarity score denotes the quality of the match between the core sequence of a matrix (i.e. the five most conserved positions within a matrix) and a part of the input sequence.

miRNA expression profiles

miRNA expression profiles were identified from the mammalian miRNA expression atlas (8). Information for the expression profiles of 548 human and 451 mouse miRNAs over 172 human and 68 mouse small RNA libraries were derived from cell lines and tissues.

SNPs

SNPs located within the genomic positions of miRNA hairpins and corresponding TFBSs were downloaded from the UCSC table browser (13). For human, Polymorphism data from dbSnip database (14) or genotyping arrays SNP130 were used with 18833531 identified SNPs. For mouse, SNP128 was used with 14893502 identified SNPs.

Implementations

The miRGen repository has been implemented using relational database technology. All data are stored in a MySQL relational database management system. Figure 2 illustrates part of the entity-relationship model of our application. All results are available through a user-friendly interface that allows searches for miRNAs and for TFs of interest. For mature miRNAs, it is possible to view targets predicted by the program microT-ANN and for miRNAs found in the same transcript, the user can see a functional annotation of their targets on molecular

References Human
Genes
Human
miRNA
Mouse
Genes
Mouse
miRNA
Corcoran et al. (7) 73 148
Landgraf et al. (8) 201 347 191 590
Ozsolak et al. (9) 191 268
Marson et al. (10) 346 507 195 422

DISCUSSION
This version of miRGen is the first attempt to build a widely accessible and user-friendly database that connects TFs and miRNAs through putative and experimentally supported functional relationships. The connections identified in the database will further our understanding of the TF-mediated regulation of miRNA genes, and pave the way for the mapping of the interplay between TFs and miRNAs as regulatory molecules. The identification of SNPs on miRNA locations and their corresponding TFBSs, as well as the expression profiles of miRNAs can improve our insight into the involvement of miRNAs in developmental processes and disease.

Deregulation of TF-mediated gene expression has been shown to extensively affect protein coding genes, and lead to disease (17,18). MiRNA expression levels have also been shown to change significantly in different disease states (19,20). The availability of both these resources in the same database will allow researchers to identify regulatory elements, such as TFs that may affect the expression of miRNAs. For this reason, we believe miRGen 2.0 will be an important resource for researchers of diverse disciplines interested in miRNA regulation and function.

AVAILABILITY
The miRGen database will be continuously maintained and freely available at http://www.microrna.gr/mirgen/.
4. DATA ACQUISITION AND DATA PREPARATION

REFERENCES

4.2 DRUMS: Disk Repository with Update Management and Select option for high throughput sequencing data

DRUMS: Disk Repository with Update Management and Select option for high throughput sequencing data

Martin Nettling1,2, Nils Thieme2, Andreas Both*2 and Ivo Grosse1,3

Abstract

Background: New technologies for analyzing biological samples, like next generation sequencing, are producing a growing amount of data together with quality scores. Moreover, software tools (e.g., for mapping sequence reads), calculating transcription factor binding probabilities, estimating epigenetic modification enriched regions or determining single nucleotide polymorphism increase this amount of position-specific DNA-related data even further. Hence, requesting data becomes challenging and expensive and is often implemented using specialised hardware. In addition, picking specific data as fast as possible becomes increasingly important in many fields of science. The general problem of handling big data sets was addressed by developing specialized databases like HBase, HyperTable or Cassandra. However, these database solutions require also specialized or distributed hardware leading to expensive investments. To the best of our knowledge, there is no database capable of (i) storing billions of position-specific DNA-related records, (ii) performing fast and resource saving requests, and (iii) running on a single standard computer hardware.

Results: Here, we present DRUMS (Disk Repository with Update Management and Select option), satisfying demands (i)-(iii). It tackles the weaknesses of traditional databases while handling position-specific DNA-related data in an efficient manner. DRUMS is capable of storing up to billions of records. Moreover, it focuses on optimizing relating single lookups as range request, which are needed permanently for computations in bioinformatics. To validate the power of DRUMS, we compare it to the widely used MySQL database. The test setting considers two biological data sets. We use standard desktop hardware as test environment.

Conclusions: DRUMS outperforms MySQL in writing and reading records by a factor of two up to a factor of 10000. Furthermore, it can work with significantly larger data sets. Our work focuses on mid-sized data sets up to several billion records without requiring cluster technology. Storing position-specific data is a general problem and the concept we present here is a generalized approach. Hence, it can be easily applied to other fields of bioinformatics.

Keywords: Database, HERV, SNP, DNA related data, High throughput data

Background

With the beginning of the information age in the 90s of the last century, a large set of processes are established to manipulate and analyze data. In particular in the field of bioinformatics, many different workflows produce a growing amount of data. One example are sequencing technologies, which are capable of sequencing an entire human genome in less than a day. Moreover, extensive software suites for analyzing biological data sets exist, e.g. http://galaxy.psu.edu/ [1-3]. In addition, it is possible that an analyzing process produces more output data than provided input. For example, the input size of the HERV data set used in this work is about 4 GB. The output of the mapping with BLAST is about 50 GB large. Hence, rapid processes for storing and querying data are needed as it has impact on the general performance of the analytic processes.
Position-specific DNA related data (psDrd)

In the field of bioinformatics, data related to DNA sequences are of particular importance. Examples are single nucleotide polymorphisms (SNPs) [4], transcription factor binding affinities and probabilities [5,6], and RNAseq data [7,8]. We generalize these types of data by the term position-specific DNA-related data (psDrd). A psDrd record is an information related to a specific DNA position. psDrd records have three characteristics. First, a psDrd record \( R \) can be represented by a key-value pair \( R = (K, V) \). The key \( K \) is composed of the sequence identifier and the position of the associated value \( V \). Hence, the key is unique, and records can be easily sorted. Second, psDrd records are usually requested by region (e.g., querying for all mutations in a specific gene or looking for transcription factors that are binding near a given position). We call this kind of access range select. Third, all psDrd of the same kind need the same space to be stored on device, i.e., two different records are represented by the same number of bytes. In contrast, textual annotations are generally of variable length. These three specific properties can be utilized for optimizing data handling of psDrd.

Time- and resource-intensive computations on psDrd

Many biological processes and bioinformatics algorithms have psDrd as input or output. This type of data is essential for understanding biological and biochemical processes. Furthermore, diagnostics in medicine for cancer prediction and genetic diseases are using psDrd [9–11].

Many activities in bioinformatics focus on analyzing psDrd. However, often file and folder strategy or a standard databases like MySQL [12] are used for data management. These approaches are straightforward but not optimized for the intended processing of psDrd. In addition, data types used in these tools are expensive and time consuming, data types used in these tools are expensive and time consuming. Hence, we extend the DRUM concept by allowing the selection of records by key (single lookup) or by range (range selects). Within this concept we decoupled I/O-processes from memory processes to avoid blocking single components. Following the three psDrd data properties, the following architecture decisions were made for DRUMS in addition to the DRUM concept: 1) All records are equally sized, so that jumping to the start position of an arbitrary record in the file is possible. Therefore, a sparse index [15] can be applied efficiently, making rapid single selects possible by the following two steps: The sparse index points to a block of records, where the psDrd of interest might be found. To finally find the requested record, a binary search is performed. The binary search massively benefits from equally sized records. 2) Records, which are close to each other on DNA are stored close on disk according to their keys. This enables efficient range selects. 3) Records are organized in

4.2 DRUMS: Disk Repository with Update Management and Select option
4. DATA ACQUISITION AND DATA PREPARATION

Architecture of DRUMS

DRUMS is composed of the interacting components described in this section. Before each component is described in detail, we give a high-level overview of the insert and select process of DRUMS.

Processes

Insert process The high-level overview of the insert process of DRUMS is shown in Figure 1. KV pairs are sent to DRUMS. As in DRUM, the incoming records are already distributed in memory between RAM buffers B (called memory buckets). Each bucket Bᵢ in memory has a corresponding bucket Dᵢ on disk. The sizes of the buckets are dynamic. If a bucket Bᵢ exceeds a predefined size or memory limitations are reached, a synchronisation process, consisting of four phases, is started:

1) The bucket Bᵢ is taken and replaced by an empty one. Hence, incoming data can still be buffered. 2) The KV pairs of Bᵢ are sorted by their keys. 3) Bᵢ and Dᵢ are synchronised using mergesort. Already existing records can be updated using state-dependent operations. 4) The merged data is continuously written back to bucket Dᵢ. Hence, input data is now saved persistently on the disk.

Note: Step 3 and 4 of the synchronisation process are performed chunk-wise, so that optimal read and write performance can be achieved. The optimal chunk-size depends on the used hardware, the size of a single record, the expected data volume, and several parameters in DRUMS. Therefore, it has to be determined empirically.

Range select process Figure 2 shows the high-level overview of the select process. When a request is sent to DRUMS, four steps are performed to read the requested records given by the keys Kₛ and Kₑ (start and end of the range). 1) The requested bucket Dᵢ is identified by \( M(K) \rightarrow Dᵢ \). 2) The index of Dᵢ is used for determining the correct chunk Cᵢ of the first requested record \( Rₛ = \left( Kₛ, Vₛ \right) \). 3) Within Cᵢ a binary search is performed for finding \( Rₛ \). The binary search massively benefits from equally sized records. 4) A sequential read is performed until \( Rₑ \) was found and consequently \( Rₛ \) returned. It might be needed to perform the sequential read over chunk and bucket boundaries.

Single select process A request of a single row (single select) is considered as special case of the range select process where \( Kₛ = Kₑ \). Therefore, it is covered by step 1 to 3.

Components of DRUMS

BucketContainer and its buckets

The BucketContainer is a buffer that is organized in buckets B (memory buckets). It manages the distribution of incoming records to the buckets in RAM. As in DRUM, the distribution of the incoming records \( R = \left( K, V \right) \) to the buckets B is based on a predefined mapping function \( M(K) \rightarrow Bᵢ \).

The BucketContainer is decoupled from any I/O-operation, so that preparing the data for writing can be done in parallel to the I/O-processes. The larger the size of the BucketContainer, the larger are the parts of the data...
that can be processed sequentially. This increases the performance significantly as sequential I/O-operations are the most efficient on HDDs and SSDs.

**SyncManager, SyncProcess, and Synchronizer**

The SyncManager manages all SyncProcesses. It observes the BucketContainer and verifies the preconditions for the synchronisation of buckets $B$ with their counterparts on disk $D$. If these preconditions are fulfilled, the SyncManager instantiates new SyncProcesses. Several SyncProcesses can be run in parallel. In our implementation, a bucket in memory must reach a predefined fill level or age to be synchronized.

A new SyncProcess is always instantiated with the largest bucket in the BucketContainer fulfilling the above mentioned condition. When a new SyncProcess is started, the affected bucket in the BucketContainer is replaced by an empty one. In this way the synchronization process is not blocking further insert operations for this bucket.

The SyncProcess instantiates new Synchronizers. A Synchronizer is in charge of writing data from the bucket $B_i$ in memory to the bucket $D_i$ on disk. All records are sorted in $B_i$ and in $D_i$. Hence, the Synchronizer is capable of using mergesort for synchronizing the records in memory with those on disk.

**Representation and structure of the data**

Each persistent bucket is represented by a file on a hard disk. The file is structured into two parts (see Figure 3): (i) the header with meta information and the index structure referencing chunks of a predefined size and (ii) the rest of the file used for the records to store, which are organized in chunks. A sparse index [15] is applied as it is memory efficient and takes advantage of the order of $psDrd$s.

Whenever a bucket $D$ is opened for reading or writing, the header and the index are read into memory. In this way, a rapid access to the required chunks is possible.

The internal representation of a record in a chunk is a sequence of bytes. This sequence is composed of a key-part and a value-part. Each part may consist of several subparts, each of its own data-type (e.g., integer, long, char or even high level data structures like objects). Because of the fact that each record is of equal size, data structures and memory can be easily reused by application of the adaptor and the prototype pattern [16].

**Implementation of DRUMS**

DRUMS is build upon Oracle Java 1.6. Therefore, it is platform independent. We developed DRUMS in an atomic thread-based way. All components work asynchronously and are exchangeable. This allows fast adaptations on single subprocesses or exchanging whole components like the Synchronizer.

**Results and discussion**

In this section we first give a short introduction into two different $psDrd$ sets used for evaluation. Second, we present the results and the evaluation approach considering (i) inserts, (ii) random lookups, and (iii) random range selects.

To prove the superiority of DRUMS in comparison with standard solutions within a desktop environment, we compare it to MySQL which is used widely in the bioinformatics community.

Two different $psDrd$ sets are evaluated. The data sets are described below. DRUMS as well as MySQL were tested comparatively using the three measures: (i) - (iii). For all tests a standard desktop computer was used. MySQL as well as DRUMS are limited to use only 2 GB of the available memory. Details can be obtained from Table 1.

**Data sets**

**SNP-Data from the 1001 genomes project**

The 1001 Genomes Project [17,18] has the goal to understand the resulting of small mutations in different accessions of the reference plant Arabidopsis thaliana.
4. DATA ACQUISITION AND DATA PREPARATION

Table 1 Test system

<table>
<thead>
<tr>
<th>Processor</th>
<th>Intel Xeon E3122S (4 native cores, no hyperthreading)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Memory</td>
<td>8 GB</td>
</tr>
<tr>
<td>Operation system</td>
<td>Debian 6.0 (Squeeze)</td>
</tr>
<tr>
<td>Hard drive</td>
<td>Western digital WD10EALX-759, 32 MB cache</td>
</tr>
</tbody>
</table>

The desktop system which was used for the tests. MySQL as well as DRUMS are limited to use only 2 GB of the available memory.

Each accession mainly consists of five attributes: accession identifier, sequence identifier, position on sequence, source base, and target base. We downloaded filtered quality data of the strains sequenced by the Gregor Mendel Institute and the Salk institute on 2012-01-15, containing 251 data sets, with 137, 369, 902 SNPs. From all files, we extracted the data of the following five columns: accession name, chromosome, position on chromosome, reference nucleotide, and mutated nucleotide. For the definitions of the used data types and their configuration (e.g., index properties) used in MySQL and DRUMS see Table 2.

All data are public available at http://1001genomes.org/datacenter/.

HERV data

Human endogenous retroviruses (HERVs) have integrated themselves in the human genome millions of years ago. Because of the high number of existing HERV fragments, they are thought to have a regulatory role. To investigate a possible influence of HERVs, it is needed to locate HERV fragments. Therefore, over 7000 known HERV fragments were blasted against the human genome to find new putative HERV-like regions. In the work of Konstantin Kruse [19] all regions with an E-value less than 1 were accepted as putative HERV-like regions. In the work of Konstantin Kruse [19] all regions with an E-value less than 1e − 20 were accepted as putative HERV-like region. This lead to 802, 710, 938 single records, stored in 20 files with tab-separated data field, with a total size of 50 GB. From these files we used the following seven columns: query id, subject id, query start, query end, target start, target end, and E-value. For the definitions of the used data types and their configuration (e.g., index properties) used in MySQL and DRUMS see Table 2.

All data are public available at http://1001genomes.org/datacenter/.

Table 2 Data types used for SNP data

<table>
<thead>
<tr>
<th>Column</th>
<th>MySQL properties</th>
<th>DRUMS properties</th>
</tr>
</thead>
<tbody>
<tr>
<td>Accession name</td>
<td>TINY INT, primary key</td>
<td>1 byte, key part 1</td>
</tr>
<tr>
<td>Chromosome</td>
<td>SMALL INT, primary key</td>
<td>2 byte, key part 2</td>
</tr>
<tr>
<td>Position on chromosome</td>
<td>INT, primary key</td>
<td>4 byte, key part 3</td>
</tr>
<tr>
<td>Reference nucleotide</td>
<td>VARCHAR</td>
<td>1 byte, value part 1</td>
</tr>
<tr>
<td>Mutated nucleotide</td>
<td>VARCHAR</td>
<td>1 byte, value part 2</td>
</tr>
</tbody>
</table>

Used data types in MySQL and DRUMS for SNP data. All columns being part of the primary key are indexed.

Insert performance

DRUMS must be able to store hundreds of millions of records. Because of this, it is needed to evaluate the insert performance.

To estimate the insert performance, we measure the time for inserting 10^6 records. We obtain 140 time measurements points in case of SNP-Data and 800 for HERV data. Figures 4a and 4b show the insert performance of DRUMS (blue) and MySQL (green). Despite using bulk requests for inserting the data, it was impossible to insert all 800 million HERV records into the MySQL instance. MySQL inserts about 200 million records in the first week, but Figure 4b shows that the insert performance has dropped to 300 records per second after one week. The insert performance of DRUMS also decreases, but it was able to insert the whole data set within 4.53 hours. At the end of the test, DRUMS was still able to perform more than 20000 inserts per second.

Figure 4a and 4b show that DRUMS has a better insert performance than MySQL on both test datasets. The insert performance of MySQL and of DRUMS decreases with the number of records already inserted. Regarding MySQL one possible explanation is the continuous reorganisation and rewriting of the index.

The insert performance of DRUMS decreases slowly in comparison to MySQL. The reason for this is the decreasing ratio of read- to write-accesses with each round of synchronisation. With other words, DRUMS must read more and more records to write with the growing amount of data already stored on disk. However, DRUMS still inserts more than 20000 records per second at the end of the insert test for HERV data, corresponding to approximately 400 kB per second.

Performance on random lookups

From the view of bioinformatics, single lookups make no sense in both experiments. However, the performance of single-lookups is a significant indicator for the overall performance and the suitability of the implementation of a tool for handling data sets. Moreover, the test may show how close the measured performance to the theoretical hardware limits of the used standard desktop hardware is. Considering the test environment, it is assumed that a random access would take approximately 20 ms. Hence, if no other disk accesses are done, it would be theoretically possible to read 50 records per second.

Figures 5a and 5b show the performance of MySQL and DRUMS, when performing random lookups. Again, DRUMS performs better than MySQL in case of handling our two data sets. Figure 5a implies that DRUMS is able to do 160 times more random lookups than theoretically possible, when accessing SNP data. In comparison,
Table 3 Data types used for HERV data

<table>
<thead>
<tr>
<th>Column</th>
<th>MySQL properties</th>
<th>DRUMS properties</th>
</tr>
</thead>
<tbody>
<tr>
<td>Chromosome</td>
<td>TINY INT, primary key</td>
<td>1 byte, key part 1</td>
</tr>
<tr>
<td>Start-position on chromosome</td>
<td>INT, primary key</td>
<td>4 byte, key part 2</td>
</tr>
<tr>
<td>End-position on chromosome</td>
<td>INT, primary key</td>
<td>4 byte, key part 3</td>
</tr>
<tr>
<td>Start-position on HERV</td>
<td>SMALL INT, primary key</td>
<td>2 byte, key part 4</td>
</tr>
<tr>
<td>End-position on HERV</td>
<td>SMALL INT, primary key</td>
<td>2 byte, key part 5</td>
</tr>
<tr>
<td>Id of referenced HERV</td>
<td>SMALL INT, primary key</td>
<td>2 byte, key part 6</td>
</tr>
<tr>
<td>Strand on chromosome</td>
<td>TINY INT, primary key</td>
<td>1 byte, key part 7</td>
</tr>
<tr>
<td>E-value</td>
<td>DOUBLE</td>
<td>4 byte, value part 1</td>
</tr>
</tbody>
</table>

Used data types in MySQL and DRUMS for HERV data. All columns being part of the primary key are indexed.

only 20 random lookups per second are performed when accessing HERV data. The reason for this difference are cache structures provided by the operating system and the underlying hardware.

In case of accessing SNP data, the complete data set might be cached by the operating system after approximately 650,000 lookups. Hence, organizing the SNP data as DRUMS structure results in a file size small enough that it could be loaded into memory. Therefore, nearly each request could be answered from the operating systems cache after a warm up. In contrast, the HERV data set is too large to fit into memory, so only a few random lookups could be answered from cache. The increasing performance of MySQL and DRUMS in Figure 5b is also an indication for the use of caches. Figure 5b shows that DRUMS can perform 20 random lookups of theoretically possible 50.

While considering the experimental results of MySQL, the impression is conveyed that the defined index was not used correctly. However, a closer look validates the results as the explicit MySQL index for the SNP table has the size of 2380 MB, which will not fit into the allowed 2 GB of main memory. Hence, even index-based searches in MySQL need several accesses to the hard disk resulting in worse performance. In contrast, the sparse index of each bucket of DRUMS requires just 0.5 MB, which sums

![Figure 4](https://via.placeholder.com/150)

**Figure 4 Insert performance.** The blue line represents DRUMS, the green line represents MySQL. (a) Insert performance on SNP-data (b) Insert performance on HERV data. Concerning MySQL, it was impossible to insert all 800 million HERV records. DRUMS inserted the complete data set within 4.53 hours.
4. DATA ACQUISITION AND DATA PREPARATION

up to only 123 MB for all buckets. To find a single record in a chunk, DRUMS performs a binary search. The binary search can be done very efficiently for the reason that all records are of equal size. Because of the reduced demands on the hardware, DRUMS provides a good performance even on very large data sets like HERV.

Performance on random range selects
As described in the section Background, psDrd-records are mostly requested by range. Therefore, the need to benchmark the performance of range requests is obvious. The request for the SNP-data is as follows: Select all SNPs on chromosome c between position x and y for

(a) single-select performance (SNP)
(b) single-select performance (HERV)

(a) range-select performance (SNP)
(b) range-select performance (HERV)
all ecotypes in the database. To perform the read test for SNP-data, we first randomly generated 10^6 ranges of length 10^5 to 10^9. Second, we request records within those ranges randomly distributed over the whole genome of Arabidopsis thaliana.

Analogously, we generate 10^6 test requests for the HERV data set with lengths from 10^5 to 10^9. Again, we randomly distributed range-requests over the whole human genome. It might be a common task to filter the requested data by value. MySQL provides this functionality by defining the filter condition in the WHERE-clause. To accomplish this in DRUMS, the returned records must be checked iteratively. In this test, we filter the requested HERV records by an E-value less than 10^{-20}, 10^{-25}, 10^{-30}, 10^{-35}, 10^{-40}, 10^{-45} or 10^{-50}, randomly chosen.

Figures 6a and 6b show the results of the range select test. Once more, both databases perform much better on the smaller SNP-data set. Besides caching, this time another explanation for this observation is that a range request on the SNP-data contains in average 3 times fewer records than a range request on the HERV data. The performance increases with the number of read records. The performance of DRUMS increases by a factor of 10 and of MySQL by a factor of 26. However, DRUMS performs in average on the SNP-data 24 times faster than MySQL.

Regarding the larger HERV data set, DRUMS is able to perform 30 range-selects per second in average. This is over 15000 times faster than MySQL.

Within the whole test, 64 billion records were read in 9.61 hours. That corresponds to an overall read performance of 35.7 MB per second, filtering included. In contrast, MySQL read 6.6 million records in 26.35 hours, that corresponds to only 1.3 kB per second.

Conclusions
We defined psDrd (position-specific DNA related data) and showed three important properties of this kind of data. The flaws of DRUM were shown, which is already suitable for storing psDrd, but not for requesting it efficiently. The article introduces DRUMS, a data management concept optimized to tackle the challenges of dealing with mid-size data sets in form of psDrd using standard desktop technology instead of expensive cluster hardware.

An implementation of the DRUMS concept was compared to the widely spread standard database management solution MySQL considering two data sets of the bioinformatics context. On the larger HERV data set, the evaluated DRUMS implementation was 23 times faster inserting all records, two times faster performing random lookups, and 15456 faster performing range requests. Hence, the experiments show that dealing with psDrd benefits significantly from the characteristics of the DRUMS concept. Therefore, our main contribution is suggesting this data management concept for increasing the performance during data intensive processes while keeping the hardware investments low.

Availability and requirements
Project name: DRUMS
Project home page: http://mgledi.github.io/DRUMS
Project home page of examples: http://github.com/mgledi/BioDRUMS
Operating system: Platform independent
Programming language: Java
Other requirements: none
License: GNU GPL v2
Any restrictions to use by non-academics: No specific restrictions.

Competing interests
The authors declare that they have no competing interests.

Authors’ contributions
MN and NT developed and tested the Java code. All of the authors contributed to the design of the software architecture. All of the authors read and approved the final version of the manuscript.

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5 Predicting transcription factor binding sites using Phylogenetic Footprinting

5.1 Detecting and correcting the binding-affinity bias in ChIP-Seq data using inter-species information

Detecting and correcting the binding-affinity bias in ChIP-seq data using inter-species information

Martin Nettling1*, Hendrik Treutler2, Jesus Cerquides3 and Ivo Grosse1,4

Abstract

Background: Transcriptional gene regulation is a fundamental process in nature, and the experimental and computational investigation of DNA binding motifs and their binding sites is a prerequisite for elucidating this process. ChIP-seq has become the major technology to uncover genomic regions containing those binding sites, but motifs predicted by traditional computational approaches using these data are distorted by a ubiquitous binding-affinity bias. Here, we present an approach for detecting and correcting this bias using inter-species information.

Results: We find that the binding-affinity bias caused by the ChIP-seq experiment in the reference species is stronger than the indirect binding-affinity bias in orthologous regions from phylogenetically related species. We use this difference to develop a phylogenetic footprinting model that is capable of detecting and correcting the binding-affinity bias. We find that this model improves motif prediction and that the corrected motifs are typically softer than those predicted by traditional approaches.

Conclusions: These findings indicate that motifs published in databases and in the literature are artificially sharpened compared to the native motifs. These findings also indicate that our current understanding of transcriptional gene regulation might be blurred, but that it is possible to advance this understanding by taking into account inter-species information available today and even more in the future.

Keywords: Binding-affinity bias, ChIP-seq, Phylogenetic footprinting, Evolution, Transcription factor binding sites, Gene regulation
We then develop a phylogenetic footprinting model that focuses on orthologous regions of monkey, dog, cow, and horse. Target regions of five ChIP-seq data sets of human and related species is measurable beyond statistical noise in motifs of the reference species than in phylogenetically related species. This stronger binding-affinity bias yields more biased motifs in the reference species than in phylogenetically related species. This stronger binding-affinity bias increases classification performance, we investigate if a correction of the binding-affinity bias leads to an improvement or a deterioration of the classification performance. In subsection “Modeling the binding-affinity bias increases classification performance”, we describe the basic idea of how the binding-affinity bias could be detected based on inter-species information using a toy example. In the remaining subsections we perform three studies based on ChIP-seq data sets of five transcription factors and on multiple alignments of the human ChIP-seq target regions with orthologous regions from monkey, dog, cow, and horse.

In subsection “Decrease of information contents in motifs due to the contamination bias” we describe the basic idea of how the binding-affinity bias could be detected based on inter-species information. In subsection “Using sequence-information of phylogenetically related species to detect the binding-affinity bias” we compare the sequence motifs predicted with and without the correction of the binding-affinity bias.

5.1 Detecting and correcting the binding-affinity bias in ChIP-Seq data using inter-species information

Results and discussion

In subsection “Using sequence-information of phylogenetically related species to detect the binding-affinity bias”, we describe the basic idea of how the binding-affinity bias could be detected based on inter-species information using a toy example. In the remaining subsections we perform three studies based on ChIP-seq data sets of five transcription factors and on multiple alignments of the human ChIP-seq target regions with orthologous regions from monkey, dog, cow, and horse.

In subsection “Decrease of information contents in motifs due to the contamination bias” we describe the basic idea of how the binding-affinity bias could be detected based on inter-species information. In subsection “Using sequence-information of phylogenetically related species to detect the binding-affinity bias” we compare the sequence motifs predicted with and without the correction of the binding-affinity bias.

Using sequence-information of phylogenetically related species to detect the binding-affinity bias

Detecting and correcting the binding-affinity bias might be possible because the binding-affinity bias inherent to the ChIP-seq experiment in the reference species (Fig. 1a) is stronger than the indirect binding-affinity bias in orthologous regions from phylogenetically related species. Under this assumption, the information content of the predicted motifs [23] should decrease with the phylogenetic distance from the reference species due to the increasing number of mutations.

To illustrate this idea, we present a toy example consisting of six binding sites from four phylogenetically related species in Fig. 1b and Table 1. In this toy example, we assume an exaggerated binding-affinity bias of three high-affinity binding sites captured by the ChIP-seq experiment and three low-affinity binding sites not captured by the ChIP-seq experiment. In real world applications the native motif is unknown and the motif predicted on the available data is biased to an unknown degree. In the presented toy example, however, the native motif is considered to be known so that the effect of the binding-affinity bias on the motifs of the reference species (species 1) and the phylogenetically related species (species 2, 3, and 4) can be illustrated.
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Table 1 Influence of binding-affinity bias on information content. We illustrate the effect of binding-affinity bias with the given toy example of a ChIP-seq experiment for six binding sites in four species. Due to low binding-affinity, red binding sites are insufficiently bound. This results in the absence of red binding sites in the measured data which we denote binding-affinity bias. Binding sites with low binding-affinity typically comprise dissimilar bases in contrast to black binding sites with high affinity and common bases. The absence of red binding sites leads to a sharpening of the resulting motif, which we indicate using the information content. The information content without binding-affinity bias is equal in all species, whereas the information content with binding-affinity bias increases in all species. The vital point is that the effect of binding-affinity bias decreases with phylogenetic distance, which involves an increasing number of mutations. Please find a visualization of this toy example in Fig. 1b.

<table>
<thead>
<tr>
<th>Binding site</th>
<th>Species 1</th>
<th>Species 2</th>
<th>Species 3</th>
<th>Species 4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Binding site 6</td>
<td>A A T T A A T T A A T T A A T T A A T T</td>
<td>A A T T A A T T A A T T A A T T</td>
<td>A A T T A A T T A A T T A A T T</td>
<td>A A T T A A T T A A T T A A T T</td>
</tr>
<tr>
<td>Number of mutations in all binding sites</td>
<td>0</td>
<td>6</td>
<td>9</td>
<td>14</td>
</tr>
<tr>
<td>Information content without binding-affinity bias</td>
<td>1.13</td>
<td>1.13</td>
<td>1.13</td>
<td>1.13</td>
</tr>
<tr>
<td>Information content with binding-affinity bias</td>
<td>1.77</td>
<td>1.54</td>
<td>1.31</td>
<td>1.31</td>
</tr>
</tbody>
</table>

The motif predicted from the three target regions containing high-affinity binding sites is strongly biased in reference species 1, and it is impossible to predict the native motif from only those three target regions. However, a shadow of this strong binding-affinity bias also exists in orthologous regions of species 2, 3, and 4, so the motifs predicted from these orthologous regions in species 2, 3, and 4 are biased, too. This bias in species 2, 3, and 4, however, is weaker than the bias in reference species 1, and this difference can be exploited for detecting and correcting the binding-affinity bias and for predicting the native motif from the three target regions of high-affinity binding sites in reference species 1 and their orthologous regions in species 2, 3, and 4.

Specifically, the binding-affinity bias introduced by the ChIP-seq experiment in reference species 1 causes a strong increase of the information content of the predicted motif (1.77 bit) compared to the native motif (1.13 bit). The shadow of the binding-affinity bias in species 2, 3, and 4 also causes an increase of the information contents of the motifs predicted in species 2 (1.54 bit), species 3 (1.31 bit), and species 4 (1.31 bit), but this increase in species 2, 3, and 4 is smaller than in reference species 1 (Table 1 and Fig. 1b). The increase of information content decreases with the number of observed mutations and thus the phylogenetic distance of species 2, 3, and 4 to reference species 1 in which the ChIP-seq experiment has been performed. Hence, the observation of a decreased information content of motifs predicted in orthologous regions of phylogenetically related species compared to the information content of the motif predicted in the
5.1 Detecting and correcting the binding-affinity bias in ChIP-Seq data using inter-species information

reference species could indicate the presence of a binding-affinity bias and possibly allow the correction of that bias.

Decrease of information contents in motifs from phylogenetically related species

We investigate this hypothesis on human ChIP-seq data of five transcription factors [10, 24] and multiple alignments of the human ChIP-seq target regions with orthologous regions from monkey, dog, cow, and horse [25] ("Data" Methods). We calculate the information contents of motifs from human (reference species), monkey, dog, cow, and horse for each of the five data sets ("Decrease of information contents in motifs from related species" Methods and present the results in Fig. 2. We find for each of the five data sets that the information content of the motif from the reference species is significantly higher ($p < 1.83 \times 10^{-14}$, Wilcoxon Signed-Rank Test, Additional file 1: Table S1) compared to the information contents of the motifs from monkey, dog, cow, and horse.

Modeling the binding-affinity bias increases classification performance

Motivated by this observation, we develop a phylogenetic footprinting model capable of taking into account the contamination bias ($M^C$), the binding-affinity bias ($M^C_{BA}$), neither one or the other $M^C$, or both ($M^C_{BA}$) ("Modeling the binding-affinity bias" Methods and Additional file 1: Section 1). In order to study to which degree these models are capable of modeling multiple alignments originating from ChIP-seq data, we consider the principle of parsimony [26], which states that the simplest of competing explanations is the most likely to be correct. As the new model $M^C_{BA}$ is more complex than the traditional model $M^C$, we should accept it only if it provides a more accurate representation of the data. A standard approach for measuring how accurately a model represents a data set is to measure its performance of classifying, in this case, motif-bearing and non-motif-bearing alignments, and a standard approach for measuring classification performance is stratified repeated random sub-sampling validation ("Measuring classification performance" Methods, Fig. 5).

Using this approach we measure the performance of the four models $M^C$, $M^C_{BA}$, $M^C$, and $M^C_{BA}$ to classify each of the five data sets against the other four. Fig. 3a shows that $M^C_{BA}$ yields a higher classification performance than $M^C$ in all five data sets ($p < 2.3 \times 10^{-17}$, Wilcoxon Signed-Rank Test, Additional file 1: Table S2), indicating that the new model $M^C_{BA}$ is more realistic than the traditional model $M^C$. We also find that $M^C_{BA}$ yields a significantly higher classification performance than $M^C_{BA}$ in all five data sets ($p < 1.8 \times 10^{-17}$, Wilcoxon Signed-Rank Test), which indicates that taking into account the binding-affinity bias has a larger impact on the classification performance than taking into account the contamination bias (Additional file 1: Figure S1, Figure S2, Figure S10, Figure S11, Figure S12, Figure S13, Figure S14, Figure S15 and Figure S16).

Modeling the binding-affinity bias leads to softened motifs

Next, we investigate the information contents of the corrected motifs predicted by models $M^C_{BA}$ and $M^C_{BA}$ that take into account the binding-affinity bias and the traditional motifs predicted by models $M^C$ and $M^C$ that neglect this bias. Fig. 3b shows that the information contents of motifs predicted by $M^C$ are significantly higher than the information contents of motifs predicted by $M^C_{BA}$ ($p < 4.0 \times 10^{-18}$, Wilcoxon Signed-Rank Test). We also find that the information contents of motifs predicted by $M^C_{BA}$ are higher than the information contents of motifs predicted by $M^C_{BA}$ ($p < 4.0 \times 10^{-18}$, Wilcoxon Signed-Rank Test, Additional file 1: Table S4), stating that...
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Fig. 3 Comparison of models $M_{BA}$ and $M_{C}$. a Mean classification performance and standard error of the two models $M_{BA}$ and $M_{C}$ quantified by the area under the receiver operating characteristic curve. We find for each of the five data sets a significantly increased classification performance for $M_{C}$ compared to $M_{BA}$. Examples for ROC curves are shown in Additional file 1: Figure S10, Figure S11, Figure S12, Figure S13, Figure S14 and Figure S15. b Mean information content and standard error of the motifs predicted by the two models $M_{BA}$ and $M_{C}$. We find for each of the five data sets a significantly decreased information content in motifs predicted by $M_{BA}$ compared to $M_{C}$ ($p < 4.0 \times 10^{-15}$).

the binding-affinity bias is stronger than the contamination bias. Equivalently, this states that the joint effect of both biases leads to an artificial sharpening of the motifs and an artificial overestimation of the binding affinities (Additional file 1: Figure S3, Figure S4, Figure S17, Figure S18).

Finally, we inspect the differences of the corrected motifs predicted by $M_{BA}$ and $M_{C}$ and the traditional motifs predicted by $M_{C}$ and $M_{C}$. Fig. 4 shows the differences between the base distributions of pairs of motifs for $M_{BA}$ and $M_{C}$ by difference logos (“Visualizing motif differences with DiffLogo” Methods). We find for each of the five data sets that the corrected motifs are softer than the traditional motifs distorted by the binding-affinity bias. Specifically, we find that the amount of decrease of the most abundant bases in the corrected motifs compared to the traditional motifs is roughly proportional to the base abundance, whereas the increase of the remaining bases is not proportional to the base abundance. Hence, the corrected motifs are not simply a uniformly softened version of the traditional motifs, but motifs with different degrees of dissimilarity at different positions (Additional file 1: Figure S5, Figure S6, Figure S7, Figure S8 and Figure S9).

Conclusions

We studied the possibility of detecting and correcting the binding-affinity bias in ChIP-seq data using interspecies information. We found that the fact that this bias is stronger in target regions of the reference species than its shadow in orthologous regions of phylogenetically related species enables the detection and correction of this bias. We proposed a phylogenetic footprinting model capable of taking into account the binding-affinity bias in addition to the contamination bias, and we applied this model and its three special cases that neglect one of the two biases or both to five ChIP-seq data sets. We found by stratified repeated random sub-sampling validation that taking into account the binding-affinity bias always improves motif prediction, that the motif binding-affinity bias leads to a distortion of motifs that is even stronger than the distortion caused by the contamination bias, and that the corrected motifs are typically softer than those predicted by traditional approaches. The comparison of corrected and traditional motifs showed small but noteworthy differences, suggesting that the refinement of traditional motifs from databases and from the literature might lead to the prediction of novel binding sites, cis-regulatory modules, or gene-regulatory networks and might thus advance our attempt of understanding transcriptional gene regulation as a whole.

Methods

In this section we describe “Decrease of information contents in motifs from related species” (i) the determination of the information contents of motifs in the reference species and phylogenetically related species, “Modeling the binding-affinity bias” (ii) the phylogenetic footprinting model that can take into account the binding-affinity bias, the contamination bias, neither one or the other, or both, “Measuring classification performance” (iii) the measurement of the classification performance of these four phylogenetic footprinting models using stratified repeated random sub-sampling validation, and “Visualizing motif differences with DiffLogo” (iv) the visualisation of differences between the corrected and the traditional motifs.

Decrease of information contents in motifs from related species

We determine the information content $I(P)$ of a motif $P$ as described in [23]:

$$H_\ell(P) = \log_2(|A|) - \sum_{a \in A} p_{\ell,a} \cdot \log_2(p_{\ell,a})$$

$$I(P) = \sum_\ell H_\ell(P),$$

(1)
5.1 Detecting and correcting the binding-affinity bias in ChIP-Seq data using inter-species information

where \( A = A, C, G, T \) is the alphabet, \( p_{\ell,a} \) is the probability of base \( a \) at position \( \ell \) in motif \( P \), and \( H_\ell(P) \) denotes the information content of position \( \ell \) in motif \( P \).

We measure the information contents of motifs in five species using repeated random sub-sampling as follows. Initially, we choose one motif for each of the transcription factors CTCF, GABP, NRSF, SRF, and STAT1 from the JASPAR database, namely MA0139.1 for CTCF, MA0062.2 for GABP, MA0138.2 for NRSF, MA0083.2 for SRF, and MA0137.3 for STAT1 [27]. In the first step, we generate a test set from the set of positive alignments (Table 2) by removing randomly 200 alignments. In the second step, we predict for each transcription factor one binding site per target region in all target regions of the reference species (human) in the corresponding test data set, extract the predicted binding sites from the reference species as well as the binding sites at the same positions in the orthologous regions, and calculate for each species the information content of the resulting motif as specified above. We perform both steps 100 times and report the mean and standard error of the information content for each of the five species.

Modeling the binding-affinity bias
In this section we describe the probabilistic model for modeling the binding-affinity bias as a data generating process. A derivation of the log-likelihood for motif-bearing and non-motif-bearing alignments can be found in Additional file 1: Section 1.

Let \( O \) be the number of species. A data set comprises \( N \) independent multiple sequence alignments. We use \( X_n \) to refer to the \( n \)-th sequence alignment. Every alignment is formed by \( O \) sequences. The \( o \)-th

Table 2 Data set statistics for human ChIP-seq data. For each of the five transcription factors (TFs) CTCF, GABP, NRSF, SRF, and STAT1, we specify the (i) average length of transcription factor binding site (TFBS), the (ii) number of alignments, and the (iii) average length of alignments.

<table>
<thead>
<tr>
<th>TF</th>
<th>TFBS length</th>
<th>Number of alignments</th>
<th>Avg. length</th>
</tr>
</thead>
<tbody>
<tr>
<td>CTCF</td>
<td>20 bp</td>
<td>467</td>
<td>213 bp</td>
</tr>
<tr>
<td>GABP</td>
<td>12 bp</td>
<td>451</td>
<td>236 bp</td>
</tr>
<tr>
<td>NRSF</td>
<td>21 bp</td>
<td>460</td>
<td>245 bp</td>
</tr>
<tr>
<td>SRF</td>
<td>12 bp</td>
<td>394</td>
<td>242 bp</td>
</tr>
<tr>
<td>STAT1</td>
<td>11 bp</td>
<td>360</td>
<td>244 bp</td>
</tr>
</tbody>
</table>
sequence is denoted by \( X_n^v \). By convention, the reference sequence (that in which the selection process has taken place) is species 1. Each sequence of alignment \( X_n \) is composed of \( L_n \) nucleotides. We denote by \( X_n^{u_o} \) the \( u \)-th nucleotide of the \( o \)-th sequence of the \( n \)-th alignment. All nucleotides are presented by the set \( A = \{A, C, G, T\} \).

We assume the existence of a common ancestor of all of \( O \) species. The sequence of the common ancestor of the \( n \)-th alignment is a hidden variable \( \pi_n \), with \( Y_o^n \) representing its \( u \)-th nucleotide. The substitution probability that nucleotide \( Y_o^n \) is substituted by the nucleotide \( X_n^{u_o} \) is denoted by the variable \( \gamma_{o,u} \).

An alignment \( X_n \) may contain a binding site or not. This is denoted by the variable \( M_n \). The length of the binding site is denoted by the variable \( W \) and the position of the binding site in alignment \( X_n \) is denoted by the variable \( \ell_n \).

The \( n \)-th alignment \( X_n \) is sampled as follows. The first decision to be made is whether or not the alignment contains a binding site. This is denoted by variable \( M_n \), which follows a Bernoulli distribution with parameter \( 1 - \alpha \). Thus, whenever variable \( M_n \) is equal to 1 (\( M_n^1 \)), the alignment contains a binding site and when \( M_n \) is equal to 0 (\( M_n^0 \)), it does not.

Thus, parameter \( \alpha \) is the probability that alignment \( X_n \) contains no binding site. If \( \alpha \) equals 0, the sampled data is uncontaminated, because all alignments contain a copy of the binding site. The larger the value of \( \alpha \), the higher the percentage of non motif-bearing alignments in the sampled data. A value of \( \alpha \) equal to 1 models a data set where no binding sites are present.

Next we introduce the data generating process for non-motif-bearing alignments and later we explain that for motif-bearing alignments.

1. Sample the primordial sequence as follows: For each position \( u \) of the sequence sample nucleotide \( Y_o^n \) from the background equilibrium distribution \( \pi_o \) independent of the previous nucleotides.

2. For each of the descent species \( o \in \{1, \ldots, O\} \), sample its sequence given the primordial sequence as follows: To sample nucleotide \( u \), we apply to nucleotide \( Y_o^n \) of the primordial sequence the F81 \[28\] mutation model taking as equilibrium distribution \( \pi_o \).

The generating process for motif-bearing sequences is slightly more complex, since it has to deal both with the generation of the binding site and with the selection process. First, we describe how to sample an alignment without taking into account the selection process. Second, we show how to modify this procedure so that the selection process is considered.

Sample a motif-bearing alignment \( X_n \) as follows:

1. Sample the start position of the binding site \( \ell_n \) from the uniform distribution.

2. Sample the primordial sequence. For each position \( u \) of the sequence outside the binding site, we sample nucleotide \( Y_o^n \) from the background equilibrium distribution \( \pi_o \). For each position \( u \) of the binding site, we sample nucleotide \( Y_o^n \) from the equilibrium distribution \( \pi_o^{\ell_n-\ell_n+1} \).

3. For each of the descent species \( o \in \{1, \ldots, O\} \), sample its sequence \( X_n^{u_o} \) as follows: For each position \( u \) of the descent species \( o \) outside the binding site, apply to nucleotide \( X_n^{u_o} \) of the primordial sequence the F81 mutation model taking as equilibrium distribution \( \pi_o \). For each position \( u \) of the descent species \( o \) inside the binding site, apply to nucleotide \( X_n^{u_o} \) of the primordial sequence the F81 mutation model taking as equilibrium distribution \( \pi_o^{\ell_n-\ell_n+1} \).

Finally, to model the selection process, we introduce the variable \( \beta \). \( \beta \) is used to quantify the degree of the binding-affinity bias in the reference species. We assume that a transcription factor binds binding site \( B \) with a probability proportional to \( p(B|\pi)\beta^{-1} \). As \( B \) occurs in vivo with probability \( p(B|\pi) \), it occurs in the set of immunoprecipitated sequences with a probability proportional to \( p(B|\pi) \cdot p(B|\pi)\beta^{-1} = p(B|\pi)\beta \).

We can interpret the meaning of \( \beta \) as follows: If \( \beta \) is greater than one, low-affinity binding sites are more frequently rejected with respect to \( p(B) \) and high-affinity binding sites are less frequently rejected with respect to \( p(B) \). This leads to an under-representation of low-affinity binding sites and an over-representation of high-affinity binding sites in the ChIP-seq data set, thus modeling a data set that is affected by the binding-affinity bias. If \( \beta \) is equal to one, low-affinity binding sites are rejected as frequently as high-affinity binding sites, leading to a representative set of binding sites in the ChIP-seq data set, which is not affected by the binding-affinity bias.

Based on that selection model, sample a motif-bearing alignment that has passed the selection process as follows:

1. Sample a motif-bearing alignment disregarding the selection process following the procedure specified above.

2. Decide whether the alignment is accepted or rejected based on the probability of acceptance of the binding site found at the reference species. If the alignment is rejected, go to step 1.

Thus, we denote (i) the model with \( \alpha = 0 \) and \( \beta = 1 \) by \( M^- \), (ii) the model with with \( \alpha > 0 \) and \( \beta = 1 \) by
5.1 Detecting and correcting the binding-affinity bias in ChIP-Seq data using inter-species information

\( M_1 \), (iii) the model with \( \alpha = 0 \) and \( \beta > 1 \) by \( M_{BA} \), and (iv) the model with \( \alpha > 0 \) and \( \beta > 1 \) \( M_1 \). \( M_1 \) can only handle the contamination bias, not the binding-affinity bias. \( M_{BA} \) can only handle the contamination bias, but not the binding-affinity bias. \( M_{BA} \) can only handle the binding-affinity bias, but not the contamination bias. And \( M_{BA} \) can handle both the contamination bias and the binding-affinity bias.

We call \( M_1 \), \( M_1 \), \( M_{BA} \), and \( M_{BA} \) foreground models. For modeling the background alignments, we use the model with \( \alpha = 1 \) and \( \beta = 1 \), which we call background model and which we denote by \( B \).

Measuring classification performance

For measuring the classification performance of the four models \( M_1 \), \( M_{BA} \), \( M_1 \), and \( M_{BA} \), we perform stratified repeated random sub-sampling validation as illustrated in Fig. 5 using data sets of the five human transcription factors CTCF, GABP, NRSF, SRF, and STAT1 that have been used for benchmarking the phylogenetic footprinting program MotEvo [25].

In step 1, we generate two training sets and two disjoint test sets for each of the five transcription factors as follows. We randomly select 200 alignments from the set of alignments (Table 2) of a particular transcription factor as positive training set, and we choose the set of the remaining alignments as positive test set. We randomly select 500 alignments from the set of alignments of the four remaining transcription factors as negative training set and another disjoint set of 500 alignments as negative test set.

In step 2, we train a foreground model \( (M_1, M_{BA}, M_1, M_{BA}) \) on the positive training set and a background model \( B \) on the negative training set by expectation maximization [29] using a numerical optimization procedure in the maximization step.

We restart the expectation maximization algorithm, which is deterministic for a given data set and a given initialization, 150 times with different initializations and choose the foreground model and the background model with the maximum likelihood on the positive training data and the negative training data, respectively, for classification. We use a likelihood-ratio classifier of the two chosen foreground and background models, apply this classifier to the disjoint positive and negative test sets, and calculate the receiver operating characteristics curve, the precision recall curve, and the area under both curves as measures of classification performance.

We repeat both steps 100 times and determine (i) the mean area under the receiver operating characteristic curve and its standard error and (ii) the mean area under the precision recall curve and its standard error.

Data

The data used in this work originate from human ChIP-seq data of the five human transcription factors CTCF, GABP, NRSF, SRF, and STAT1, where the ChIP-seq data for GABP and SRF published in [10] are available from the QuEST web page [30], and the ChIP-seq data for CTCF, NRSF, and STAT1 published in [24] are available from the SISSRs web page [31]. All five data sets have been filtered for high-quality reads and mapped to a reference
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Visualizing motif differences with DiffLogo

We used the R package DiffLogo [35] to depict the differences between the predicted motifs of the models $M^P$, $M^B$, $M^C$, and $M^{PB}$. DiffLogo is an open source software that is capable of depicting the differences between multiple motifs [35]. This is realized by visualizing all pairwise differences in an $N \times N$-grid with an empty diagonal. Each entry in the grid is called difference logo. The degree of difference of two motifs is calculated by the sum of all differences between the base distributions of two sequence motifs. Differences are visualized using a stack of bases for each motif position. A single difference logo depicts the position-specific differences between the base distributions of two sequence motifs. Differences are visualized using a stack of bases for each motif position. The height of each base stack is proportional to the degree of differential symbol abundance. Bases with a positive height indicate a gain of abundance and bases with a negative height indicate a loss of abundance. The stack height in the positive direction must be equal to the stack height in the negative direction, because the sum of base abundance gain must be equal to the sum of base abundance loss.

Additional files

Additional file 1: Supplementary Methods, Results, Figures, and Examples. This file is structured in four sections.

1. Modeling the binding-affinity bias, we describe how to determine the likelihood of non-motif-bearing and motif-bearing alignments modeling the contamination bias and the binding-affinity bias. In section 2, Example interpretation of difference logos, we give an exemplary interpretation of some difference logos.
2. Supplementary Figures, contains supplementary Figures S1-S18.
3. Supplementary Tables, contains supplementary Tables S1-S10.

Additional file 2: Sequence data. This archive contains data files of gap-free alignments of the ChIP-seq positive regions for each of the transcription factors CTCF, GABP, NRSF, SRF, and STAT1 in FASTA format.

Competing interests

The authors declare that they have no competing interests.

Authors' contributions

MN and IG developed the key idea. MN and JC developed the computational methods. MN and HT performed the studies. All authors wrote, read, and approved the final manuscript.

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5.2 Unrealistic phylogenetic trees may improve phylogenetic footprinting

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Combining phylogenetic footprinting with motif models incorporating intra-motif dependencies

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Abstract

Background: Transcriptional gene regulation is a fundamental process in nature, and the experimental and computational investigation of DNA binding motifs and their binding sites is a prerequisite for elucidating this process. Approaches for de-novo motif discovery can be subdivided in phylogenetic footprinting that takes into account phylogenetic dependencies in aligned sequences of more than one species and non-phylogenetic approaches based on sequences from only one species that typically take into account intra-motif dependencies. It has been shown that modeling (i) phylogenetic dependencies as well as (ii) intra-motif dependencies separately improves de-novo motif discovery, but there is no approach capable of modeling both (i) and (ii) simultaneously.

Results: Here, we present an approach for de-novo motif discovery that combines phylogenetic footprinting with motif models capable of taking into account intra-motif dependencies. We study the degree of intra-motif dependencies inferred by this approach from ChIP-seq data of 35 transcription factors. We find that significant intra-motif dependencies of orders 1 and 2 are present in all 35 datasets and that intra-motif dependencies of order 2 are typically stronger than those of order 1. We also find that the presented approach improves the classification performance of phylogenetic footprinting in all 35 datasets and that incorporating intra-motif dependencies of order 2 yields a higher classification performance than incorporating such dependencies of only order 1.

Conclusion: Combining phylogenetic footprinting with motif models incorporating intra-motif dependencies leads to an improved performance in the classification of transcription factor binding sites. This may advance our understanding of transcriptional gene regulation and its evolution.

Keywords: ChIP-Seq, Phylogenetic footprinting, Evolution, Transcription factor binding sites, Gene regulation
take into account intra-motif dependencies. Irrespective of the wide variety of different motif models used, all of these approaches have in common that they do not take into account phylogenetic information available from orthologous sequences of phylogenetically related species.

Complex motif models that take into account intra-motif dependencies have been shown to outperform simpler motif models like the PWM model [11–13]. Examples for highly popular tools that model intra-motif dependencies are Dimont [14], MEME-Chip [15], DeepBind [16], and diChIP Musk [17]. In contrast, the second group of de-novo motif discovery approaches known as phylogenetic footprinting incorporates orthologous sequences of at least two phylogenetically related species. The basic idea of these approaches is that TFBSs tend to be subject to negative selection during evolution, which can increase the recognition of TFBSs in the reference species. Phylogenetic motif models, which model the binding of TFs to their TFBSs and their evolution simultaneously, are based on evolutionary models such as the popular Felsenstein model [18]. Irrespective of the wide variety of different phylogenetic motif models used, all of these approaches have in common that they do not take into account intra-motif dependencies.

Not all sequences from the reference species may have orthologous sequences in phylogenetically related species, and not all aligned sequences may comprise functional TFBSs at the same alignment positions [19]. Moreover, alignment errors, binding site turnovers, and spurious alignments from convergent evolution may affect the utility of phylogenetic footprinting. Nevertheless, phylogenetic footprinting has been shown to outperform one-species approaches for many TFs and have become increasingly attractive due to next generation sequencing and the resulting avalanche of data [20–22].

Examples for highly popular phylogenetic footprinting tools that have been applied to eukaryotes and prokaryotes are FootPrinter [23], PhyME [24], MONKEY [25], MicroFootprint [26], Phylogenetic Gibbs Sampler [27], PhyloGibs [28], PhyloGibs-MP [29], or MotEvo [30].

In summary, one-species approaches neglect phylogenetic information, whereas phylogenetic footprinting, which incorporates this information, neglects intra-motif dependencies. The main objective of this work is to develop an approach that combines these two ideas and to investigate if taking into account intra-motif dependencies can improve phylogenetic footprinting. Specifically, we propose a simple phylogenetic footprinting model (PFM) capable of taking into account both intra-motif dependencies and phylogenetic information in Methods, and we study if modeling intra-motif dependencies improves phylogenetic footprinting based on human ChiP-Seq data of 35 TFs and more than $10^5$ multiple alignments of human ChiP-seq positive regions and their orthologous sequences of 9 mammalian species ranging from chimp to cow in Results.

### Methods

In this section we describe (i) the studied datasets, (ii) the used notation and the likelihood calculation of the PFM, (iii) the performance measure, (iv) the calculation of the mutual information, and (v) details regarding the estimation algorithm and implementation of the proposed model.

### Data

We use freely available ChiP-Seq data for 50 transcription factors from the ENCODE project [31, 32]. The ChiP-seq experiments were performed by several production groups in the ENCODE Consortium and analysed by the ENCODE Analysis Working Group based on a uniform processing pipeline developed for the ENCODE Integrative Analysis effort [33]. We focus on datasets for the human H1-hESC cell line. The uniform processing pipeline utilizes the SPP peak caller [34] and biological replicates (at least two per transcription factor) are analysed jointly with a Irreproducible Discovery Rate (IDR) score of at least 2%. The resulting ChiP-seq regions of the Uniform TFBS track reference the hg19 assembly [35] and each comprise the chromosome, start position, end position, and an enrichment score. We exclude 15 datasets which yield repetitive motifs analog to [13] and hence retain datasets of 35 TFs.

For each TFs we select the top 20% of the available ChiP-seq regions ranked by enrichment score. We denote these regions as ChiP-seq positive regions and use them as basis for the positive dataset (Additional file 1: Table S1 and Additional file 1: Section 1.3). We denote the regions between ChiP-seq positive regions on one chromosome as ChiP-seq negative regions. For each TF we extract two regions of length 500 bp from each ChiP-seq negative region centered at one third and two thirds, and use these as basis for the negative dataset. Hence, there are roughly twice as many negative regions than positive regions. We remove regions from the positive and the negative region sets that are shorter than 20 bp. For each region in the positive and negative region sets we extract the corresponding alignment consisting of 46 mammals using the freely available multiple genome alignment from UCSC [36].

We apply the following steps to each alignment. We remove alignment columns with gap-symbols or ambiguous symbols in the human sequence and concatenate the remaining alignment columns. We retain the 10 species with the best alignment coverage, namely Human (hg19), Chimp (panTro), Baboon (papHam), Orangutan (ponAbe), Rhesus (rheMac), Marmoset (callJac), Horse, (equCab), Dog (canFam), Gorilla (gorGor), and Cow (bosTau).
5.2 Unrealistic phylogenetic trees may improve phylogenetic footprinting

We replace ambiguous symbols with gap-symbols. We remove all alignments which comprise no base symbols for 20% or more species. See Additional file 1: Table S1 for statistics on the number of ChIP-Seq positive regions and the number of extracted alignments and see Additional file 1: Table S2 for details about the origin of the used ChIP-Seq data and Additional file 2 contains all extracted alignments.

Phylogenetic footprinting model

Notation

Each dataset of each TF contains N alignments, with each alignment containing O sequences (one per observed species). Of course the number of alignments per TF, N, varies from TF to TF. See Additional file 1: Table S1. The n-th alignment is denoted by \(X_n\) and its length is denoted by \(L_n\). Each sequence of alignment \(X_n\) is composed of \(L_n\) symbols. We denote by \(X_n^\ell\) the \(\ell\)-th symbol of the \(n\)-th sequence of the \(n\)-th alignment. All symbols belong to the set \(A = \{A, C, G, T, \ldots\}\) where \(A, C, G,\) and \(T\) denote the bases and \(\ldots\) denotes a gap in the alignment. Missing sequences in alignment \(n\) are represented by \(L_n\) gap symbols.

An alignment \(X_n\) may or may not contain a binding site. This is encoded in the variable \(M_n\), with \(M_n = 0\) indicating that alignment \(X_n\) does not contain a motif and \(M_n = 1\) indicating that alignment \(X_n\) does contain a motif. This model is known as ZOOPS (zero or one occurrence of a binding site per sequence) or NOOPS (noisy OOPS) model. Due to its simplicity and its modularity this model is widely used for de-novo motif discovery [37–40].

Likelihood

The probability that the alignment \(X_n\) is generated by our PFM can be written as

\[
p(X_n|\theta) = p(X_n|M_n = 0, \theta) \cdot p(M_n = 0|\theta) + p(X_n|M_n = 1, \theta) \cdot p(M_n = 1|\theta) \tag{1}
\]

with variable \(M_n\) taking a Bernoulli distribution and \(\theta\) denoting model parameters, namely (i) the topology of the phylogenetic tree, (ii) the substitution probabilities, and (iii) the evolutionary model with its stationary probabilities for the flanking regions as well as for the binding site regions.

We need to specify the probability for non-motif-bearing \(p(X_n|M_n = 0, \theta)\) and for motif-bearing alignments \(p(X_n|M_n = 1, \theta)\). For reasons of clarity we omit \(\theta\) in the following.

Likelihood of a non-motif-bearing alignment

Since sequences are assumed to be conditionally independent, the probability of an alignment decomposes as the product of the probability of each of its sequences:

\[
p(X_n|M_n = 0) = \prod_{\ell=1}^{O} p(X_n^\ell|M_n = 0) \tag{2}
\]

Now, the probability of each sequence follows a homogeneous Markov Chain of order C:

\[
p(X_n^\ell|M_n = 0) = \prod_{\ell=1}^{O} p(X_n^\ell|M_n^\ell=1,0, M_n = 0) \tag{3}
\]

where \(p(u,k)\) stands for the (at most C) predecessors of the \(u\)-th base for a sequence starting at position \(k\), namely the set \(p(u,k) = \{v \mid \max(k,u-C) \leq v < u\}\), and

\[
p(X_n^\ell|\theta) = \sum_{u=1}^{L_n-\ell-1} p(X_n|\ell, M_n = 1) \times p(M_n|\ell) \tag{5}
\]

Likelihood of a motif-bearing alignment

We note \(W\) for the length of the motif. Since the motif can be present in different positions, the probability of a motif-bearing assignment is a weighted sum over each possible motif position \(\ell_o\):

\[
p(X_n|\ell_o, M_n = 1) = \prod_{\ell=1}^{O} p(X_n^\ell|\ell, M_n = 1) \tag{6}
\]

And the probability of each single sequence breaks into three parts: (i) an initial non-motif bearing part containing bases \(i(\ell_o) = \{1, \ldots, \ell_o - 1\}\), (ii) the motif, containing bases \(m(\ell_o) = \{\ell_o, \ldots, \ell_o + W - 1\}\) and (iii) a final non-motif bearing part formed by bases \(e(\ell_o) = \{\ell_o + W, \ldots, L_n\}\):

\[
p(X_n^\ell|\ell_o, M_n = 1) = p(X_n^i(\ell_o)|\ell_o, M_n = 1) \times p(X_n^m(\ell_o)|\ell_o, M_n = 1) \times p(X_n^e(\ell_o)|\ell_o, M_n = 1) \tag{7}
\]

with the non-motif bearing parts following a homogeneous Markov Chain of order C as described above.
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5.2 Unrealistic phylogenetic trees may improve phylogenetic footprinting

Implementation

We implement the proposed PFM based on the freely available Java Framework Jstacs [42]. Among others, Jstacs provides ready-to-use sequence models for reuse, numerical and non-numerical optimization procedures for model estimation, serialization of models, and methods for the statistical evaluation of results. In contrast to existing tools which are typically focused on application, using Jstacs we are able to compare different PFMs in a detailed way by extracting mandatory information about the inferred models and the predicted binding sites.

Algorithm 1 shows the pseudocode for inferring a PFM from a set of alignments. The implementation of the proposed phylogenetic footprinting model is available at https://github.com/mgledi/PhyFoo/.

Algorithm 1 Motif discovery algorithm for the proposed PFM. Upon random initialization of the model parameters we iteratively estimate sequence weights and model parameters with multiple algorithm restarts, where $R$ denotes the number of restarts of the whole algorithm, and $S$ denotes the number of iterations. The result is the set of model parameters with maximum likelihood

1. Data: Set of alignments $\{X_1, \ldots, X_N\}$
2. for $r = 1 \ldots R$ do
3.   Initialize $\theta^r$ randomly
4.   for $s = 1 \ldots S$ do
5.     E-step: Estimate $p(X_{\ell}^{\sigma i(t_{\ell}, \sigma)} | \ell, M_r = 1, \theta^r)$ for each position $\ell$ in each alignment $X_{\ell}$ given the model parameters $\theta^r$ (see Eq. 8)
6.     M-step: Maximize $p(X_{\ell}^{\sigma i(t_{\ell}, \sigma)} | \ell, M_r = 1, \theta^r)$ regarding $\theta^{s+1}$ given all alignments and the probabilities $p(X_{\ell}^{\sigma i(t_{\ell}, \sigma)} | \ell, M_r = 1, \theta^s)$ (see Eq. 1)
7.     end for
8.   Keep $\theta^{s+1}$ denoted $\theta$
9. end for
10. Result: $\theta \in \{\theta_1, \ldots, \theta_R\}$ with maximum likelihood

Results and discussion

We propose a model for phylogenetic footprinting that is capable of taking into account intra-motif dependencies as specified in Methods 2. Specifically, we model intra-motif dependencies in TFBSs as well as dependencies among adjacent bases in flanking sequences by Markov models of orders 0, 1, and 2, and we denote the proposed PFM by PFM(0), PFM(1), and PFM(2).

In the first subsection we study if the proposed PFMs can capture intra-motif dependencies of orders 1 and 2 in ChIP-Seq data of 35 TFs. In the second subsection we study if modeling base dependencies can improve phylogenetic footprinting. Both studies are based on human sequences extracted from ENCODE ChIP-seq data [33] and corresponding orthologous sequences of 9 mammalian species, yielding 35 data sets comprising 135196 multiple sequence alignments with an average length of 124 bases (Methods 1).

Intra-motif dependencies can be captured by phylogenetic footprinting

In this subsection we study to which degree intra-motif dependencies can be captured using the PFMs of orders 1 and 2.

We measure the degree of intra-motif dependencies of order 1 between two neighboring bases or of order 2 between a dimer and its neighboring base by the MI as described in Methods 4. The MI quantifies the amount of information in a base or a dimer about the neighboring base in units of bits and ranges from 0 bits in case of statistical independence to 2 bits in case of deterministic dependency of the considered base on the preceding base or the preceding dimer. We compute the MI for every position of a binding site and call the resulting vector of MI values MI profile.

For each of the 35 TFs, we compute the two MI profiles of orders 1 and 2 from the motifs obtained by phylogenetic footprinting using the PFM(2). We present the resulting 35 × 2 MI profiles as Additional file 3 and the 2 × 2 MI profiles of the two TFs CJUN and Nrf as examples in Fig. 1a.

First, we study the MI profiles of order 1 for these two TFs. For both TFs we find statistically significant intra-motif dependencies between neighboring bases at all positions. For CJUN, intra-motif dependencies of order 1 are particularly strong at motif positions 2 to 4, yielding a maximum MI of 0.52 bits at motif position 4. For Nrf, intra-motif dependencies of order 1 are particularly strong at motif positions 8 to 11 and 14 to 15, yielding a maximum MI of 0.23 bits at motif position 11.

Next, we study the MI profiles of order 2. Again, we find statistically significant intra-motif dependencies between dimers and their neighboring bases at all positions for both CJUN and Nrf. For CJUN, intra-motif dependencies of order 2 are particularly strong at motif positions 2 to 4, yielding a maximum MI of 0.70 bits at motif position 3. For Nrf, intra-motif dependencies of order 2 are particularly strong at motif positions 8 to 11 and 13 to 15, yielding a maximum MI of 0.28 bit at motif position 11.

Moreover, we find that intra-motif dependencies of order 2 are significantly stronger than the corresponding intra-motif dependencies of order 1 at several positions for both CJUN and Nrf. Comparing the MI profiles of orders 1 and 2, we find that the MI profile of order 2 is up to twofold higher than the MI profile of order 1 for CJUN and up to sevenfold higher for Nrf, stating that in both TFs there are significant intra-motif dependencies of...
order 2 beyond those expected from the corresponding intra-motif dependencies of order 1.

Next, we study the MI profiles of orders 1 and 2 for all 35 TFs. In order to condense the results and to allow a visual comparison of the results for both profiles and all 35 TFs, we show for each MI profile and each TF the maximum and mean MI values in Fig. 2a.

We find that the average of the 35 maximum MI values of order 1 is 0.39 bits, whereas the average of the 35 maximum MI values of order 2 is significantly greater at 0.56 bits. Likewise, we find that the average of the 35 mean MI values of order 1 is 0.14 bits, whereas the average of the 35 mean MI values of order 2 is significantly greater at 0.23 bits. These observations suggest that intra-motif dependencies are present in all of the studied TFs and that intra-motif dependencies of order 2 are typically stronger than those of order 1.

By scrutinizing Figs. 2a and b, however, we also find that the maximum and mean MI values vary significantly from TF to TF. For example, we find a maximum and mean MI value of order 1 of 0.11 bits and 0.05 bits for CEBPB and a maximum and mean MI value of order 1 of 0.89 bits and 0.20 bits for Mxi. Analogously, we find a maximum and mean MI value of order 2 of 0.16 bits and 0.07 bits for CEBPB and a maximum and mean MI value of order 2 of 1.15 bits and 0.37 bits for Mxi.

To study the possibility that these captured intra-motif dependencies are an artifact resulting from a mixture of different species-specific motifs, we finally study the similarity of the 10 species-specific motifs as well as the 20 species-specific MI profiles of orders 1 and 2. We find that the observed pairwise differences between the species-specific motifs are not significant (Additional file 1: Section 1.1.1). Moreover, we find that the species-specific MI profiles are similar to each other and to the corresponding MI profiles captured by phylogenetic footprinting (Additional file 4, Additional file 1: Section 1.1.2).

Both findings indicate that the intra-motif dependencies shown in Fig. 1b and in Additional file 3 cannot be explained as an artifact resulting from a mixture of different species-specific motifs.

**Modeling intra-motif dependencies improves phylogenetic footprinting**

In this subsection we study if modeling base dependencies can improve phylogenetic footprinting.

First, we compute the classification performance of the PFM of orders 0, 1, and 2 as described in Methods 3. Second, we determine the increase of the classification performance of the PFM taking into account base dependencies of orders 1 and 2 relative to the classification performance of the PFM neglecting base dependencies as described in Methods 3. Here, positive values indicate an increase of classification performance, while negative values indicate a decrease of classification performance.

Figure 3a shows the classification performances of the PFM of orders 0, 1, and 2 for each of the 35 TFs, and Fig. 3b shows the corresponding relative increases. We
Fig. 2 Maximum and average MIs of MI profiles inferred by the PFM(2) for all 35 TFs. In Fig. a we show the maximum MI of the MI profiles of orders 1 and 2. In Fig. b we show the average MI of the MI profiles of orders 1 and 2. The dashed lines indicate the mean of the maximum MIs and the mean of the average MIs for both MI profiles respectively. The degree of intra-motif dependencies depends on the TF and is always larger in case of intra-motif dependencies of order 2. Please see Additional file 3 for the MI profiles of all 35 TFs.

find that modeling base dependencies of order 1 increases the classification performance in 31 of 35 cases, and we find that modeling base dependencies of order 2 increases the classification performance in all of the 35 cases. Moreover, we find that modeling base dependencies of order 2 always yields a higher classification performance than modeling base dependencies of order 1.

By scrutinizing Fig. 3a, we find that the differences of the classification performances of the PFMs of orders 1 and 2 and the PFMs of order 0 vary significantly from TF to TF. For example, in case of base dependencies of order 1 we find the highest difference of 11% for CHD2 and the lowest difference of −1% for Rad21. In case of base dependencies of order 2 we find the highest difference of 13% for Rad21 and the lowest difference of 1% for RXRA.

By scrutinizing Fig. 3b, we find that also the relative increases of classification performances vary significantly from TF to TF. For example, in case of base dependencies of order 1 we find the highest increase of 70% for JARIDA1A and the lowest increase of −7% for Rad21. In case of base dependencies of order 2 we find the highest increase of 78% for JARIDA1A and the lowest increase of 7% for RXRA.

Figure 4 summarizes the results by showing (a) the classification performance of the PFMs of orders 0, 1, and 2 averaged over all 35 TFs and (b) the relative increases of classification performances averaged over all 35 TFs. We observe that the average classification performance increases significantly from order 0 to order 1 and from order 1 to order 2. Specifically, we find that the average classification performance of the PFM(1) is 4.6% higher than that of the PFM(0) and that the average classification performance of the PFM(2) is 3.5% higher than that of the PFM(1). We find that the average relative increase of the classification performance of the PFM(1) over that of the PFM(0) is 25% and that the average relative increase of the classification performance of the PFM(2) over that of the PFM(0) is 42%.

Next, we study the robustness of the proposed approach with respect to the number of species in the multiple sequence alignments. We perform the same study on the same 35 datasets with alignments comprising only subsets of the 10 species, and we find that for all subsets the classification performance increases significantly from order 0 to order 1 for many of the 35 TFs and from order 1 to order 2 for all of the 35 TFs (Additional file 1: Section 1.2).

These findings indicate that taking into account base dependencies improves phylogenetic footprinting, but they also indicate that this improvement is small. Given the fact that taking into account base dependencies improves one-species approaches, too, it could well be that the improvement obtained by taking into account
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![Classification performance for PFM with base dependencies of orders 0, 1 and 2.](image)

**Fig. 3** Classification performance for PFM with base dependencies of orders 0, 1 and 2. 
- **a** We show the mean and standard error of the ROC AUC for PFM of orders 0, 1, and 2 averaged over 25-fold stratified repeated random subsampling. 
- **b** We plot the mean and standard error of the relative increase of the ROC AUC for the PFM of orders 1 and 2 relative to the PFM of order 0 for each of the 35 TFs. Taking into account base dependencies of order 1 increases the classification performance for 31 TFs. Taking into account base dependencies of order 2 increases the classification performance in all cases and is larger compared to taking into account base dependencies of order 1 in all cases. See Additional file 6 for detailed ROC and PR curves for the PFM of order 2.

![Classification performance averaged for all 35 TFS.](image)

**Fig. 4** Classification performance averaged for all 35 TFS. 
- **a** We show the ROC AUC for PFM of orders 0, 1, and 2 in percent averaged over 25-fold stratified repeated random subsampling and averaged over all 35 TFS. The overall classification performance increases with the order of the PFM. 
- **b** We show the improvement of the ROC AUC for the PFM of orders 1 and 2 relative to the PFM of order 0 averaged over 25-fold stratified repeated random subsampling and averaged over all 35 TFS.

Base dependencies in one-species approaches is greater than in phylogenetic footprinting. Such a difference could result in the situation where the advantage of phylogenetic footprinting over one-species approaches when neglecting base dependencies decreases or even turns into a disadvantage when taking into account base dependencies.

To study to which degree the small improvement of phylogenetic footprinting by taking into account base dependencies might be overshadowed by a possibly greater improvement of one-species approaches, we compare the classification performances of the four cases of one-species approaches and phylogenetic footprinting when neglecting and taking into account base dependencies (Additional file 1: Section 1.3). Consistent to previous studies, we find that phylogenetic footprinting yields a higher (lower) classification performance compared to one-species approaches for 23 (12) of the 35 TFS when neglecting base dependencies. When taking into account base dependencies, however, phylogenetic footprinting yields a higher (lower) classification performance compared to one-species approaches in 31 (4) of the 35 TFS.
5.2 Unrealistic phylogenetic trees may improve phylogenetic footprinting

This finding indicates that the small improvement of phylogenetic footprinting by taking into account base dependencies is greater than the corresponding improvement of one-species approaches. It also indicates that the previously observed advantage of phylogenetic footprinting over one-species approaches when neglecting base dependencies (23 to 12) does not decrease or turn into a disadvantage, but becomes even more pronounced (31 to 4), when taking into account base dependencies. This increased advantage of phylogenetic footprinting over one-species approaches achieved by taking into account base dependencies is surprising as it indicates the presence of some synergy of modeling both phylogenetic and base dependencies.

We finally study for each of the 35 TFs which of the four models yields the highest classification performance, and we find that one-species approaches neglecting base dependencies yield the highest classification performance for one TF (CEBPB), one-species approaches taking into account base dependencies yield the highest classification performance, and phylogenetic footprinting taking into account base dependencies yields the highest classification performance for 31 TFs. This finding indicates that phylogenetic footprinting can be improved by taking into account base dependencies, that species-specific TF motifs cannot be improved by taking into account phylogenetic dependencies, and that there is a surprising synergy of simultaneously modeling both phylogenetic and base dependencies.

Conclusions

In this work, we introduced a phylogenetic footprinting model capable of taking into account base dependencies and evaluated this phylogenetic footprinting model on ChIP-seq data of 35 TFs. We found significant intra-motif dependencies of orders 1 and 2 in all 35 datasets and that the inferred intra-motif dependencies of order 2 are stronger than those of order 1 for all 35 TFs. We also found that these intra-motif dependencies cannot be explained as an artifact resulting from a mixture of different species-specific motifs. We further found that the classification performance of the introduced phylogenetic footprinting model is higher than that of phylogenetic footprinting models neglecting base dependencies for all of the 35 TFs and higher than that of one-species approaches for 31 of the 35 TFs. These findings suggest that combining phylogenetic footprinting with motif models incorporating intra-motif dependencies may lead to an improved prediction of TFBSs and thus advance our understanding of transcriptional gene regulation and its evolution.
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References

5.3 Combining phylogenetic footprinting with motif models incorporating intra-motif dependencies

Phlogenetics

Unrealistic phylogenetic trees may improve phylogenetic footprinting

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Abstract

Motivation: The computational investigation of DNA binding motifs from binding sites is one of the classic tasks in bioinformatics and a prerequisite for understanding gene regulation as a whole. Due to the development of sequencing technologies and the increasing number of available genomes, approaches based on phylogenetic footprinting become increasingly attractive. Phylogenetic footprinting requires phylogenetic trees with attached substitution probabilities for quantifying the evolution of binding sites, but these trees and substitution probabilities are typically not known and cannot be estimated easily.

Results: Here, we investigate the influence of phylogenetic trees with different substitution probabilities on the classification performance of phylogenetic footprinting using synthetic and real data. For synthetic data we find that the classification performance is highest when the substitution probability used for phylogenetic footprinting is similar to that used for data generation. For real data, however, we typically find that the classification performance of phylogenetic footprinting surprisingly increases with increasing substitution probabilities and is often highest for unrealistically high substitution probabilities close to one. This finding suggests that choosing realistic model assumptions might not always yield optimal predictions in general and that choosing unrealistically high substitution probabilities close to one might actually improve the classification performance of phylogenetic footprinting.

Availability and Implementation: The proposed PF is implemented in JAVA and can be downloaded from https://github.com/mgledi/PhyFoo

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Supplementary information: Supplementary data are available at Bioinformatics online.

1 Introduction

Gene regulation is a highly complex process in nature based on several sub-processes such as transcriptional regulation including DNA methylation (Smith and Meissner, 2013), histone modifications (Tessarz and Kouzarides, 2014) and promoter escaping (Sainsbury et al., 2015) as well as post-transcriptional regulation including modulated mRNA decay (Schoenberg and Maquat, 2012), siRNA interference (de Fougerolles et al., 2007; Tam et al., 2008) and alternative splicing (Luco et al., 2010; Sultan et al., 2008). One important step in this complex process is the regulation of transcriptional initiation by the interaction of transcription factors (TFs) with their binding sites (Hobert, 2008; Voss and Hager, 2014). Hence, identifying transcription factor binding sites (TFBSs) and inferring their binding motifs is a prerequisite in modern...
5.3 Combining phylogenetic footprinting with motif models incorporating intra-motif dependencies

biology, medicine and biodiversity research (Nowrousian, 2010; Villar et al., 2014). The last decade has witnessed a spectacular development of sequencing technologies unleashing new potentials in identifying TFBSs (Kalakowskii et al., 2010; Furey, 2012; Lasken and McLean, 2014; van Dijk et al., 2016). Due to the increasing number of available genomes of different species and due to increasing computational resources, approaches for de-novo motif discovery based on phylogenetic footprinting have become increasingly attractive.

Examples of highly popular tools for phylogenetic footprinting are FootPrinter (Blanchette and Tompa, 2003), PhyMe (Sinha et al., 2004), MONKEY (Moses et al., 2004a), PhyloGibbs ( Siddharthan et al., 2005), Phylogenetic Gibbs Sampler (Newberg et al., 2007), PhyloGibs-MP ( Siddharthan, 2008) and MotEvo (Arnold et al., 2012). Supplementary Table S1 provides a comparison of these tools regarding the used evolutionary model, sequence model and learning principle.

One prerequisite for most phylogenetic footprinting approaches are multiple sequence alignments (MSAs) of upstream regions of orthologous genes of multiple not too closely related species (Anisimova et al., 2013). These MSAs capture phylogenetic information, and the key idea of using these MSAs as starting point for phylogenetic footprinting results from the observations that (i) functional TFBSs are phylogenetically conserved and (ii) phylogenetically conserved TFBSs are aligned in MSAs. Examples of highly popular tools for aligning non-coding genomic regions are T-Coffee (Notredame et al., 2000), WalFRANK (Lottspeich and Goldman, 2010) and MAFFT (Katoh and Standley, 2013).

Phylogenetic footprinting improves the de-novo motif discovery by incorporating phylogenetic dependencies within the MSA in contrast to approaches based on sequences from only one species. Such evolutionary models of DNA sequence evolution such as the F81 model (Felsenstein, 1981) have been adapted to model the evolution of TFBSs in a species-specific manner, and it has been shown that these adapted models, which we call phylogenetic footprinting models (PFMs) for brevity, can detect TFBSs more accurately than models that neglect phylogenetic dependencies (Clark et al., 2007; Gertz et al., 2006; Hardison and Taylor, 2012; Hawkins et al., 2009; Moses et al., 2004a; Nettling et al., 2017).

One fundamental prerequisite for phylogenetic footprinting is a phylogenetic tree including substitution probabilities attached to each of its branches, and choosing an appropriate phylogenetic tree and appropriate substitution probabilities is pivotal for the classification performance of phylogenetic footprinting (Kc and Livesay, 2011). However, estimating substitution probabilities within TFBSs is substantially harder than estimating them e.g. in protein-coding regions for at least two reasons:

First, the positions of TFBSs are unknown when performing phylogenetic footprinting, whereas the positions of protein-coding regions are known when estimating substitution probabilities there. Second, protein-coding regions are much longer than TFBSs, so one can use a much larger number of bases for estimating substitution probabilities for protein-coding regions than for TFBSs.

Estimating substitution probabilities within TFBSs is challenging, but several valuable studies have been performed in this direction (Doniger and Fay, 2007; Pollard et al., 2010; Schaeffer et al., 2015; Tugrul et al., 2015). For example, studies on synthetic data have indicated that small substitution probabilities in the motif and moderate substitution probabilities in the flanking sequences can be preferable for motif recognition (Sinha et al., 2004), and studies on different yeast species have confirmed these findings and shown that the likelihood of the Jukes-Cantor model (Jukes and Cantor, 1969) increases relative to a thymine background (\textit{"polyT}) for small substitution probabilities in the motif and moderate substitution probabilities in the flanking sequences (Moses et al., 2004b).

These and similar findings, however, have not lead to a robust approach of estimating substitution probabilities within TFBSs prior to or as part of phylogenetic footprinting, so the substitution probabilities are often simply taken from the literature or guessed, and their influence on the classification performance of phylogenetic footprinting has not yet been studied systematically.

Here, we study this influence based on a synthetic dataset and five real datasets of the TFs CTCF, GABP, NRSF, SRF and STAT1. Specifically, we describe the PFM, the datasets, the tested phylogenetic trees, the performance measure, and implementation details in section Methods, and we study the classification performance of phylogenetic footprinting as a function of the substitution rate for synthetic and real datasets, compare the results to those of phylogenetic footprinting based on expert trees from the literature, and discuss the findings in the context of several factors that affect the evolution of TFBSs in sections 3 and 4.

2 Materials and methods

In this section we describe (i) the used notation and the likelihood calculation of the PFM, (ii) the investigated datasets, (iii) the performance measure, (iv) the systematic investigation of phylogenetic trees and (v) the implementation of the PFMs.

2.1 Phylogenetic footprinting model

2.1.1 Notation

Our data contains N alignments, with each alignment containing O sequences (one per observed species) of length Lw.

Our phylogenetic model incorporates the existence of H additional hidden species, that is, species for which we cannot observe their sequences. Both hidden and observed species conform a tree.

First, for each species k but the root, pa(k) denotes the ancestor of species k in the tree. The root species is noted r. Our probabilistic model contains a random variable S_n^k for each nucleotide 1 \leq n \leq L_w of each species 1 \leq k \leq O + H of each alignment 1 \leq n \leq N. These random variables take values in the set of bases \{A, C, G, T\}. We note pa(S_n^k) the nth nucleotide in the nth alignment of species pa(k) (the ancestor of k). By definition, the root has no ancestor and hence pa(S_{n}^{r}) = \emptyset. We also refer to nucleotide S_n^k as A_n^k when species k is observed, and as Y_n^k when species k is hidden. Furthermore we note by V_n^k (respectively S_n^k) the set containing each random variable Y_n^k (respectively S_n^k), with O + 1 \leq k \leq O + H and Y_n^k the set containing every random variable in V_n^k with 1 \leq n \leq L_w.

An alignment A_n may or may not contain a TFBS. This is encoded in variable M_n, with M_n^k indicating that alignment A_n does not contain a motif and M_n^k indicating that alignment A_n does contain a motif.

2.1.2 Likelihood

The probability that the alignment A_n is generated by the PFM can be written as

\[ p(A_n | \theta) = p(A_n | M_n^0, \theta) \times p(M_n^0 | \theta) + p(A_n | M_n^1, \theta) \times p(M_n^1 | \theta) \]

with variable M_n taking a Bernoulli distribution and \theta denoting model parameters, namely the topology of the phylogenetic tree, the substitution probabilities and the evolutionary model with its
stationary probabilities for the flanking regions as well as the TFBS regions.

We need to specify the probability for non-motif-bearing \( p(A_i|M_i) \) and for motif-bearing alignments \( p(A_i|M_i^*) \). For reasons of clarity we omit \( \theta \) in the following.

### 2.1.3 Likelihood of a non-motif-bearing alignment

The probability that alignment \( A_i \) is generated by the PFM as a non-motif-bearing alignment is

\[
p(A_i|M_i) = \sum_{Y_i} p(A_i|Y_i, M_i^*)
\]

(1)

We assume that each nucleotide alignment is independent of any other nucleotide alignment given \( \theta \) and \( M_i^* \). Furthermore, we assume that in each nucleotide alignment, the species satisfy the conditional independencies encoded by the phylogenetic tree. Thus,

\[
p(A_i|M_i^*) = \prod_{j=1}^{t} \sum_{x_{ij}} p(S_i^j|x_{ij}, M_i^*)
\]

(2)

\[
- \prod_{j=1}^{t} \sum_{x_{ij}} \prod_{k=1}^{L_i} p(S_i^k|x_{ij}, p_a(S_k^k), M_i^*)
\]

(3)

where

\[
p(S_i^k) = \frac{a(S_i^k - b, M_i^*)}{2}
\]

\[
p_i^k = \begin{cases} \gamma_k & \text{if } k = r \\ \gamma_k \times p_i^k + (1 - \gamma_k) \delta_{k-1} & \text{if } k \neq r 
\end{cases}
\]

according to the F81 model, where the base distribution of each position of the background sequence is denoted by \( \tau_k \), the probability of a nucleotide \( a \) in the background sequence is denoted by \( p_a \), and the substitution probability from the ancestor species to species \( k \) is denoted by \( \gamma_k \). For more realistic phylogenetic models \( \gamma_k \) might also depend on specific nucleotide transitions.

### 2.1.4 Likelihood of a motif-bearing alignment

The probability that alignment \( A_i \) is generated by the PFM as a motif-bearing alignment is

\[
p(A_i|M_i^*) = \sum_{x_{ij}} p(A_i|Y_i, \ell_i, M_i^*)
\]

(4)

where \( W \) is the length of the TFBS and \( \ell_i \) is the position of the TFBS in alignment \( A_i \). Since single nucleotide alignments are assumed independent and considering the conditional independencies in the phylogenetic tree we have

\[
p(A_i|M_i^*) = \prod_{j=1}^{t} \sum_{x_{ij}} p(A_i|M_i^*)
\]

(5)

with \( p(S_i^j|x_{ij}, M_i^*) = \prod_{k=1}^{L_i} p(S_i^k|x_{ij}, p_a(S_k^k), M_i^*) \) and

\[
- \prod_{j=1}^{t} \sum_{x_{ij}} \prod_{k=1}^{L_i} p(S_i^k|x_{ij}, p_a(S_k^k), M_i^*)
\]

\[
p(S_i^k|x_{ij}, p_a(S_k^k), M_i^*) = \begin{cases} \gamma_k^i & \text{if } k = r \\ \gamma_k^i \times p_i^k + (1 - \gamma_k^i) \delta_{k-1} & \text{if } k \neq r
\end{cases}
\]

As for the non-motif-bearing alignment, the base distribution of each position of the background sequence is denoted by \( \tau_k \) and the probability of a nucleotide \( a \) in the background sequence is denoted by \( p_a \). The base distributions of a motif sequence of length \( W \) are denoted by \( p_a \) with \( a \in \{1, \ldots, W \} \) and the probability of a nucleotide \( a \) at position \( j \) in a motif sequence is denoted by \( p_j^a \). The substitution probability from the ancestor species to species \( k \) is denoted by \( \gamma_k \).

Finally we assume motifs to be uniformly distributed, thus having that \( p(a^W_i|M_i^*) = \frac{1}{W} \), which completes the specification of the likelihood function.

### 2.2 Data

#### 2.2.1 Real data

The data used in this work originate from human Chip-Seq data of the five TFs CTCF, GABP, NRSF, SRF and STAT1 (Itoh et al. (2008); Valouev et al. (2008)) and gapped alignments of the Chip-Seq target regions from human with orthologous regions from monkey, cow, dog and horse. The original data provided by Arnold et al. (2012) consist of 900 gapped alignments for each of the five TFs. Each gapped alignment consists of sequences from six species. Since gapped alignments have a higher risk of showing mathematical side effects, we process them to derive ungapped alignments following three steps:

(i) We remove the species that causes the highest number of gaps in all alignments. Accordingly, we remove sequences from opossum and keep orthologous regions from human, monkey, cow, dog and horse.

(ii) In each alignment, we remove all alignment columns that contain at least one gap. (iii) We remove all alignments that are shorter than 21 bp, which is the length of the longest TFBS motif (NRSF) in the presented studies. Supplementary Table S2 shows details about the resulting datasets. All datasets are available as Supplementary Material.

#### 2.2.2 Synthetic data

The synthetic dataset used in this work is generated using the PFM specified in section 2.1 with a star topology.

A negative set of 1000 non-motif-bearing alignments each of length \( L = 300 \) is generated. Each non-motif bearing alignment is generated in two steps as follows. (i) Sample the primordial sequence. For each position \( u \in \{1, L\} \) of the sequence, sample a nucleotide from the uniform distribution \( \tau_u \). (ii) For each of the descent species \( o \in \{1, \ldots, 5\} \), sample a mutated sequence given the primordial sequence position-wise. For each position \( u \in \{1, L\} \), apply the F81 Felsenstein (1981) mutation model with the equilibrium distribution \( \tau_u \) and substitution probability \( \gamma = 0.2 \) to the nucleotide of the primordial sequence at position \( u \).

A positive set of 750 motif-bearing alignments each of length \( L = 300 \) is generated. Each motif-bearing alignment is generated as follows:

(ii) Sample the primordial sequence given a TFBS length of \( W = 15 \).

(a) Sample the start position \( \ell \in \{1, L-W+1\} \) of the TFBS from the uniform distribution.

(b) For each position \( u \in \{1, \ell - 1\} \) and \( u \in \{\ell + W, L\} \) of the flanking sequence, we sample the nucleotide at position \( u \) from the uniform distribution \( \tau_u \). For each position \( u \in \{\ell, \ell + W - 1\} \) of the TFBS, we sample the nucleotide at position \( u \) from the distribution \( \pi_{\ell, \ell}\cdot \). The distribution \( \pi_{u, w} \) with \( u \in \{1, \ldots, 15\} \) is uniformly drawn from the simplex.

(iii) For each of the descent species \( o \in \{1, \ldots, 5\} \), sample a mutated sequence given the primordial sequence position-wise.

(a) For each position \( u \in \{1, \ell - 1\} \) and \( u \in \{\ell + W, L\} \) of the flanking sequence, apply the F81 mutation model with the equilibrium distribution \( \tau_u \) and substitution probability \( \gamma = 0.2 \) to the nucleotide of the primordial sequence at position \( u \).

(b) For each position \( u \in \{\ell, \ell + W - 1\} \) of the TFBS, apply the F81 mutation model with the equilibrium distribution \( \tau_{\ell, \ell}\cdot \) and substitution probability \( \gamma = 0.2 \) to the nucleotide of the primordial sequence at position \( u \).
5.3 Combining phylogenetic footprinting with motif models incorporating intra-motif dependencies

2.3 Phylogenetic trees
To systematically investigate the influence of different phylogenetic trees on classification performance and hence on motif prediction, we introduce two simplifications. First, the underlying phylogenetic tree is a star topology implying that all species have one common ancestor. Second, all branches in the star topology have the same length, i.e. the probability that a base in the primordial sequence is replaced by a new base in a descendant sequence is the same for all sequences.

Now, it is possible to systematically vary the substitution probabilities \( \gamma = (0.05, 0.1, \ldots, 1.0) \), where \( \gamma \) is inversely proportional to the phylogenetic relatedness. Small \( \gamma \) encode close phylogenetic relations and large \( \gamma \) encode distant phylogenetic relations. Especially, \( \gamma = 1.0 \) implies that the species are phylogenetically unrelated, i.e. the sequences of each alignment are statistically independent.

2.4 Classification performance
We evaluate all PFMs by a stratified repeated random sub-sampling validation by estimating all PFMs from a training set and measuring classification performance on a test set as follows.

In step 1, we generate two training sets and two disjoint test sets for each of the five TFs as follows. We randomly select 200 alignments from the set of alignments of a particular TF as positive training set, leaving the remaining alignments as positive test set. We perform a base shuffling on the positive set of alignments of the same TF to get a negative set of alignments. We randomly select 200 alignments from this set of shuffling as negative training set and leave the remaining alignments as negative test set.

In step 2, we train a foreground model on the positive training set and a background model on the negative training set by expectation maximization (Lawrence and Reilly, 1990) using a numerical optimization procedure in the maximization step. We restart the expectation maximization algorithm, which is deterministic for a given dataset and a given initialization, 20 times with different initializations and choose the foreground model and the background model with the maximum likelihood on the positive training data and the negative training data, respectively, for classification. We use a likelihood-ratio classifier of the two chosen foreground and background models, applying this classifier to the positive and negative test sets, and calculate the area under the receiver operating characteristic curve and the area under the precision recall curve as measures of classification performance.

We repeat both steps 100 times and determine (i) the mean area under the receiver operating characteristic curve and its standard error and (ii) the mean area under the precision recall curve and its standard error.

2.5 Implementation
In order to investigate the influence of different phylogenetic trees in a fair and detailed way, we implement the proposed PFM on the freely available Java Framework *Jstacs* (Grau et al., 2012). Among others, *Jstacs* provides ready-to-use sequence models for reuse, numerical and non-numerical optimization procedures for model estimation, serialization of models and methods for the statistical evaluation of results. In contrast to existing tools which are typically focused on application, using *Jstacs* we are able to compare different PFMs in a detailed way by extracting mandatory information about the inferred models and the predicted TFBSs.

**Algorithm 1** shows the pseudocode for inferring a PFM from a set of alignments. The implementation of the proposed PFM is available at https://github.com/mgledi/PhyFoo.

```plaintext
Algorithm 1. Motif discovery algorithm for the proposed PFM. Upon random initialization of the model parameters we iteratively estimate sequence weights and model parameters in multiple algorithm restarts, where \( K \) denotes the number of restarts of the whole algorithm, and \( T \) denotes the number of iterations. The result is the set of model parameters together with maximum likelihood.

1: Data: Set of alignments \( A = \{A_1, \ldots, A_N\} \)
2: Flanking model: Maximize \( p(A|\theta^0) \) for the model parameters \( \theta^0 \subset \theta^1 \).
3: for \( t = 1 \ldots K \) do
   4: Initialize \( \pi_n \subset \theta^1 \) randomly for \( n \in \{1, \ldots, W\} \).
   5: for \( t = 1 \ldots T \) do
      6: E-step: Estimate \( p(A_n|\pi_n, M_T, \theta^t) \) for each position \( \pi_n \) in each alignment \( A_n \) given the model parameters \( \theta^t \).
      7: M-step: Maximize the expected value of the complete-data log-likelihood with respect to model parameters \( \pi_n \) and denote the resulting argmax by \( \theta^{t+1} \).
   8: end for
   9: Keep \( \theta^{t+1} \) denoted \( \theta^t \).
10: end for
11: Result: \( \theta \in \{\theta_1, \ldots, \theta_K\} \) with maximum likelihood.
```

3 Results
In this section, we investigate the classification performance of the PFM specified in section 2.1 as a function of the substitution probability for a synthetic dataset and five real datasets. The synthetic dataset is generated using the PFM described in section 2.2. The five real datasets originate from human CHIP-Seq experiments of the five TFs CTCF, GABP, NRSF, SRF and STAT1 and MSAs of the predicted target regions with orthologous regions from monkey, cow, dog and horse as described in section 2.2.

In section 2.1.1, we study the likelihood of the popular PFM specified in section 2 as a function of the substitution probability for the synthetic dataset and the real dataset of TF CTCF. In section 2.1.2, we study the classification performance of the PFM as a function of the substitution probability for the same datasets. In section 2.1.3, we study the classification performance of the PFM as a function of the substitution probability for the same datasets. In section 2.1.4, we study the classification performance of the PFM based on three selected phylogenetic trees for all five datasets of the TFs CTCF, GABP, NRSF, SRF and STAT1.

3.1 Likelihood on synthetic and real data
First, we test the implemented expectation maximization algorithm for the PFM specified in section 2.1 and summarized in **Algorithm 1** by applying it to synthetic data generated with a substitution probability of 0.2 as described in section 2.2 and to real data of TF CTCF. In both cases, we vary the substitution probability \( \gamma \) of the PFMs from 0.05 to 1.0 with increments of 0.05.

In case of synthetic data, we expect the best fit of the PFMs and thus the highest likelihood when the substitution probability \( \gamma \) of the PFMs is close to the substitution probability of 0.2 used for data generation. In case of real data of TF CTCF, we expect the best fit of the PFMs and thus the highest likelihood when the substitution
probability $\gamma$ of the PFMs is in the range of 0.1 $\leq \gamma \leq 0.4$ according to Gertz et al. (2006).

Figure 1a shows the likelihood as a function of the substitution probability $\gamma$ ranging from 0.05 to 1.0 with increments of 0.05 for synthetic data, and we observe the expected function with a maximum at the substitution probability of $\gamma = 0.2$, which is equal to the substitution probability used for data generation. Figure 1b shows the likelihood as a function of the substitution probability $\gamma$ for real data of TF CTCF, and we again observe the expected function with a maximum at the substitution probability of $\gamma = 0.2$, which is a reasonable value and in the range of 0.1 $\leq \gamma \leq 0.4$ suggested by Gertz et al. (2006).

These findings indicate that the applied PFM and the applied maximum-likelihood principle are capable of identifying reasonable substitution probabilities for synthetic and real data of TF CTCF, where reasonable substitution probabilities mean substitution probabilities close to those used for data generation in case of synthetic data and in the range suggested by experts for real data of TF CTCF.

### 3.2 Classification performance on synthetic and real data

Second, we study the classification performance of the PFMs by the method described in section 2.3 on the same two datasets. We again vary $\gamma$ from 0.05 to 1.0 with increments of 0.05 and compute the classification performance as a function of $\gamma$ as described in section 2.4.

In case of both synthetic and real data, we expect that the classification performance looks qualitatively similar to the likelihood as a function of $\gamma$, i.e., we expect that the classification performance is highest for $\gamma$ close to 0.2 for synthetic data and in the range of 0.1 $\leq \gamma \leq 0.4$ for real data of TF CTCF.

Figure 2a shows the classification performance as a function of $\gamma$ for synthetic data, and we observe the expected function with a maximum at $\gamma = 0.2$, which is equal to the substitution probability used for data generation and equal to the location of the maximum of the likelihood. These results are in agreement with those of Sinha et al. (2004) who additionally find that an underestimation of the true substitution probability leads to a more severe degradation of the classification performance than an overestimation of equal magnitude.

Figure 2b shows the classification performance as a function of $\gamma$ for real data of TF CTCF, but here we observe a function that is different from the expected function, different from the function observed for synthetic data, and different from the likelihood function of Figure 1b. Specifically, we observe that the maximum is achieved for an unrealistically high value of $\gamma = 1.0$, which is clearly outside of the range of substitution probabilities of 0.1 $\leq \gamma \leq 0.4$ suggested by Gertz et al. (2006) and much greater than the value of $\gamma = 0.2$ at which the maximum of the likelihood is located.

This observation is surprising because a substitution probability of $\gamma = 1.0$ corresponds to a PFM that assumes the orthologous sequences in the MSAs be statistically independent, i.e. phylogenetically unrelated. It indicates that choosing a realistic substitution probability in the range of 0.1 $\leq \gamma \leq 0.4$ might lead to an inferior classification performance of phylogenetic footprinting compared to choosing an unrealistic substitution probability of $\gamma = 1.0$.

### 3.3 Classification performance and likelihood on four additional real datasets

Third, we study if the phenomenon that the maximum classification performance is achieved for an unrealistically high value of $\gamma$ is specific for TF CTCF or possibly also present in other TFs. Hence, we perform the studies of sections 2.2.1 and 2.2.2 for four additional ChIP-Seq datasets of TFs GABP, NRSF, SRF and STAT1.

Figure 3a–d shows the four classification performances and the four likelihoods as functions of $\gamma$. For the likelihoods, we observe clear maxima for realistic substitution probabilities in the range of 0.1 $\leq \gamma \leq 0.2$ in all four cases. However, for the classification performances, we observe the four maxima for unrealistically high substitution probabilities $\gamma \geq 0.8$. This observation is again surprising and states that the classification performance of phylogenetic footprinting is higher for an unrealistically high substitution probability of $\gamma = 1.0$ than for realistic substitution probabilities in the range of 0.1 $\leq \gamma \leq 0.4$ for all five TFs CTCF, GABP, NRSF, SRF and STAT1.

In order to test if this result could be an artifact of the choice of the negative dataset, we study the classification performance when negatives are taken from the positives of the other datasets as done by Arnold et al. (2012). We obtain the same surprising results that the classification performance is higher for a substitution probability of $\gamma = 1.0$ than for realistic substitution probabilities for all five TFs (Supplementary Figs S5, S9, S13, S17 and S21).

Next, we scrutinize the motifs obtained by PFMs with a substitution probability of $\gamma = 1.0$. For synthetic data, we find that the motifs obtained by PFMs with $\gamma = 1.0$ are highly similar to the motifs used for data generation (Supplementary Fig. S1). For real data, we find that the motifs obtained by PFMs with $\gamma = 1.0$ are highly similar to the motifs obtained by PFMs with realistic substitution probabilities in the range of 0.1 $\leq \gamma \leq 0.4$ (Supplementary Figs S2, S6, S10, S14 and S22). These findings suggest that the
5.3 Combining phylogenetic footprinting with motif models incorporating intra-motif dependencies

Fig. 3. Classification performance and likelihood for different substitution probabilities. We plot the classification performance (decreasing) and likelihood (increasing) on data of the four TFs GABP, NRSF, SRF and STAT1 for substitution probabilities γ ∈ (0.05, 0.1, ..., 1.0). (a) GABP. The maximum likelihood is achieved for γ = 0.2. The best classification performance is achieved for γ = 1.0. (b) NRSF. Maximum likelihood is achieved for γ = 0.15. The best classification performance is achieved for γ = 0.8. (c) STAT1. The maximum likelihood is achieved for γ = 0.15. The best classification performance is achieved for γ = 1.0. For each of the four TFs, we find qualitatively similar curves when quantifying the classification performance by the area under the PR curve (see Supplementary Figs S8, S12, S16 and S20).

3.4 Classification performance using realistic phylogenetic trees

Fourth, we study if the phenomenon that the maximum classification performance is achieved for unrealistically high values of γ, which we observed for PFMs with a star topology, also occurs when using realistic phylogenetic trees. This study is motivated by observations that PFMs with phylogenetic trees with realistic tree topologies have the potential to yield higher classification performances than PFMs with phylogenetic trees with unrealistic star topologies (Newberg et al., 2007; Palumbo and Newberg, 2010).

Hence, we study the classification performances of PFMs on synthetic data with different tree topologies and different substitution probabilities, and we find in all cases the highest classification performances near the substitution probabilities used for data generation (Supplementary Material section 4.2 and Supplementary Fig. S25). In addition to generating synthetic data by the F81 substitution model (Felsenstein, 1981), we also generate them by the more realistic HKY substitution model Hasegawa et al. (1985) in combination with different tree topologies and different substitution probabilities, and we find again the highest classification performances near the substitution probabilities used for data generation (Supplementary Material sections 4.4 and 4.5 and Supplementary Figs S27 and S28).

Next, we study the classification performance of the PFM on real data using a phylogenetic tree and substitution probabilities from the literature (Arnold et al., 2012). We denote the PFM with a phylogenetic tree and substitution probabilities from the literature by $\lambda^{M^{CTCF}}$, the PFM with a phylogenetic tree with a star topology and substitution probabilities according to the maximum-likelihood estimates of Figures 1b and 3a-d by $\lambda^{M^{M^{CTCF}}}$, and the PFM with a phylogenetic tree with a star topology and substitution probabilities of $\gamma = 1.0$ by $\lambda^{M^{M^{CTCF}}}$.

Figure 4 shows the classification performances of $\lambda^{M^{CTCF}}$, $\lambda^{M^{M^{CTCF}}}$ and $\lambda^{M^{M^{CTCF}}}$ for each of the five TFs CTCF, GABP, NRSF, SRF and STAT1. Interestingly, we find that $\lambda^{M^{M^{CTCF}}}$ yields a significantly higher classification performance than the other two PFMs. In addition, we investigate the classification performances of PFMs with a star topology and a tree topology from the literature with branch lengths estimated from the data, and we find also in this case that $\lambda^{M^{M^{CTCF}}}$ yields a significantly higher classification performance than the other two PFMs (Supplementary Material section 3 and Supplementary Fig. S23).

These findings state that, in case of real data, choosing unrealistic model assumptions—namely a phylogenetic tree with a star topology and substitution probabilities of $\gamma = 1.0$—might yield higher classification performances than the same PFMs with more realistic phylogenetic trees and more realistic substitution probabilities.

4 Discussion

Possible explanations for this unexpected observation might be unrealistic model assumptions of the substitution model, heterogeneous substitution probabilities at different TFBS positions, and different DNA regions, heterogeneous substitution probabilities at different times of evolution, or the construction of incorrect or at least partially erroneous MSAs.

Violations of model assumptions sometimes lead to a poor classification performance or to a strange dependence of the classification performance on one or several model parameters. Such a situation might occur in phylogenetic footprinting, where PFMs typically assume the same phylogenetic tree and the same substitution probabilities for all positions of all TFBSs, for all TFBSs and all of their flanking regions, and for all chromosomal regions and all MSAs despite the fact that all of these assumptions are almost certainly violated (Conrad et al., 2011; Lercher and Hurst, 2002; Moses et al., 2003; Schuster-Böckler and Lehrer, 2012; Tian et al., 2008; Weber et al., 2007; Wolfe et al., 1989).

Heterogeneous substitution probabilities among different DNA regions are omnipresent and typically taken into account when modeling the evolution of proteins or protein-coding genes. However, this heterogeneity is typically neglected in PFMs, where this...
assumption would lead to potential over-fitting (Hawkins, 2004) due to the facts that the positions of TFBSs are unknown in phylogenetic footprinting and that TFBSs are much shorter than protein-coding genes.

Heterotachous substitution probabilities, i.e., substitution probabilities that vary with time, are another feature that is typically neglected in PFMs despite being omnipresent in both functional TFBSs as well as their flanking regions. Neglecting heterotachy might lead to the estimation of severely biased substitution probabilities, to incorrect motif predictions, and thus to a poor classification performance (Kolaczkowski and Thornton, 2004).

Incorrect or at least partially erroneous MSAs are another problem that might lead to the violation of model assumptions (Kim and Ma, 2011; Lo¨ytynoja et al., 2012). In particular, insertions and deletions as well as heterogeneity in sequence composition such as a varying GC-content (Hardison and Taylor, 2012) might cause MSA algorithms to become potentially imprecise and might thus affect all downstream analyses (Lo¨ytynoja and Goldman, 2008).

Maximum-likelihood estimators can be proven to achieve the highest classification performance in the asymptotic limit of infinitely large datasets and under the prerequisite that the models used for classification are exactly those used for data generation. However, both prerequisites are typically not fulfilled in practice, so it often happens that the highest classification performance is not achieved by those parameters that maximize the likelihood.

This situation apparently occurs for phylogenetic footprinting in a surprisingly pronounced manner, which seems to indicate that the likelihoods of currently used PFMs are less affected by violated model assumptions than their classification performances. On an intuitive level, PFMs with realistic phylogenetic trees and realistic substitution probabilities seem to be more strongly affected by heterogeneity, heterotachy, and errors in MSAs than PFMs with unrealistically high substitution probabilities, so using such unrealistically high substitution probabilities might be a temporarly useful choice until more sophisticated PFMs capable of coping with heterogeneity, heterotachy and errors in MSAs are being developed.

5 Conclusions

We have studied the influence of choosing different phylogenetic trees and different substitution probabilities on the likelihood and the classification performance of PFMs. We have performed these studies on synthetic and real data obtained from ChiP-Seq experiments performed in human and MSAs of ChiP-Seq positive regions with upstream regions of orthologous genes in monkey, cow, dog and horse.

We find that the likelihood depends on the substitution probability in a qualitatively similar manner for synthetic and real data, where it reaches a maximum for realistic substitution probabilities in the range of $0.1 \leq \gamma \leq 0.2$. In contrast, we find that the classification performance depends on the substitution probability in a qualitatively different manner for synthetic and real data.

For synthetic data, the classification performance reaches a maximum at the values of the substitution probability used for data generation, which coincide with those values that maximize the likelihood. For real data, however, it increases with the substitution probability and stops increasing only at unrealistically high values of the substitution probability in the range of $0.8 \leq \gamma \leq 1$, which are very different from those values that maximize the likelihood.

We find in all of the studied datasets that PFMs using unrealistic substitution probabilities of $\gamma = 1.0$ yield higher classification performances than PFMs using realistic substitution probabilities.

One possible explanation for this strange behavior of the classification performance on the substitution probability is the presence of heterogeneous and heterotachous substitution probabilities, which are neglected by currently used PFMs, and the sensitive dependence of PFMs on the reconstructed MSAs that might be partially incorrect.

Apparently, PFMs using unrealistic substitution probabilities of $\gamma = 1.0$ are more robust to these and possibly other violations of the model assumptions than PFMs based on realistic substitution probabilities, and this robustness might lead to less biased parameter estimates and thus more accurate phylogenetic footprints.

This observation leads to the strange practical recommendation of using PFMs using unrealistic substitution probabilities of $\gamma = 1.0$ instead of using PFMs using realistic substitution probabilities until there are more sophisticated models for the evolution of TFBS and their flanking regions that take into account heterogeneity and heterotachy as well as partially erroneous alignments in a position-specific manner.

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Conflict of Interest: none declared.

References


5.3 Combining phylogenetic footprinting with motif models incorporating intra-motif dependencies


5. PREDICTING TRANSCRIPTION FACTOR BINDING SITES USING PHYLOGENETIC FOOTPRINTING
6 Visualisation of motifs

6.1 DiffLogo: A comparative visualisation of sequence motifs

DiffLogo: a comparative visualization of sequence motifs

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Abstract

Background: For three decades, sequence logos are the de facto standard for the visualization of sequence motifs in biology and bioinformatics. Reasons for this success story are their simplicity and clarity. The number of inferred and published motifs grows with the number of data sets and motif extraction algorithms. Hence, it becomes more and more important to perceive differences between motifs. However, motif differences are hard to detect from individual sequence logos in case of multiple motifs for one transcription factor, highly similar binding motifs of different transcription factors, or multiple motifs for one protein domain.

Results: Here, we present DiffLogo, a freely available, extensible, and user-friendly R package for visualizing motif differences. DiffLogo is capable of showing differences between DNA motifs as well as protein motifs in a pair-wise manner resulting in publication-ready figures. In case of more than two motifs, DiffLogo is capable of visualizing pair-wise differences in a tabular form. Here, the motifs are ordered by similarity, and the difference logos are colored for clarity. We demonstrate the benefit of DiffLogo on CTCF motifs from different human cell lines, on E-box motifs of three basic helix-loop-helix transcription factors as examples for comparison of DNA motifs, and on F-box domains from three different families as example for comparison of protein motifs.

Conclusions: DiffLogo provides an intuitive visualization of motif differences. It enables the illustration and investigation of differences between highly similar motifs such as binding patterns of transcription factors for different cell types, treatments, and algorithmic approaches.

Keywords: Sequence analysis, Sequence logo, Sequence motif, Position weight matrix, Binding sites

Background

Biological polymer sequences encode information by the order of their monomers, i.e., bases or amino acids. Often specific parts of the polymer sequence are of particular interest, as they encode, for instance, the binding of transcription factors to specific binding sites [1, 2], the binding to micro-RNA-targets in mRNAs, splice donor sites and splice acceptor sites in pre-mRNAs [3, 4], the presence of phosphorylation sites in proteins, or the folding of specific protein domains [5]. The set of subsequences of one specific biological process are often represented as a sequence motif.

A sequence motif is a model, that represents the preference for the monomers based on a set of aligned biopolymer sequences. Sequence motifs are the result of pipelines comprising wet-lab experiments and motif prediction algorithms, and are frequently used as the basis of in silico predictions [6]. Thus, sequence motif are critical for research of a wide range of problems in biology and bioinformatics.

Considering a particular transcription factor, there are many pipelines that combine wet-lab experiments such as HT-SELEX [7, 8], ChIP-Seq [9] or DNase-Seq footprinting [10] with motif prediction algorithms such as MEME [2, 11], ChIPMunk [12], POSMO [13], or Dimont [14]. Wet-lab experiments differ in their experimental setup, e.g., ecotypes, cell types, developmental stage, time points, or treatment, and motif prediction algorithms differ in their mathematical theory and implementation details.

Visualizing the results of motif discovery is nowadays accomplished by sequence logos [15], the de facto...
standard for visualizing motifs in biology and bioinformatics. Sequence logos emerged as an essential tool for researchers to interpret findings, document work, share knowledge, and present results.

However, comparing multiple sequence logos by visual inspection is sometimes tricky. Differences between sequence logos of two unrelated transcription factors are usually obvious, whereas differences between sequence logos of the same transcription factor are often less obvious and rather hard to perceive as depicted in Fig. 1. Moreover, the results of motif discovery algorithms need to be compared against huge reference databases such as JASPAR [16] or UniProbe [17] or motifs from literature.

For this reason, the comparison of motifs is of primary interest. Several numerical measures including variants of Euclidean distance, Pearson correlation, and Jensen-Shannon divergence have been used to compare motifs [18–21]. These measures express the difference of motifs as a single number that can be easily utilized subsequently, e.g., for rankings or clustering algorithms. However, these measures lose the information of what exactly makes the difference between the motifs of interest. Hence, the comparison of multiple pairs of motifs can result in similar measures.

There are various tools for the analysis and visualization of motifs as summarized in Table 1. The R package seqLogo [22] is an implementation of sequence logos. In the context of motif comparison, sequence logos may be interpreted as a comparison of the input motif with a uniformly distributed motif. The web application iceLogo [23] extends this approach by comparing the input motif with a motif that follows the same background distribution at each motif position. Basically, seqLogo and iceLogo are designed for the presentation of single motifs. In contrast, the R package MotifStack [24] and the web application STAMP [25] are designed for the presentation of multiple motifs. Here, the input motifs are clustered and presented as sequence logos. Thus, the approach of both tools may be interpreted as multiple comparisons with a uniformly distributed motif. The web application Two Sample Logo [26] is capable of comparing two input motifs on the basis of probability theory. This comparison is performed for each motif position individually and results in a sophisticated motif comparison. Depending on the focus of each tool, the input format is a set of aligned sequences and/or a position frequency matrix or position weight matrix. In addition, some tools focus exclusively on DNA motifs, while others cover DNA, RNA, and protein motifs or even allow arbitrary alphabets. Table 1 summarizes tools and their capabilities. In section 4 of Additional file 1, we additionally provide comparative example plots generated by seqLogo, iceLogo, STAMP, Two Sample Logo, and DiffLogo.

We intend the pair-wise comparison of motifs and extend this idea towards the comparison of multiple motifs as follows.

We focus on the comparison of position-specific symbol distributions of two motifs. We neglect dependencies between different motif positions to reduce complexity. As suggested by the sequence logo approach, we intend to represent the characteristics of each motif position by the two properties stack height and symbol height within a stack. The stack height is to be proportional to the degree of distribution dissimilarity. The symbol height is to be proportional to the degree of differential symbol abundance.

We intend to compare three or more motifs on the basis of pair-wise motif comparisons. This comparison is to take into account all pair-wise motif comparisons, suggesting an arrangement in a grid with one row and one column for each motif and one cell for each motif comparison. Similar motifs are to be placed in nearby rows and columns, and the degree of similarity between all motifs is to become obvious at a glance analogous to heatmaps. The grid is to be complemented with a display of the individual sequence logos for further comparisons.

![Fig. 1 Sequence logos of CTCF motifs from cell lines H1-hESC and HUVEC. The two sequence logos are highly similar in their conservation profile (height of stacks) and nucleotide preference at the individual motif positions.](image-url)
6. VISUALISATION OF MOTIFS

Table 1 Comparison of related tools. We compare six publicly available tools on the basis of five criteria.

<table>
<thead>
<tr>
<th>Tools</th>
<th>Alphabet</th>
<th>Input format</th>
<th>Comparison</th>
<th>Clustering</th>
<th>Extensible</th>
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<tr>
<td>iceLogo</td>
<td>DNA/RNA, proteins</td>
<td>sequences</td>
<td>average</td>
<td>-</td>
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<tr>
<td>MotifStack</td>
<td>any</td>
<td>matrix</td>
<td>uniform</td>
<td>hclust</td>
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<td>UPGMA/SOTA</td>
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</tr>
<tr>
<td>Two Sample Logo</td>
<td>DNA/RNA, proteins</td>
<td>sequences</td>
<td>position-specific</td>
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</tr>
<tr>
<td>DiffLogo</td>
<td>any</td>
<td>sequences, matrix</td>
<td>position-specific</td>
<td>hclust, optimal leaf ordering</td>
<td>✓</td>
</tr>
</tbody>
</table>

In the first and second columns, we examine the kind of supported input, in the third and fourth column we examine the mode of action, and in the fifth column we examine whether the tool is extensible. For the criterion “alphabets” we summarize the supported biopolymers out of DNA, RNA, and proteins or arbitrary alphabets in case of “any”. For the criterion “input format” we discriminate a set of “sequences” versus “matrix”, which addresses at least one out of the formats position weight matrix (PWM), position frequency matrix (PFM), and position count matrix (PCM). For the criterion “comparison” we characterize the kind of distribution that is used for motif comparison (“uniform” is the uniform distribution, “average” is the average base distribution in a set of sequences, and “position specific” is a position-specific distribution). For the criterion “clustering” we point out whether there is a clustering of motifs and which cluster-algorithm is used. For the criterion “extensible” we note whether the tool is extensible by the user.

Implementation
In this section, we first define the used notation. We then briefly describe the classical sequence logo. Subsequently, we introduce the difference logo for the visualization of pair-wise motif differences. We discuss this new method and explore potential biological interpretations. Finally, we propose an approach for employing difference logos for the joint comparison of multiple motifs.

Basic notation and sequence logo
Consider a motif as an abstract description of a given set of aligned sequences of common length \( L \) from the alphabet \( \mathcal{A} \). The relative frequency of symbol \( a \in \mathcal{A} \) at position \( \ell \in [1, L] \) corresponds to the (estimated) probability \( p_{\ell,a} \). In case of two motifs, we use \( p_{\ell,a} \) for the first motif and analogously \( q_{\ell,a} \) for the second motif.

The well-known sequence logo visualizes a motif with a symbol stack for each position. We denote the height of the stack at position \( \ell \) by \( H_\ell \) and the height of symbol \( a \) within this stack by \( H_{\ell,a} \). In the traditional sequence logo, \( H_\ell \) and \( H_{\ell,a} \) are defined by

\[
H_\ell = \log_2(|\mathcal{A}|) - \sum_{a \in \mathcal{A}} p_{\ell,a} \cdot \log_2(p_{\ell,a}) \tag{1}
\]

\[
H_{\ell,a} = p_{\ell,a} \cdot H_\ell \tag{2}
\]

which states that the height of a stack at position \( \ell \) reflects the degree of conservation at position \( \ell \) quantified by the information content and that the height of each symbol at position \( \ell \) is proportional to its frequency at position \( \ell \). Hence, the traditional sequence logo is an intuitive visualization of both (i) conserved motif positions and (ii) abundant bases.

The approach of DiffLogo
As specified earlier, we compare motifs per position. Similar to the sequence logo, we show a symbol stack for each position. We redefine the calculation of \( H_\ell \) and use this measure as the total height of position \( \ell \) reflecting the difference of the symbol distribution of both motifs at this position. We redefine the calculation of \( H_{\ell,a} \) and use this measure as the height of a symbol within the stack at position \( \ell \). In the following, \( H_{\ell,a} \) can be positive or negative. Symbols with positive values \( H_{\ell,a} \) are plotted upward. Symbols with negative values \( H_{\ell,a} \) are plotted downward.

Generally, there is a plethora of well-understood mathematical criteria that can be combined to define the height of a symbol stack and the relative heights of symbols within the stack such as probability differences, information divergences, distance measures, or entropies [27]. In the following, we present DiffLogo with the example of the Jensen-Shannon divergence for the calculation of \( H_\ell \) and normalized probability differences for the calculation of \( H_{\ell,a} \). We denote the combination of these two measures as weighted difference of probabilities.

Weighted difference of probabilities
We calculate the stack height for each motif position using the Jensen-Shannon divergence. The Jensen-Shannon divergence is a measure for the dissimilarity of two probability distributions based on information theory [28] (see Fig. 2). In contrast to other measures, the Jensen-Shannon divergence shows a comparable behavior when evaluating dissimilarities of distributions near the uniform distribution. The Jensen-Shannon divergence of two motifs at position \( \ell \) is given by

\[
H_\ell = \frac{1}{2} \sum_{a \in \mathcal{A}} p_{\ell,a} \log_2 \frac{p_{\ell,a}}{m_{\ell,a}} + \frac{1}{2} \sum_{a \in \mathcal{A}} q_{\ell,a} \log_2 \frac{q_{\ell,a}}{m_{\ell,a}},
\]

where \( m_{\ell,a} = p_{\ell,a} + q_{\ell,a} \).

We define the height of each symbol by

\[
H_{\ell,a} = r_{\ell,a} \cdot H_\ell,
\]

where \( r_{\ell,a} \) is the relative frequency of symbol \( a \) at position \( \ell \).
where we define the weight $r_{\ell,a}$ as
\[
r_{\ell,a} = \begin{cases} 
\frac{p_{\ell,a} - q_{\ell,a}}{\sum_{a' \in A} |p_{\ell,a'} - q_{\ell,a'}|} & \text{if } p_{\ell} \neq q_{\ell} \\
0 & \text{otherwise.}
\end{cases}
\] (5)

$r_{\ell,a}$ is the probability difference of symbol $a$ at position $\ell$ between two motifs normalized by the sum of absolute probability differences at this position. We use normalized probability differences as these are indicators for the gain or loss of symbol abundance and provide a view on the symbol distribution differences of both motifs. As a consequence, symbols less abundant in the second motif compared to the first motif are plotted upward, and symbols more abundant in the second motif compared to the first motif are plotted downward.

This representation emphasizes a high gain or loss of probability in co-occurrence with a high gain or loss of information content. The sum of the heights of symbols with a gain of probability and the sum of the heights of symbols with a loss of probability are equal at every position, because each gain of probability of one symbol implies a loss of probability of the remaining symbols. The advantage of this approach is that we are capable of seeing differences of position-specific symbol distributions and of seeing those symbols that are responsible for these differences by gaining or losing abundance.

**Comparison of multiple motifs**

According to the requirements formulated above, we propose a visualization for the joint comparison of $N \geq 3$ motifs given the measure $H_{\ell}$ as follows.

We plot the difference logos of all $N \times (N - 1)$ motif pairs with a common ordinate scaling. We define a scalar dissimilarity value $D$ for a pair of motifs as the sum of all stack heights in the corresponding difference logos,
\[
D = \sum_{\ell=1}^{L} H_{\ell}. \quad (6)
\]

We compute a motif order to group similar motifs. Here, we take the optimal leaf order of a hierarchical clustering of the motifs based on $D$ (function `hclust` in R package `stats` and function `orderoptimal` in R package `cba`). We arrange the difference logos ordered in an $N \times N$ grid with an empty diagonal. Difference logos opposing each other across the diagonal of the grid correspond to each other by an inversion of the ordinate. We visualize $D$ with the background color of the corresponding difference logo using a color gradient from green (most similar among all pairwise comparisons) to red (most dissimilar). We outline the motif names above each column and left of each row. In addition, we allow the possibility of drawing the classic sequence logos and the cluster tree above the columns as auxiliary information.

The advantage of this approach is that we are capable of surveying the overall similarities and dissimilarities in the resulting difference logo grid. Greenish regions indicate similar motif groups and reddish rows and columns indicate less similar motifs. Given a region of interest, it is furthermore possible to comprehend the origins of dissimilarities from the individual difference logos and optionally the sequence logos.

**R package**

`DiffLogo` is written in R [29]. We provide the implementation as a ready-to-use R package. For symbol drawing, `DiffLogo` uses adapted methods from the package.
seqLogo [22] in the software suite bioconductor [30]. DiffLogo allows the analysis of sequence motifs defined over arbitrary alphabets.

The core functions can be parameterized with functions for $H_\ell$ and $r_{\ell\alpha}$. Hence, the user is capable of combining different formulae for $H_\ell$ and $r_{\ell\alpha}$. We provide implementations of the Jensen-Shannon divergence and the normalized probability difference used for the difference logos presented in this manuscript. In addition, DiffLogo provides other implementations for $H_\ell$ and $r_{\ell\alpha}$ as alternatives. Exemplarily, we show the result of eight different combinations of measures for stack height and symbol height in Additional file 1: Tables S1 and S2. The DiffLogo package comprises example data, example code, and further documentation.

Results and discussion
In this section, we present three examples demonstrating the utility of DiffLogo in different applications. First, we examine differences in motifs of DNA binding sites of the same transcription factor from five different cell lines. Second, we examine differences in motifs of DNA binding sites of three different transcription factors with similar binding motifs. Third, we examine differences in motifs of a protein domain.

DNA motifs of same transcription factor
We consider sequence logos and difference logos of binding sites of the human insulator CTCF in different cell lines as obtained by motif discovery from ChIP-seq data [31] based on preprocessed ChIP-seq data from the ENCODE project. For CTCF motif inference, sequences with $p$-values smaller than $10^{-6}$ were selected. All data are freely available as Additional File of the original publication [31]. Since CTCF is a DNA-binding protein, the alphabet corresponds to the four nucleotides in this case.

In Fig. 1, we plot the sequence logos for two of these cell types, namely H1-hESC and HUVEC. Considering the sequence logos, both motifs look highly similar with regard to the conservation as well as the nucleotide preference of individual motif positions, and differences between both motifs are hard to perceive. Considering the corresponding difference logo in Fig. 3 (row 1, column 5 or row 5 column 1), however, we instantly see that indeed a large number of motif positions exhibits differences in nucleotide composition. We find the largest difference.

![Fig. 3](image-url)
6.1 DiffLogo: A comparative visualisation of sequence motifs


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According to the difference logo at position 8 of the motifs, where nucleotide C is more prevalent in cell type H1-hESC compared to HUVEC, whereas the opposite holds for nucleotide T. This difference is less visible in the sequence logos, even with hindsight from the difference logo, due to the low conservation at this position. Specifically, the probability of C increases from 0.35 (HUVEC) to 0.58 (H1-hESC), whereas the probability of T drops by a factor of 2 from 0.44 (HUVEC) to 0.21 (H1-hESC). Depending on the application, this difference at position 8 might have a decisive influence on the outcome of, e.g., *in silico* binding site prediction.

In the literature, several positions with substantial motif differences uncovered by DiffLogo are known to be related to CTCF binding affinity. For instance [32] show that "low occupancy" CTCF binding sites are enriched for C or G at position 18 compared to "high occupancy" sites, which in our case might indicate that the H1-hESC ChIP-seq data set contains a larger number of such "low occupancy" sites than the HUVEC data set.

In a large-scale study [33], CTCF core motifs are partitioned by the presence or absence of additional upstream and downstream motifs, where the greatest variations in the core motifs between partitions can be found at positions 1-3, 6, 8, 11, 12, 18, and 20, which cover those positions varying in the difference logo. Again, these partitions are related to binding affinity and occupancy of CTCF.

In summary, DiffLogo helps to identify several motif positions with substantial variation between cell types, known to be related to CTCF binding affinity and binding site occupancy.

In real-world applications, motifs for more than two cell types are often studied, which might render the pairwise comparison of difference logos a tedious task. We support such an evaluation across multiple cell types by a structured visualization of multiple difference logos as shown in Fig. 3. Here, we compare the pairwise difference logos of CTCF motifs from five cell types, namely H1-hESC, MCF7, HeLa-S3, HepG2, and HUVEC. The cluster tree and background color of the cells are based on numerical measures of motif differences (cf. Implementation) and guide us to the most notable differences between pairs of motifs. For instance, we observe from the tree and background colors that the motifs of H1-hESC and MCF7 are highly similar. The same holds true for the motifs of HeLa-S3, HepG2, and HUVEC, whereas motifs show substantial differences between these two groups. To further facilitate the visual comparison of multiple motifs, we leaf-order the cluster tree such that neighboring motifs are as similar as possible. Due to this ordering, the difference between motif pairs increases with increasing distance from the main diagonal of the difference logo grid. For instance, the topology of the clustering would allow to invert the order of the three leaves under the right sub-tree in Fig. 3, which, however, would bring the quite dissimilar motifs of H1-hESC and MCF7 in direct neighborhood. From Fig. 3, we also observe that the two motifs of H1-hESC and HUVEC are the most dissimilar ones among the motifs studied. A visualization of all nine available motifs can be found in Additional file 1: Figure S1.

**DNA motifs of different transcription factors**

We demonstrate the utility of DiffLogo for motifs derived from binding assays for the human transcription factors Max, Myc, and Mad (Mxi1) from Mordelet et al. [34]. These three basic helix-loop-helix transcription factors are members of a regulatory network of transcription factors that controls cell proliferation, differentiation, and cell death. Each transcription factor binds to different sets of target sites, regulates different sets of genes, and thus plays a distinct role in human cells. However, Myc, Max, and Mad have almost identical PWMs, which all correspond to an E-box motif with consensus sequence CACGTG.

The PWMs considered here have been derived from probe sequences and corresponding binding intensities of *in vitro* genomic context protein-binding microarrays [34]. The exact binding sites within the probe sequences are predicted by the de-novo motif discovery tool Dimont [14] using Slim models [35]. For each of the three transcription factors, the top 1,000 predicted binding sites are used to generate the corresponding PWM.

In Fig. 4, we plot the sequence logos and difference logos of Myc, Max, and Mad. We observe from the sequence logos that the binding motifs are almost identical. Considering the difference logos, we observe that the six core nucleotides are conserved in the motifs of all three transcription factors. We find the largest differences between the motif of Max and the motifs of Myc and Mad. In case of Max and Myc, we find a Jensen-Shannon divergence greater than 0.01 bit at positions 11, 12, 22, and 26. In case of Max and Mad, we find a Jensen-Shannon divergence greater than 0.01 bit at positions 3, 12, 22, and 25. In both cases, we mainly find more purine (adenine and guanine) in the motif of Max than in the motifs of Myc and Mad.

**Protein motifs**

As a third example, we demonstrate the utility of DiffLogo using the F-box domain, which plays a role in protein-protein binding. The complete F-box domain in this example is 48 amino acids long [36]. Here, we investigate the middle section from the 12th to the 35th amino acid.

In Fig. 5, we plot the sequence logos and difference logos of F-box domains from the three kingdoms metazoa, fungi, and viridiplantae. We observe from the cluster
Fig. 4 Comparison of E-Box motifs of Max, Myc, and Mad using DiffLogo. We plot all pair-wise difference logos and display the distance between each motif using the background color from green (similar) to red (dissimilar). We plot the sequence logos of each motif as well as the leaf-ordered cluster tree above. The motifs of the transcription factors Myc and Mad are more similar to each other than to the motif Max. The six core nucleotides with consensus sequence CACGTG are conserved in the motifs of all three transcription factors and, hence, are not visible in the difference logos.

tree and the background colors that the motifs of metazoa and fungi are highly similar, whereas motifs of this group show substantial differences to viridiplantae. The largest difference can be seen between motifs of metazoa and viridiplantae.

When comparing metazoa and fungi with viridiplantae, DiffLogo identifies positions 6, 17, and 22 with high values of the Jensen-Shannon divergence. The differences at positions 6 and 22 could be expected from the differences of the sequence logos, whereas the differences at position 17 are not immediately obvious from them. At position 6 the abundance of arginine (R) in viridiplantae is 0.54 and thus more than 10 times higher than in fungi and 12 times higher than in metazoa. At position 22 tryptophane (W) is highly abundant in viridiplantae and 4 and 3.4 times more abundant than in metazoa and fungi. At position 17 the most noticeable differences in viridiplantae to fungi and metazoa can be seen for amino acid cysteine (C), valine (V), alanine (A), and serine (S). The overall abundance increases from 0.13 in metazoa and 0.12 in fungi to 0.64 in viridiplantae. In contrast, the abundance of arginine (R), glutamine (Q), and lysine (K) is only 0.044 in viridiplantae and 0.44 in metazoa and fungi. A visualization of the full F-Box domain from four kingdoms can be found in Additional file 1: Figure S2.

Conclusion
We present DiffLogo, an easy-to-use tool for a fast and efficient comparison of motifs. DiffLogo may be applied by users with only basic knowledge in R and is highly configurable and extensible for advanced users. We introduce weighted differences of probabilities to emphasize large differences in position-specific symbol distributions. We present visual comparisons of multiple motifs stemming from motifs of one transcription factor in different cell types, different transcription factors with similar binding motifs, and species-specific protein domains. Figures generated by DiffLogo enable the identification of overall motif groups and of sources of dissimilarity. Using DiffLogo, it is easily possible to compare motifs from different sources, so DiffLogo facilitates decision making, knowledge sharing, and the presentation of results. We make DiffLogo freely available in an extensible, ready-to-use R package including examples and documentation. DiffLogo is part of Bioconductor.
6.1 DiffLogo: A comparative visualisation of sequence motifs

**Fig. 5** Comparison of three F-box domain motifs using DiffLogo. We compare the F-box domains from the kingdoms metazoa, fungi, and viridiplantae and plot all pair-wise difference logos and display the distance between each motif using the background color from green (similar) to red (dissimilar). We plot the sequence logos of each motif as well as the leaf-ordered cluster tree above. The motifs of metazoa and fungi are highly similar. All other pairwise comparisons show substantial differences.

**Availability and requirements**

- **Project name:** DiffLogo
- **Project home page:** http://github.com/mgledi/DiffLogo
- **Availability:** http://bioconductor.org/packages/DiffLogo
- **Operating system(s):** Platform independent
- **Programming language:** R
- **Other requirements:** Installation of R 1.8.0 or higher
- **License:** LGPL (≥ 2)
- **Any restrictions to use by non-academics:** None

**Additional file**

- **Additional file 1:** Supplementary Methods, Results, Figures, and Examples. This file is structured in four sections. Section 1, Additional examples, contains Figures S1 and S2. Figure S1 shows a DiffLogo grid for nine CTCF motifs. In section 2, CTCF with and without clustering, we show in detail the impact of clustering and optimal leaf ordering for a DiffLogo grid of nine CTCF motifs. In section 3, Alternative combinations of stack heights and symbol weights, we first describe the mathematical background of four implementations of $H_\ell$ and two implementations of $r_\ell$. Afterwards, we show the result of the eight possible combinations in Tables S1 and S2 on two sequence motifs. In section 4, Tool comparison, we compare DiffLogo with the five tools seqLogo, iceLogo, MotifStack, STAMP, and Two Sample Logo.

**From the set of nine CTCF motifs we selected the pair of motifs with the highest similarity according to the Jensen-Shannon divergence (GM12878 and K562) and the pair of motifs with the lowest similarity according to the Jensen-Shannon divergence (H1-hESC and HUVEC) for the comparison of the five different tools. (PDF 8775 kb)**

**Competing interests**
The authors declare that they have no competing interests.

**Authors’ contributions**
MN conceived the idea. MN, HT, JK, JG, SP, and IG developed the idea and the computational methods. MN and HT implemented and tested DiffLogo. All of the authors read and approved the final version of the manuscript.

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6. VISUALISATION OF MOTIFS


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7 Appendix

The following sections contain important additional studies important for the understanding of this thesis. More supplementary studies, figures, and tables can be found in the additional files of the corresponding articles.

7.1 Detecting and correcting the binding-affinity bias in ChIP-Seq data using inter-species information

The supplementary material of “Detecting and correcting the binding-affinity bias in ChIP-seq data using inter-species information” consists of two additional files. Additional File 1 consists of 3 sections. In Section 1, Modeling the binding-affinity bias, we describe how to determine the likelihood of non-motif-bearing and motif-bearing alignments modeling the contamination bias and the binding-affinity bias. In Section 2, Example interpretation of difference logos, we give an exemplary interpretation of some difference logos. Section 3, Supplementary Figures, contains Supplementary Figures S1-S18. Additional File 2 contains the sequence data used in the studies of this work. Here, I provide a copy of Section 1 of Additional File 1. This section is the mathematical counter part to the section “Modeling the binding-affinity bias” in “Methods” in the main manuscript, where modeling the binding-affinity bias is explained from the data generating perspective.

7.1.1 Modeling the binding-affinity bias

In this section we describe the probabilistic model for modeling the binding-affinity bias. We define the model in mathematical terms by providing the likelihood function. We use the notation from the manuscript.

Following the data-generating process described in the manuscript, the probability that the model generates an alignment $X_n$ can be written as

$$p(X_n|\theta) = p(X_n|M_n = 0, \theta) \cdot p(M_n = 0, \theta) + p(X_n|M_n = 1, \theta) \cdot p(M_n = 1, \theta)$$

$$= p(X_n|M_n = 0, \theta) \cdot \alpha + p(X_n|M_n = 1, \theta) \cdot (1 - \alpha)$$

To complete the model, we need to specify the probability for non-motif-bearing alignments $p(X_n|M_n = 0, \theta)$ and that for motif-bearing alignments $p(X_n|M_n = 1, \theta)$. 
Likelihood of a non-motif-bearing alignment

Looking at the description of the generating process for non-motif-bearing alignments we get

\[ p(X_n|M_n = 0, \theta) = \sum_{Y_n \in A} p(Y_n|M_n = 0, \theta) \prod_{o=1}^{O} p(X_{n}^{o}|Y_n, M_n = 0, \theta). \]

Note that given \( \theta \) and \( M_n = 0 \), each single nucleotide alignment is independent of any other single nucleotide alignment. Thus, the likelihood can be expressed as

\[ p(X_n|M_n = 0, \theta) = L_n \prod_{u=1}^{L_n} \sum_{Y_{n}^{u} \in A} p(Y_{n}^{u}|M_n = 0, \theta) \prod_{o=1}^{O} p(X_{n}^{u,o}|Y_n^{u}, M_n = 0, \theta). \]

Here we denote \( p(Y_{n}^{u}|M_n = 0, \theta) \) and \( p(X_{n}^{u,o}|Y_n^{u}, M_n = 0, \theta) \) by parameters

\[ p(Y_{n}^{u}|M_n = 0, \theta) = \pi_{0}^{Y_{n}^{u}} \]
\[ p(X_{n}^{u,o}|Y_n^{u}, M_n = 0, \theta) = \gamma_{o} \cdot \pi_{0}^{X_{n}^{u,o}} + (1 - \gamma_{o}) \cdot \delta_{X_{n}^{u,o} = Y_n^{u}} \]

according to the F81 model, where the base distribution of each position of the background sequence is denoted by \( \pi_{0} \), the probability of a nucleotide \( a \) in the background sequence is denoted by \( \pi_{0}^{a} \), and the substitution probability from the primordial species to species \( o \) is denoted by \( \gamma_{o} \).

Likelihood of a motif-bearing alignment

In the data generating process for motif-bearing alignments we sample alignments until one of them is accepted. Mapping this into a likelihood requires the usage of the Felsenstein’s pulley principle Felsenstein, 1981, that allows us to select any particular species as the root of the tree. In this case it will come handy to select the reference species as the root. Thus, the likelihood can be expressed as

\[ p(X_n|M_n = 1, \theta) = \sum_{\ell_n = 1}^{L_n-W+1} p(X_{n}^{1}|M_n = 1, \ell_n) \sum_{Y_n \in A} p(Y_n|M_n = 1, \ell_n) \prod_{o=2}^{O} p(X_{n}^{o}|Y_n, M_n = 1, \ell_n)p(\ell_n|M_n = 1, \theta), \]

where the base distributions of the positions 1, \ldots, \( W \) of the binding sites are denoted by \( \pi_{1}, \ldots, \pi_{W} \) and the probability of a nucleotide \( a \) in the binding site at position \( w \) is denoted by \( \pi_{w}^{a} \).
7.1 Detecting and correcting the binding-affinity bias in ChIP-Seq data using inter-species information

Given \( \pi, \ell_n \in \{1, \ldots, L_n - W + 1\} \), and \( M_n = 1 \), each single nucleotide alignment is independent of any other single nucleotide alignment, and we obtain

\[
p(X_n|M_n = 1, \theta) = \sum_{\ell_n=1}^{L_n-W+1} \prod_{u=1}^{L_n} p(X_{n}^{u,1}|M_n = 1, \ell_n) \cdot \sum_{Y_n \in \mathcal{A}} \prod_{o=2}^{O} p(X_{n}^{u,o}|Y_n, M_n = 1, \ell_n) p(\ell_n|M_n = 1, \theta).
\]

We need to determine the probability of a particular nucleotide in a specific position of the reference species after selection, that is \( p(X_{n}^{u,1}|M_n = 1, \ell_n) \). On one hand, notice that selection does not affect the probability distribution of those nucleotides outside the binding site. Thus, for \( u < \ell_n \) or \( u \geq \ell_n + W \) we have that \( p(X_{n}^{u,1} = a|M_n = 1, \ell_n) = \pi^a_0 \). On the other hand, for nucleotides in the binding site, the distribution after filtering is \( p(X_{n}^{u,1} = a|M_n = 1, \ell_n) \propto (\pi^a_{u-\ell_n+1})^\beta \). Thus, \( p(X_{n}^{u,1} = a|M_n = 1, \ell_n) = \frac{(\pi^a_{u-\ell_n+1})^\beta}{\sum_{b \in \mathcal{A}} (\pi^b_{u-\ell_n+1})^\beta} \).

The probabilities for the nucleotides in the ancestral sequence and in the non-reference species are given by the F81 model. In particular, for the ancestral sequence

\[
p(Y_n = a|X_{n}^{u,1} = b, M_n = 1, \ell_n) = \begin{cases} 
\gamma_1 \cdot \pi^a_0 + (1 - \gamma_1) \cdot \delta_{a=b} & \text{if } u < \ell_n \text{ or } u \geq \ell_n + W \\
\gamma_1 \cdot \pi^a_{u-\ell_n+1} + (1 - \gamma_1) \cdot \delta_{a=b} & \text{if } \ell_n \leq u < \ell_n + W
\end{cases}
\]

and for the non reference species

\[
p(X_{n}^{u,o} = a|Y_n = b, M_n = 1, \ell_n) = \begin{cases} 
\gamma_o \cdot \pi^a_0 + (1 - \gamma_o) \cdot \delta_{a=b} & \text{if } u < \ell_n \text{ or } u \geq \ell_n + W \\
\gamma_o \cdot \pi^a_{u-\ell_n+1} + (1 - \gamma_o) \cdot \delta_{a=b} & \text{if } \ell_n \leq u < \ell_n + W
\end{cases}
\]

Finally, since we assume binding sites to be uniformly distributed, we have that \( p(\ell_n|M_n = 1, \theta) = \frac{1}{\ell_n-W+1} \). This completes the specification of the likelihood function.
7.2 Unrealistic phylogenetic trees may improve *phylogenetic footprinting*

The supplementary material of “Unrealistic phylogenetic trees may improve phylogenetic footprinting” consists of one additional file that contains Supplementary Methods, Results, Figures, and Examples. This file comprises five sections. In **Section 1**, *Accuracy of predicted motifs*, we scrutinize the motifs obtained by PFM with a substitution probability of \( \gamma = 1.0 \). **Section 2**, *Likelihood, classification performance, and difference logos for 5 transcription factors*, contains supplementary Figures to the studies on the five TFs presented in the main manuscript. In **Section 3**, *Comparison of classification performances of PFM basing on five different phylogenetic trees*, we extend the study presented in the main manuscript and compare the classification performance on the five PFM \( M_{\text{tree}}^\gamma \), \( M_{\text{ML}}^\gamma \), \( M_{\gamma=1.0}^\gamma \), \( M_{\gamma}^\text{free} \), and \( M_{\gamma}^\text{star} \). In **Section 4**, *Synthetic tests*, we provide exemplary studies on synthetic data. **Section 5**, *Supplementary Tables*, comprises tables regarding related phylogenetic footprinting approaches, dataset statistics, and P-values for the in the main manuscript presented results. Here, I provide a copy of **Section 1** and **Section 3**.

### 7.2.1 Accuracy of predicted motifs

In the main manuscript, we show that on real data PFM basing on unrealistic substitution probabilities (unrealistic PFM) outperform PFM basing on realistic substitution probabilities (realistic PFM) in contrast to synthetic data where realistic PFM outperform unrealistic PFM. Here, we investigate the degree of similarity between the motifs inferred with realistic PFM and unrealistic PFM in two studies. First, on synthetic data, we compare the accuracy of inferred motifs for different combinations of substitution probabilities used for data generation and for motif inference. Second, on real data, we compare the motif similarity of the motif inferred using an unrealistic PFM to the motifs inferred using more realistic PFM.

#### 7.2.1.1 Test on synthetic data

We study on synthetic data to which amount different substitution probabilities for data generation and different substitution probabilities for the inference of a PFM affect the accuracy of de-novo motif prediction. We generate synthetic datasets basing on different substitution probabilities and we infer on each synthetic dataset a set of PWMs using PFM basing different substitution probabilities as follows.

First, we generate for each substitution probability \( \alpha = \{0.1, 0.2, \ldots, 1.0\} \) a dataset consisting of \( N = 1000 \) motif alignments of length \( W = 10 \) each with \( O = 5 \) species. The set of
7.2 Unrealistic phylogenetic trees may improve phylogenetic footprinting

Ancestor sequences is sampled from a \( \text{PWM} \pi \) of length \( W \) whose probability distribution is generated randomly. Each ancestor sequence is mutated using the F81 model with a star topology with all \( O \) substitution probabilities set to \( \alpha \).

Second, for each generated dataset we estimate for each substitution probability \( \gamma = \{0.1, 0.2, \ldots, 1.0\} \) a \( \text{PFM} \) with a star topology with all substitution probabilities set to \( \gamma \). For each estimated \( \text{PFM} \) we extract the PWM \( \hat{\pi}_\gamma \) and quantify the dissimilarity between \( \hat{\pi}_\gamma \) and \( \pi \) by the symmetric Kullback—Leibler divergence (KLD). A KLD equal to 0 indicates identical PWMs \( \hat{\pi}_\gamma \) and \( \pi \). The KLD is proportional to the degree of dissimilarity between the PWMs \( \hat{\pi}_\gamma \) and \( \pi \).

We repeat both steps 50 times and determine the mean KLD for each combination of \( \alpha \in \{0.1, 0.2, \ldots, 1.0\} \) and \( \gamma \in \{0.1, 0.2, \ldots, 1.0\} \). In Figure 7.1 we show the mean KLD for each combination of \( \alpha \) and \( \gamma \).

Figure 7.1: Motif accuracy for different combinations of substitution probabilities used for data generation and substitution probabilities used for motif inference.

We represent the datasets generated with a star topology with substitution probabilities set to \( \alpha = \{0.1, 0.2, \ldots, 1.0\} \) in the rows. We represent the \( \text{PFMs} \) basing on substitution probabilities \( \gamma = \{0.1, 0.2, \ldots, 1.0\} \) in the columns. For each combination of \( \alpha \) and \( \gamma \), we specify the mean KLD of the true and the estimated motif and we visualize these values with the background color from green (similar) to red (dissimilar). For each row, we find the smallest KLD for \( \alpha = \gamma \) and we find highly similar results for \( \gamma = 1.0 \).

For each dataset we find minimal KLDs for the PWM \( \hat{\pi}_{\gamma=\alpha} \) and the PWM \( \hat{\pi}_{\gamma=1.0} \). With other words, the motifs inferred with a \( \text{PFM} \) basing on a substitution probabilities with \( \gamma \) equal to \( \alpha \) (the substitution probability that was used for data generation) and the motifs inferred with a \( \text{PFM} \) basing on substitution probabilities \( \gamma \) equal to 1.0 (which implies conditional independence between sequences) are highly similar. The KLDs of the PWMs
\( \hat{\pi}_\gamma \) with \( \gamma \neq \alpha \) and \( \gamma \neq 1.0 \) are greater than or equal to the KLDs for the PWMs \( \hat{\pi}_{\gamma=\alpha} \) and \( \hat{\pi}_{\gamma=1.0} \) in every case.

### 7.2.1.2 Test on real data

In the previous study on synthetic data we have shown that the PWM inferred using the most realistic PFM \( \hat{\pi}_{\gamma=\alpha} \) and the PWM inferred using the most unrealistic PFM \( \hat{\pi}_{\gamma=1.0} \) are most similar. We study whether this relationship is also true in case of real data. In case of real data we do not know the true \( \alpha \), i.e., the substitution probability between the ancestor species and the observed species–specific sequences. Hence, we compare the PWM \( \hat{\pi}_{1.0} \) with the PWMs \( \hat{\pi}_\gamma \) for \( \gamma \in \{0.0, 0.1, \ldots, 1.0\} \). Again, we quantify the dissimilarity between \( \hat{\pi}_{1.0} \) and \( \hat{\pi}_\gamma \) by the symmetric KLD.

For each of the five TFs described in Methods 1 and each decomposition of the 100–fold stratified repeated random sub–sampling validation procedures described in Methods 4, we calculate the KLDs of the PWM \( \hat{\pi}_{1.0} \) and the PWMs \( \hat{\pi}_\gamma \) for \( \gamma \in \{0.05, 0.1, \ldots, 1.0\} \) inferred on the positive training dataset. We compute mean and standard error of the resulting 100 KLDs for each pair of the the PWM \( \hat{\pi}_{1.0} \) and the PWMs \( \hat{\pi}_\gamma \). We show mean and standard error of the KLDs as function of \( \gamma \) in Figure 7.2 for each of the five TFs. Based on the previous study and the results presented by Gertz et. al 2006 (Gertz et al., 2006), we expect a local minimum of the KLDs for \( 0.1 < \gamma \leq 0.4 \).

We find for each TF a local minimum of the KLD between the PWM \( \hat{\pi}_{1.0} \) and the PWM \( \hat{\pi}_\gamma \) for realistic substitution probabilities \( 0.1 < \gamma \leq 0.4 \) (\( \gamma = 0.35 \) for CTCF, \( \gamma = 0.3 \) for GABP, \( \gamma = 0.25 \) for NRSE, \( \gamma = 0.4 \) for SRF, \( \gamma = 0.35 \) for STAT1). For \( \gamma \) smaller than these minimums the KLD increases monotonically and for \( \gamma \) greater than these minimums the KLD first increases, reaches a local maximum for \( 0.6 \leq \gamma \leq 0.7 \), and again decreases for \( \gamma \) greater this local maximum (with a KLD equal to zero for \( \gamma = 1.0 \) per definition). In accordance to the results on synthetic data, we show that the motifs inferred using a PFM basing on unrealistic substitution probabilities are similar to the motifs inferred using a PFM basing on realistic substitution probabilities. Since the true substitution probabilities are not known in case of real data, the estimation of motifs using an unrealistic PFM is a potential more robust way to avoid errors from falsely estimated substitution probabilities, i.e., unrealistic PFMs seem to be more robust against model violations in the dataset.

### 7.2.2 Synthetic tests

In the main manuscript, we show that PFMs with unrealistic substitution probabilities outperform realistic PFMs on real data in contrast to synthetic data. Here, we investigate
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Figure 7.2: Motif dissimilarity between $\hat{\pi}_{1.0}$ and $\hat{\pi}_\gamma$ for CTCF, GABP, NRSF, SRF, and STAT1. For each TF, we plot the mean and standard error of the KLD between the PWM $\hat{\pi}_{1.0}$ and the PWMs $\hat{\pi}_\gamma$ with $\gamma = \{0.05, 0.1, \ldots, 1.0\}$ (green line). In addition, we plot the mean and standard error of the likelihood of the corresponding PFMs (red line). We find for the KLD a local minimum for $0.1 < \gamma \leq 0.4$ in every case. We find for the likelihoods a global maximum for $0.1 < \gamma \leq 0.4$ in every case (red cross).
the influence of various data properties on classification performance in order to reproduce this observation on synthetic data.

We generate synthetic datasets as described in Methods 2 and modify this procedure in different ways as follows. We vary the ratio of the size of positive and negative test data in section 7.2.2.1, we use different trees for data generation instead of a star in section 7.2.2.2, we model heterogeneity during data generation in section 7.2.2.3, we use the more realistic HKY evolutionary model instead of the F81 model for data generation in section 7.2.2.4, and we use different trees in combination with the more realistic HKY evolutionary model for data generation in section 7.2.2.5. All datasets are available at https://github.com/mgledi/PhyFoo/tree/master/data/synthetic_data/.

We apply the PFMs described in Methods 1 on each of the generated datasets with varying substitution probability $\gamma$ of the PFMs from 0.05 to 1.0 with increments of 0.05 as described in Methods 3. We study the classification performance of the PFMs by the method described in Methods 4.

7.2.2.1 Unbalanced positive and negative test data
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Figure 7.2: Classification performance for different substitution probabilities on synthetic data. We plot classification performance on synthetic data for a PFM using a star topology with all substitution probabilities set to $\gamma \in \{0.05, 0.1, \ldots, 1.0\}$, where the ratio between positive and negative test data is chosen as 1:1, 1:2, 1:3, 1:4, 1:5, 1:6, 1:7, and 1:8 respectively. The classification performance behaves as expected.
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7.2.2.2 Using trees for data generation

Tested data generation with the following three trees with five species each and all branches having the length $\gamma = 0.2$. Find below the Newick representation of the trees and the corresponding visualisation Fredslund, 2006.

Unbalanced binary tree:

```
( ( ( SPECIES_0:0.2 , SPECIES_1:0.2 ) :0.2 , SPECIES_2:0.2 ) :0.2 , SPECIES_3:0.2 ) :0.2 , SPECIES_4:0.2
```

Balanced binary tree:

```
( ( SPECIES_0:0.2 , SPECIES_1:0.2 ) :0.2 , SPECIES_2:0.2 ) :0.2 , ( SPECIES_3:0.2 , SPECIES_4:0.2 ) :0.2
```
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Balanced ternary tree:

```
( (SPECIES_0:0.2, SPECIES_1:0.2):0.2, 
  (SPECIES_2:0.2, SPECIES_3:0.2, SPECIES_4:0.2):0.2 
):0.2
```

Figure 7.3: Classification performance for different substitution probabilities on synthetic data. We plot classification performance on synthetic data for a PFM using a star topology with all substitution probabilities set to $\gamma \in \{0.05, 0.1, \ldots, 1.0\}$, where the data was generated using (i) an unbalanced binary tree, (ii) a balanced binary tree, and (iii) a balanced ternary tree respectively (trees shown above). The classification performance behaves as expected.
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7.2.2.3 Heterogeneity

Tested data generation with three different combinations of heterogeneity. In case of enabled heterogeneity for motif generation each position in each binding-site is generated using an individual star topology with each substitution probability drawn individually from $\text{beta}(3,10)$. In case of enabled heterogeneity for background and flanking region every position in the alignments that does not correspond to a binding site is generated using an individual star topology with each substitution probability drawn individually from $\text{beta}(3,10)$.

Figure 7.4: Classification performance for different substitution probabilities on synthetic data. We plot classification performance on synthetic data for a PFM using a star topology with all substitution probabilities set to $\gamma \in \{0.05, 0.1, \ldots, 1.0\}$, where the data was generated using heterogenous substitution probabilities (i) only in the background and flanking regions, (ii) only in the binding sites, and (iii) in the background, the flanking regions, and the binding sites respectively. The classification performance behaves as expected.

7.2.2.4 Using HKY model for data generation

Tested data generation using HKY model with two different combinations of transversion and transition probability.
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![Figure 7.5: Classification performance for different substitution probabilities on synthetic data.](image)

We plot classification performance on synthetic data for a PFM using a star topology with all substitution probabilities set to $\gamma \in \{0.05, 0.1, \ldots, 1.0\}$, where the data was generated using the HKY evolutionary model with (i) $\alpha = 0.4$ and $\beta = 0.2$ and (ii) $\alpha = 0.2$ and $\beta = 0.4$ respectively. The classification performance behaves as expected.

7.2.2.5 Using more complex phylogenetic trees with HKY model for data generation

Tested data generation using three different trees with the HKY model with two different combinations of transversion and transition probability.
Figure 7.6: Classification performance for different substitution probabilities on synthetic data. We plot classification performance on synthetic data for a PFM using a star topology with all substitution probabilities set to $\gamma \in \{0.05, 0.1, \ldots, 1.0\}$, where the data was generated using the HKY evolutionary model with (Ai) $\alpha = 0.4$ and $\beta = 0.2$ and (Aii) $\alpha = 0.2$ and $\beta = 0.4$ in combination with (Bi) an unbalanced binary tree, (Bii) a balanced binary tree, and (Biii) a balanced ternary tree respectively (trees shown above). The classification performance behaves as expected.
7.3 Combining *phylogenetic footprinting* with motif models incorporating intra-motif dependencies

The supplementary material of “Detecting and correcting the binding-affinity bias in ChIP-seq data using inter-species information” consists of five additional files. **Additional File 1** contains for each of the 35 TFs a $10 \times 10$ table of difference logos for a pair-wise visual comparison of species-specific motifs. **Additional File 2** contains for each of the 35 TFs the sequence logo inferred using the PFM(2) aligned with mutual information profiles of order 1, the mutual information profiles of order 2, and species-specific mutual information profiles of orders 1 and 2 for each of the 10 species. **Additional File 3** contains sequence logos and their reverse complements of predicted binding sites inferred using the PFM(0), the PFM(1) and the PFM(2) for each of the 35 TFs. **Additional File 4** contains for each TF two plots showing the 25 ROC curves and the 25 PR curves from the 25-fold stratified repeated random sub-sampling validation procedure described in **Methods 3**. **Additional File 5** This file contains three supplementary sections, presenting four additional studies, details about the implementation and some statistics regarding the datasets of all 35 TFs. **Additional File 6** contains data files of alignments of the ChIP-seq positive regions and negative control regions for each of the 35 TFs in FASTA format.

Here, we show **Section 1.1** and **Section 1.3** of **Additional File 5**. In the first subsection (former section 1.1), we study differences among species–specific motifs of 35 TFs. In the second subsection (former section 1.3), we examine the impact of base dependencies and phylogenetic dependencies on classification performance.

7.3.1 Species–specific motifs are highly similar for most TF

Intra-motif dependencies may be a constant phenomenon conserved across the examined species or a rather dynamic phenomenon significantly changing during the evolution of these species. The latter case may imply that species–specific motifs are different to a certain degree. Consequently, the estimation of base dependencies across species may result in the estimation of spurious results. Hence, **first** we visually study differences among the species–specific motifs of each of the 35 TFs using difference logos, **second** we determine whether observable differences between species–specific motifs are significant or not, and **third** we examine the distribution of position-specific MIs for each species. Therefore, we extracted for each of the 35 TFs one motif for each of the 10 species resulting in $35 \times 10$ species–specific motifs as described in **Supplementary Section 2.1**. Please note that the extracted species–specific motifs for other species than the reference species are not representative for these phylogenetically related species.
7. APPENDIX

7.3.1.1 Primates show almost no differences in their sequence logos

We use the freely available R package DiffLogo for the visual inspection of motif differences. DiffLogo enables the illustration and investigation of differences between highly similar motifs such as binding motifs of TFs from different experiments, different motif prediction algorithms, or different species. Hence, we use tables of difference logos generated with DiffLogo for a pair-wise comparison of all species-specific motifs. Each difference logo displays position-specific differences of base distributions by a stack of bases which height is proportional to the base distribution difference quantified by the Jensen-Shannon divergence. The Jensen-Shannon divergence is zero in case of two identical base distributions and 1 in case of two maximally different base distributions. The tables of difference logos for all 35 TFs can be found in Additional File 1. All sequence logos of PFM(0), PFM(1), and PFM(2) can be found in Additional File 3.

Exemplary, Supplementary Figure 7.7 shows the table of difference logos for the TF Bach1. We find that the species-specific motifs segregate into two main groups, where one group comprises seven higher primates and the second group comprises three species from the Laurasiatheria superorder, i.e., dog, horse, and cow. We find differences between the motifs of both groups at various motif positions, where the motif differences of relatively high degree are located at rather conserved motif positions as well as at more variable motif positions. For instance, we find relatively high differences at motif position 8, where guanine is more abundant in the primate motifs and the remaining bases are more abundant in the Laurasiatheria motifs. However, the maximum Jensen-Shannon divergence in all difference logos for Bach1 is below 0.01 bits.

We examine the motif differences between species-specific motifs for all 35 TFs. We see for 14 TFs that the set of ten species segregates into the two groups of seven higher primates and three from the Laurasiatheria clade as before in case of Bach1 (CEBPB, CTCF, EGR1, MafK, Max, NRSF, POU5F1, Rad21, SRF, TCF12, TEAD4, USF1, USF2, YY1). We find for the remaining 21 TFs that the motifs of the seven higher primates are more similar to each other compared to the motifs of dog, horse, and cow. With other words, in these cases the pairwise difference logos of dog, horse, and cow do not form a second cluster. The differences observed among species-specific motifs could partly result from missing binding sites in some species. Supplementary Table S6 shows for each species and for each TF the proportion of sequences which are available for the computation of species-specific motifs.
7.3 Combining phylogenetic footprinting with motif models incorporating intra-motif dependencies

Figure 7.7: Comparison of species-specific motifs for the TF Bach1. We depict a table of difference logos with one row and one column for each species-specific motif to emphasize the differences between species-specific motifs. Each difference logo depicts the motif differences position-wise with a stack of bases, which height is calculated by the Jensen-Shannon divergence of the position-specific base distributions. The overall similarity between species-specific motifs is calculated by the sum of Jensen-Shannon divergences of all motif positions and depicted by the background color of the difference logos from green (similar) to red (dissimilar). The table of difference logos indicates, that the ten species-specific Bach1 motifs primarily segregate into two clusters, where one cluster comprises seven primates and the other cluster comprises three non-primates (cow, dog, and horse).

7.3.1.2 Species–specific motifs are typically highly similar

We study the statistical significance of differences between species–specific motifs as follows. We examine for each of the 35 TFs the similarity of species–specific motifs using a statistical test for each two species \((10 \times 9)/2 = 45\) species pairs. We calculate for each TF and for each two species the p-value for the null hypothesis that two species–specific motifs arise from the same distribution as described in Supplementary Section 2.2 resulting in \(35 \times 45 = 1575\) pairwise comparisons. We count for each two species how often we reject the null hypothesis for a confidence level of \(\alpha = 0.05\). These counts range from 0 to 35,
where 0 means that the species-specific motifs of two species show no significant differences for each transcription factor and 35 means that the species-specific motifs of two species show significant differences for each transcription factor. The binary nature of the results of statistical tests can lead to the issue that comparisons between three species are not transitive, i.e., if there are no significant differences between the species-specific motifs of species A and B and there are no significant differences between the species-specific motifs of species B and C it can happen that there are significant differences between the species-specific motifs of species A and C.

Supplementary Table S3 shows the results for each pair of species. We find that the seven primate-specific motifs are highly similar to each other and that the three species-specific motifs of cow, dog, and horse show greater differences compared to those of the seven primates. Using a significance level of 95%, we expect 5% of all 1575 pairwise differences to be significant by chance. We find for only 47 of 1575 pairwise comparisons that two species-specific motifs show significant differences. However, we find only 47 (3%) of the pairwise differences to be significant, stating that the observed differences are not greater than expected by chance.

Specifically, we find that these 47 cases apply only to 6 of the 35 TFs, namely Bach1, CEBPB, MafK, Max, SP1, and USF1 and typically only apply to comparisons between a primate species and one of the species dog, cow, and horse. We find no significant differences between the seven primates reflecting the close phylogenetic relationship and accordingly the high sequence similarity. Amongst the three species dog, cow, and horse we find for 1 of the 105 pairwise comparisons significant differences.

These results imply that the motifs estimated across species as presented in the previous section are typically not a mixture of species-specific motifs.

7.3.1.3 Intra-motif dependencies are highly similar for all species

We examine for each of the 35 TFs the distribution of species-specific MIs using mutual information profiles $I^S_1$ and $I^S_2$ as described in Methods 4 for each species $S \in \{ hg19, panTro, papHam, ponAbe, rheMac, calJac, equCab, canFam, gorGor, bosTau \}$. Figure 7.8 shows two examples of species-specific mutual information profiles $I^S_1$ and $I^S_2$ for the two TFs CJUN and Nrf. All species-specific mutual information profiles are available in Additional File 2.

First, we study the species-specific mutual information profiles $I^S_1$. We find for each of the 35 TFs that the species-specific mutual information profiles $I^S_1$ are highly similar for all species. We also find that the MIs in the mutual information profiles $I_1$ are sometimes stronger, sometimes weaker, and often averaged compared to the species-specific MIs $I^S_1$. 

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7.3 Combining phylogenetic footprinting with motif models incorporating intra-motif dependencies

Figure 7.8: Sequence logos and intra-motif dependencies for the TFs (left) CJUN and (right) Nrf. We depict for both TFs (i) the sequence logo inferred by the PFM(2) from all species in the first row, (ii) the species-specific mutual information profiles inferred from the PFM(1) in the second row, and (iii) the species-specific mutual information profiles inferred from both models are highly similar to each other.

implying that the mutual information profiles $I_1$ inferred from all species are partly a result of interference of species-specific MIs. For example, in case of TF CJUN at motif positions $w \in \{2, 3, 4\}$, the MIs $I_1(w)$ are smaller than the MIs $I_1^S(w)$ for all species except horse and marmoset and in case of TF Nrf at motif positions $w \in \{8, 9, 10, 11\}$ the MIs $I_1(w)$ are higher than the MIs $I_1^S(w)$ for all species. Specifically, we find the largest difference between two $I_1^S$ for FOSL1 with 0.35 bits. However, the mutual information profiles $I_1$ inferred from all species are typically highly similar to the species-specific mutual information profiles $I_1^S$.

Second, we examine species-specific mutual information profiles $I_2^S$. We find for each of the 35 TFs that the species-specific mutual information profiles $I_2^S$ are highly similar for all species. We also find that the MIs in the mutual information profiles $I_2$ are sometimes stronger, sometimes weaker, and sometimes averaged compared to the species-specific MIs
II S implying that the mutual information profiles I2 inferred from all species are partly a result of interference of species-specific MIs. For example, in case of CJUN the mutual information profile I2(w) is typically smaller than the mutual information profile II S 2(w) for all species at all motif positions w and in case of Nrf at motif positions w ∈ {8−11} the MIs I2(w) are higher than the MIs II S 2(w). Specifically, we find the largest difference between two II S 2 for FOSL1 with 0.48 bits. However, the mutual information profiles I2 inferred from all species are typically highly similar to the species-specific mutual information profiles II S 2 as in case of I1 and II S 1.
7.3 Combining phylogenetic footprinting with motif models incorporating intra-motif dependencies

7.3.2 Taking into account phylogeny improves classification performance in almost all cases.

It has been shown that taking into account base dependencies improves one-species approaches neglecting phylogenetic dependencies and it has been shown that taking into account phylogenetic dependencies can improve one-species approaches neglecting base dependencies. In the manuscript we have shown that taking into account base dependencies improves phylogenetic footprinting. Unfortunately, it can not be concluded from these observations that a model taking into account base dependencies and phylogenetic dependencies outperforms a model taking into account base dependencies but neglecting phylogenetic dependencies, because phylogenetic dependencies may potentially impair the model taking into account base dependencies.

Here, we systematically study the impact of both higher order base dependencies and phylogenetic dependencies to classification performance. Therefore, we study the performances of four different models, namely i) a model taking into account neither base dependencies nor phylogenetic dependencies (human(0)), ii) a model taking into account base dependencies of order 2 and neglecting phylogenetic dependencies (human(2)), iii) a model neglecting base dependencies and taking into account phylogenetic dependencies PFM(0), and iv) a model taking into account both base dependencies and phylogenetic dependencies PFM(2) as described in Methods 2. The models PFM(0) and PFM(2) take into account phylogenetic dependencies and are inferred from the alignments described in Methods 1. The models human(0) and human(2) do not take into account phylogenetic dependencies and are inferred from the human sequences of the alignments described in Methods 1. The models human(0) and human(2) are special cases of PFM(0) and PFM(2) incorporating only one species.

Based on these four models we perform all pair-wise comparisons, namely a) human(0) against human(2), b) human(0) against PFM(0) c) PFM(0) against PFM(2) d) human(2) against PFM(2) e) human(0) against PFM(2) and f) human(2) against PFM(0).

For case a), it has been shown that human(2) typically outperforms human(0), i.e., that modeling base dependencies improves classification performance. For case b), it has also been shown that PFM(0) typically outperforms human(0), i.e., modeling phylogenetic dependencies improves classification performance. For case c), we have shown that PFM(2) outperforms PFM(0), i.e., that taking into account higher order base dependencies improves phylogenetic footprinting. For case e) we assume that PFM(2) outperforms human(0) considering the cases a) and b). The cases d) and f) are unknown so far.

We measure the classification performance of all four models as described in Methods 3 on datasets of 35 TFs. Figure 7.9 shows the corresponding values for the four models human(0), PFM(0), human(2), and PFM(2) for each of the 35 TFs. See Supplementary
Table S4 and Supplementary Table S5 for statistics of the results shown in Supplementary Figure 7.9.

It is not surprising that the model taking into account both base dependencies and phylogenetic dependencies outperforms the model ignoring base dependencies and phylogenetic dependencies (case e). We find that modeling base dependencies typically improves classification performance (cases a and c). Interestingly, we find that modeling base dependencies clearly outperforms modeling phylogenetic dependencies (case f). In fact, solely taking into account phylogenetic dependencies shows only a partial improvement (case b), but taking into account both phylogenetic dependencies and base dependencies shows a clear performance improvement compared to solely taking into account base dependencies (case d). These results suggest that phylogenetic footprinting approaches benefit from taking into account base dependencies and that approaches on single species already taking into account base dependencies benefit from taking into account phylogenetic dependencies.

Figure 7.9: Classification performance of the models human(0) and human(2) on human sequences and [PFM(0)] and [PFM(2)] on alignments of ten species for each of the 35 TFs. We show the mean and standard error of the ROC AUC. See Table S4 and Table S5 for summary statistics.
7.3 Combining *phylogenetic footprinting* with motif models incorporating intra-motif dependencies

Figure 7.10: Classification performance of the two models PFM(0) and PFM(2) incorporating phylogenetic dependencies for each of the 35 TFs. We show the mean and standard error of the relative increase of ROC AUC of (top) PFM(0) relative to the classification performance of human(0) and (bottom) PFM(2) relative to the classification performance of human(2). Typically both models show a higher classification performance.
Figure 7.11: Classification performance of the two models human(2) and PFM(2) incorporating base dependencies of order two for each of the 35 TFs. We show the mean and standard error of the relative increase of ROC AUC of (top) human(2) relative to the classification performance of human(0) and (bottom) PFM(2) relative to the classification performance of PFM(0). Typically both models show a higher classification performance.
7.4 DiffLogo: A comparative visualisation of sequence motifs

The supplementary material of “DiffLogo: a comparative visualization of sequence motifs” consists of one additional file that contains Supplementary Methods, Results, Figures, and Examples. This file comprises four sections. Section 1, Additional examples, contains Figures S1 and S2. In Section 2, CTCF with and without clustering, we show in detail the impact of clustering and optimal leaf ordering for a DiffLogo grid of nine CTCF motifs. In Section 3, Alternative combinations of stack heights and symbol weights, we describe the mathematical background of four implementations of $H_\ell$ and two implementations of $r_{\ell,a}$ and show an exemplary comparison of the eight combinations. In Section 4, Tool comparison, we compare DiffLogo with the five tools seqLogo, iceLogo, MotifStack, STAMP, and Two Sample Logo. Here, I provide a copy of Section 3.

7.4.1 Alternative combinations of stack heights and symbol weights

We consider two motifs represented by two PWMs $p$ and $q$. The height of symbol $a$ in the symbol stack at position $\ell$ of the difference logo is denoted $H_{\ell,a}$ and given by

$$H_{\ell,a} = r_{\ell,a} \cdot H_\ell,$$

where $H_\ell$ represents the height of the symbol stack at position $\ell$ and the weight $r_{\ell,a}$ represents the proportion of symbol $a \in \mathcal{A}$ in the symbol stack at position $\ell$, where $\mathcal{A}$ is the alphabet. We calculate $H_{\ell,a}$ for different measures $H_\ell$ and $r_{\ell,a}$ to emphasize different facets of distribution differences. We propose various alternatives to calculate the measures $H_\ell$ and $r_{\ell,a}$ as follows (illustrated in supplementary Table S1).

In the following sections, the information content of a PWM $p$ at position $\ell$ is denoted $H^p_\ell$ and given by

$$H^p_\ell = \log_2(|\mathcal{A}|) - \sum_{a \in \mathcal{A}} p_{\ell,a} \cdot \log_2(p_{\ell,a}),$$

where $p_{\ell,a}$ is the probability of symbol $a$ at position $\ell$ in PWM $p$. $H^q_\ell$ is defined analogously.

7.4.1.1 Different calculations of stack heights $H_\ell$

Jensen–Shannon divergence
The Jensen–Shannon divergence is a measure for the difference of two probability distributions based on information theory. The Jensen–Shannon divergence at position $\ell$ is denoted by $H^{(i)}_\ell$ and given by
\[
H^{(i)}_\ell = \frac{1}{2} \sum_{a \in A} p_{\ell,a} \left( \log_2(p_{\ell,a}) - \log_2(m_{\ell,a}) \right) + \frac{1}{2} \sum_{a \in A} q_{\ell,a} \left( \log_2(q_{\ell,a}) - \log_2(m_{\ell,a}) \right),
\]
where $m_{\ell,a} = \frac{1}{2}(p_{\ell,a} + q_{\ell,a})$. $H^{(i)}_\ell$ is symmetric and limited to $[0, 1]$. This measure especially emphasizes large distribution differences.

**Change of information content (stack)**

The change of information content (stack) is a measure for the absolute change of information content between two probability distributions. The change of information content (stack) at position $\ell$ is denoted by $H^{(ii)}_\ell$ and given by
\[
H^{(ii)}_\ell = \sum_{a \in A} |p_{\ell,a} H^{p}_\ell - q_{\ell,a} H^{q}_\ell|.
\]
$H^{(ii)}_\ell$ is symmetric and limited to $[0, 2 \log_2(|A|)]$. This measure especially emphasizes large changes of information content.

**Relative change of information content**

The relative change of information content is a measure for the absolute change of information content relative to the average information content of the two probability distributions. The relative change of information content at position $\ell$ is denoted by $H^{(iii)}_\ell$ and given by
\[
H^{(iii)}_\ell = \begin{cases} 
\sum_{a \in A} |p_{\ell,a} H^{p}_\ell - q_{\ell,a} H^{q}_\ell| & \text{if } p_{\ell} \neq q_{\ell} \\
0 & \text{otherwise.}
\end{cases}
\]
$H^{(iii)}_\ell$ is symmetric and limited to $[0, 2 \log_2(|A|)]$. This measure especially emphasizes large changes of information content relative to the information content of the given distributions.

**Change of probabilities (stack)**
The change of probabilities (stack) is a measure for the absolute change of probabilities between two probability distributions. The change of probabilities (stack) at position $\ell$ is denoted by $H^{(iv)}_{\ell}$ and given by

$$H^{(iv)}_{\ell} = \sum_{a \in A} |p_{\ell,a} - q_{\ell,a}|$$

$H^{(iv)}_{\ell}$ is symmetric and limited to $[0, 2]$. This measure especially emphasizes large changes of probabilities.

### 7.4.1.2 Different calculations of symbol weights $r_{\ell,a}$

#### Change of probability (symbol)

The change of probability (symbol) is a measure for the change of symbol-specific probability relative to the sum of absolute symbol-specific probability differences of the given probability distributions. The change of probability (symbol) of symbol $a$ at position $\ell$ is denoted by $r^{(i)}_{\ell,a}$ and given by

$$r^{(i)}_{\ell,a} = \begin{cases} \frac{p_{\ell,a} - q_{\ell,a}}{\sum_{a' \in A} |p_{\ell,a'} - q_{\ell,a'}|} & \text{if } p_{\ell} \neq q_{\ell} \\ 0 & \text{otherwise.} \end{cases}$$

$r^{(i)}_{\ell,a}$ is antisymmetric and limited to $[-\frac{1}{2}, \frac{1}{2}]$. This measure especially emphasizes a large change of symbol–probability. For each position of the difference logo, the height of the symbol stack with negative measures $r^{(i)}_{\ell,a}$ is equal to the height of the symbol stack with positive measures $r^{(i)}_{\ell,a}$, because each gain of symbol–probability implies a loss of probability for the remaining symbols and vice versa.

#### Change of information content (symbol)

The change of information content (symbol) is a measure for the symbol-specific change of information content relative to the sum of absolute symbol-specific differences of information content of the given probability distributions. The change of information content (symbol) of symbol $a$ at position $\ell$ is denoted by $r^{(ii)}_{\ell,a}$ and given by

$$r^{(ii)}_{\ell,a} = \begin{cases} \frac{p_{\ell,a}H_{p}^{(\ell)} - q_{\ell,a}H_{q}^{(\ell)}}{\sum_{a' \in A} |p_{\ell,a'}H_{p}^{(\ell)} - q_{\ell,a'}H_{q}^{(\ell)}|} & \text{if } p_{\ell} \neq q_{\ell} \\ 0 & \text{otherwise.} \end{cases}$$

$r^{(ii)}_{\ell,a}$ is antisymmetric and limited to $[-1, 1]$. This measure especially emphasizes a large change of symbol-specific information content.
Table 7.1: Exemplary comparison of different stack heights and symbol weights using four artificial DNA motifs of length one.
Eidesstattliche Erklärung / Declaration under Oath

Ich erkläre an Eides statt, dass ich die Arbeit selbstständig und ohne fremde Hilfe verfasst, keine anderen als die von mir angegebene Quellen und Hilfsmittel benutzt und die den benutzten Werken wörtlich oder inhaltlich entnommenen Stellen als solche kenntlich gemacht habe.

_I declare under penalty of perjury that this thesis is my own work entirely and has been written without any help from other people. I used only the sources mentioned and included all the citations correctly both in word or content._

Burgliebenau, 15.05.2017  
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Professional experience

01/2016 – today
Senior Software Engineer Research and Development
Datameer GmbH, Halle
» Development of distributed algorithms
» Development of Elasticsearch plugins

08/2012 – 10/2015
Teamlead Research and Development
Unister GmbH, Leipzig
» Analysis and interpretation of large data sets
» Development of distributed algorithms
» Leading a team of up to six team members

10/2010 – 07/2012
Junior Developer Machine-Learning
Unister GmbH, Leipzig
» Implementation of algorithms for text analysis
» Performance optimization of existing implementations

Developer of the CMS of the MLU Halle/Wittenberg
» Conception and backend development
Publications

Articles


Conference papers


Open source software

- **DRUMS**: Disk repository with update management and select option
  https://github.com/mgledi/DRUMS
- **BioDRUMS**: Example integration of DRUMS for biological data
  https://github.com/mgledi/BioDRUMS
- **DiffLogo**: Comparative visualization of sequence motifs in R
  https://github.com/mgledi/DiffLogo
- **DiffLogoUI**: A webserver for DiffLogo
  https://github.com/mgledi/DiffLogoUI

Burgliebenau, 01.12.2016

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